PREDICTABILITY OF MONTHLY STREAMFLOW DISCHARGE USING REMOTE SENSING PRECIPITATION DATA BY DATA DRIVEN MODELS

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Predictability of stream flow has been the focus of many studies involving water resources management and hydroelectric energy production. Many hydrologic models have been developed to predict future and current streamflow at various time lags and locations. However, these physically-based models require reanalyzed future data sets (particularly precipitation forcing data) to predict future streamflow. Alternatively, data driven models can also provide predictions without the need of future projections by relying on the strong seasonality and autocorrelation that exist in the streamflow data. In this study, a data driven approach has been taken to predict monthly streamflow data sets utilizing precipitation data sets and using various linear and non-linear methods. Streamflow predictions of Coruh Basin have been performed using both the Tropical Rainfall Measurement Mission (TRMM) and the ground-based station precipitation (MGM) data sets between years 2000 – 2011. Predictions are validated using independent streamflow measurements acquired from General Directorate of State Hydraulic Works (DSI). A Simple Linear Regression Model (SLR), a Multiple Linear Regression Model (MLR), an Artificial Neural Network Model (MLP), and two Copula Models (Normal Copula and Frank Copula) are constructed and their predictions are cross-compared with the climatology- and persistence-based predictions. To further investigate the source of the predictive skills of these methods, separate predictions are made using the standardized anomaly
components of data sets [after climatology (long year monthly mean) components are removed and standardized by dividing by the standard deviation of the data] and complete data sets (normal/non-standardized data sets retaining both anomaly and climatology components). Results show the best predictions are obtained from the climatology-based predictions of the stations for the complete data sets while persistence-based predictions are also strong. Predictions using standardized anomaly data sets are improved when long-term climatology values added. These climatology added predictions show above 0.90 correlations, showing heavy majority of the predictive skill and the relation between the precipitation and the streamflow data sets are due to the strong seasonality impacting both variables.

Key Words: Monthly Streamflow Prediction, Rainfall-Runoff Modeling, Copulas, TRMM Data, Artificial Neural Networks (ANN), Climatology, Persistence
ÖZ

VERİ GÜDÜMLÜ YÖNTEMLER İLE UYDU YAĞIŞ VERİLERİ KULLANILARAK AYLIK AKARSU DEBİSİ TAHMİNİ

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iyi sonuçlar akarsu akımının klimatoloji tabanlı tahminlerinden elde edilmiş ve tutarlılık tabanlı akarsu akım tahminlerinin yaklaşık olarak aynı korelasyon değerlerine sahip olduğu gözlemlenmiştir. Uzun yıllar klimatoloji bileşenleri standartlaştırılmış veri setleriyle yapılan tahminlere eklendiğinde, tahminlerde derecede gelişmeler olduğu gözlemlenmiştir. Klimatoloji bileşenlerinin eklenmiş olduğu tahminler, gerçek zamanlı gözlemlerle 0.90 değerinin üzerinde korelasyonlar göstermiştir. Bu durum yağış-akış ilişkisi ve debi tahminlerindeki birincil bileşenin güçlü mevsimsellik etkisi olduğunu göstermiş ve her iki tip veri seti (yağış ve akarsu debisi) içinde bu bileşenin ne kadar etkili olduğunu vurgulamıştır.

Anahtar Kelimeler: Aylık Akarsu Akım Tahmini, Yağış-Akım İlişkisi Modeli, Kopula, TRMM Verileri, Yapay Sinir Ağları Modeli (YSA), Klimatoloji, Tutarlılık
To My Mother…

Anneme…
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# TABLE OF CONTENTS

ABSTRACT ........................................................................................................................... V
ÖZ ........................................................................................................................................... VII
ACKNOWLEDGMENTS ........................................................................................................... X
TABLE OF CONTENTS ........................................................................................................... XI
LIST OF TABLES .................................................................................................................... XIV
LIST OF FIGURES ................................................................................................................ XVIII
ABBREVIATIONS ................................................................................................................. XXIII

CHAPTERS

1. INTRODUCTION ............................................................................................................. 1
  1.1. Problem Definition and Motivation of the Study ....................................................... 1
  1.2. Literature Review ..................................................................................................... 3
    1.2.1. Review on Earlier Studies on Runoff Prediction Methods ................................. 3
    1.2.2. Studies Focusing on Rainfall – Runoff Predictions over Turkey ....................... 8
  1.3. Main Purpose of the Study ....................................................................................... 9

2. METHODOLOGY ................................................................................................................. 11
  2.1. Prediction Models ..................................................................................................... 11
    2.1.1. Linear Regression Model .................................................................................... 15
    2.1.2. Multiple Linear Regression Model .................................................................... 17
    2.1.3. ANN Model ....................................................................................................... 20
    2.1.4. Copula Models .................................................................................................... 24
  2.2. Climatology and Persistence Benchmarks ............................................................... 26
    2.2.1. Climatology ...................................................................................................... 27
    2.2.2. Persistence ........................................................................................................ 28
  2.3. Complete and Standardized Anomaly Data sets Predictions .................................... 29
    2.3.1. Complete Data sets Predictions ........................................................................ 30
    2.3.2. Standardized Anomaly Data Sets Predictions ................................................... 31
  2.4. Study Area ................................................................................................................. 35
3.3.4. Station E23A020

3.3.4.1. Meteorology Data Predictions

3.3.4.2. TRMM Single Pixel Data Predictions

3.3.4.3. TRMM Catchment Average Data Predictions

3.3.5. Station E23A021

3.3.5.1. Meteorology Data Predictions

3.3.5.2. TRMM Single Pixel Data Predictions

3.3.5.3. TRMM Catchment Average Data Predictions

3.3.6. Station E23A023

3.3.6.1. Meteorology Data Predictions

3.3.6.2. TRMM Single Pixel Data Predictions

3.3.6.3. TRMM Catchment Average Data Predictions

3.4. Discussion of Predictions

4. SUMMARY and CONCLUSION

REFERENCES
LIST OF TABLES

Table 2.1 Coruh Basin Upper and Middle Stream Dams.................................40
Table 3.1 Correlations Between MGM Stations and TRMM Data sets ..............57
Table 3.2 Correlations between the DSI Streamflow Observation Stations .................................................................58
Table 3.3 DSI Streamflow Observation Stations Data Statistics and Autocorrelation Values .................................................................59
Table 3.4 Performance Statistics of Station E23A004 with Meteorology Data - Complete Data set Predictions .................................................................62
Table 3.5 Performance Statistics of Station E23A004 with Meteorology Data – Anomaly Component Data set Predictions .................................................................63
Table 3.6 Performance Statistics of Station E23A004 with TRMM Single Pixel Data - Complete Data set Predictions .................................................................65
Table 3.7 Performance Statistics of Station E23A004 with TRMM Single Pixel Data – Anomaly Component Data set Predictions .................................................................66
Table 3.8 Performance Statistics of Station E23A004 with TRMM Catchment Average Data - Complete Data set Predictions .................................................................68
Table 3.9 Performance Statistics of Station E23A004 with Catchment Average Data – Anomaly Component Data set Predictions .................................................................69
Table 3.10 Performance Statistics of Station E23A005 with Meteorology Data - Complete Data set Predictions .................................................................71
Table 3.11 Performance Statistics of Station E23A005 with Meteorology Data – Anomaly Component Data set Predictions .......................................................... 72
Table 3.12 Performance Statistics of Station E23A005 with TRMM Single Pixel Data - Complete Data set Predictions .......................................................... 74
Table 3.13 Performance Statistics of Station E23A005 with TRMM Single Pixel Data – Anomaly Component Data set Predictions .......................................................... 75
Table 3.14 Performance Statistics of Station E23A005 with TRMM Catchment Average Data - Complete Data set Predictions .......................................................... 77
Table 3.15 Performance Statistics of Station E23A005 with Catchment Average Data – Anomaly Component Data set Predictions .......................................................... 78
Table 3.16 Performance Statistics of Station E23A016 with Meteorology Data - Complete Data set Predictions .......................................................... 80
Table 3.17 Performance Statistics of Station E23A016 with Meteorology Data – Anomaly Component Data set Predictions .......................................................... 81
Table 3.18 Performance Statistics of Station E23A016 with TRMM Single Pixel Data - Complete Data set Predictions .......................................................... 83
Table 3.19 Performance Statistics of Station E23A016 with TRMM Single Pixel Data – Anomaly Component Data set Predictions .......................................................... 84
Table 3.20 Performance Statistics of Station E23A016 with TRMM Catchment Average Data - Complete Data set Predictions .......................................................... 86
Table 3.21 Performance Statistics of Station E23A016 with Catchment Average Data – Anomaly Component Data set Predictions .......................................................... 87
Table 3.22 Performance Statistics of Station E23A020 with Meteorology Data - Complete Data set Predictions .......................................................... 89
Table 3.23 Performance Statistics of Station E23A020 with Meteorology Data – Anomaly Component Data set Predictions .......................................................... 90
Table 3.24 Performance Statistics of Station E23A020 with TRMM Single Pixel Data
- Complete Data set Predictions

Table 3.25 Performance Statistics of Station E23A020 with TRMM Single Pixel Data
- Anomaly Component Data set Predictions

Table 3.26 Performance Statistics of Station E23A020 with TRMM Catchment Average Data - Complete Data set Predictions

Table 3.27 Performance Statistics of Station E23A020 with Catchment Average Data
- Anomaly Component Data set Predictions

Table 3.28 Performance Statistics of Station E23A021 with Meteorology Data - Complete Data set Predictions

Table 3.29 Performance Statistics of Station E23A021 with Meteorology Data
- Anomaly Component Data set Predictions

Table 3.30 Performance Statistics of Station E23A021 with TRMM Single Pixel Data
- Complete Data set Predictions

Table 3.31 Performance Statistics of Station E23A021 with TRMM Single Pixel Data
- Anomaly Component Data set Predictions

Table 3.32 Performance Statistics of Station E23A021 with TRMM Catchment Average Data - Complete Data set Predictions

Table 3.33 Performance Statistics of Station E23A021 with Catchment Average Data
- Anomaly Component Data set Predictions

Table 3.34 Performance Statistics of Station E23A023 with Meteorology Data - Complete Data set Predictions

Table 3.34 Performance Statistics of Station E23A023 with Meteorology Data
- Anomaly Component Data set Predictions

Table 3.36 Performance Statistics of Station E23A023 with TRMM Single Pixel Data
- Complete Data set Predictions
Table 3.37 Performance Statistics of Station E23A023 with TRMM Single Pixel Data – Anomaly Component Data set Predictions…………………………………………………………111

Table 3.38 Performance Statistics of Station E23A023 with TRMM Catchment Average Data - Complete Data set Predictions…………………………………………………………113

Table 3.39 Performance Statistics of Station E23A023 with Catchment Average Data – Anomaly Component Data set Predictions…………………………………………………………114

Table 3.40 Summary of the correlations of complete data set predictions with the streamflow validation timeseries………………………………………………………………………………115

Table 3.41 Summary of the correlations of anomaly component data set predictions with the streamflow validation time series………………………………………………………………………………115
LIST OF FIGURES

Figure 2.1 Structure Of The Single Neuron Information Process In The Human Brain………………………………………………………………………………………………13
Figure 2.2 Sample Regression Line and Observed Data Scatter Plot……………15
Figure 2.3 General Layout of an ANN Model ………………………………………20
Figure 2.4 Schematic Diagram of A Single Node in an ANN…………………..21
Figure 2.5 Monthly Climatology Timeseries………………………………………..27
Figure 2.6 Input time series of StreamFlow and Precipitation to the models ……30
Figure 2.7 Complete Data set Predictions ……………………………………………31
Figure 2.8 Climatology and anomaly components of flow data…………………..32
Figure 2.9 Streamflow Data Standardized Anomalies …………………………..32
Figure 2.10 Climatology and anomaly components of precipitation data ……….33
Figure 2.11 Precipitation Data Standardized Anomalies …………………………33
Figure 2.12 Climatology and Predicted Anomaly Components ………………..34
Figure 2.13 Final StreamFlow Climatology Added Prediction ………………….35
Figure 2.14 Location of Coruh Basin ………………………………………………..36
Figure 2.15 Coruh Basin …………………………………………………………….37
Figure 2.16 DEM Map of Coruh Basin …………………………………………….38
Figure 2.17 General Layout of Vegetation Cover of Coruh Basin……………….39
Figure 3.6 Station E23A004 DSI Streamflow Data v.s. TRMM Catchment Average Precipitation Data Complete Data set Predictions ........................................... 67

Figure 3.7 Station E23A004 DSI Streamflow Data v.s. TRMM Catchment Average Precipitation Data Anomaly Component Data set Predictions ........................................... 68

Figure 3.8 Station E23A005 DSI Streamflow Data v.s. Meteorology Precipitation Data Complete Data set Predictions ................................................................. 70

Figure 3.9 Station E23A005 DSI Streamflow Data v.s. Meteorology Precipitation Data Anomaly Component Data set Predictions ................................................................. 71

Figure 3.10 Station E23A005 DSI Streamflow Data v.s. TRMM Single Pixel Precipitation Data Complete Data set Predictions ......................................................... 73

Figure 3.11 Station E23A005 DSI Streamflow Data v.s. TRMM Single Pixel Precipitation Data Anomaly Component Data set Predictions ......................................................... 74

Figure 3.12 Station E23A005 DSI Streamflow Data v.s. TRMM Catchment Average Precipitation Data Complete Data set Predictions ......................................................... 76

Figure 3.13 Station E23A005 DSI Streamflow Data v.s. TRMM Catchment Average Precipitation Data Anomaly Component Data set Predictions ......................................................... 77

Figure 3.14 Station E23A016 DSI Streamflow Data v.s. Meteorology Precipitation Data Complete Data set Predictions ................................................................. 79

Figure 3.15 Station E23A016 DSI Streamflow Data v.s. Meteorology Precipitation Data Anomaly Component Data set Predictions ................................................................. 80

Figure 3.16 Station E23A016 DSI Streamflow Data v.s. TRMM Single Pixel Precipitation Data Complete Data set Predictions ......................................................... 82

Figure 3.17 Station E23A016 DSI Streamflow Data v.s. TRMM Single Pixel Precipitation Data Anomaly Component Data set Predictions ......................................................... 83

Figure 3.18 Station E23A016 DSI Streamflow Data v.s. TRMM Catchment Average Precipitation Data Complete Data set Predictions ................................................................. 85
Figure 3.19 Station E23A016 DSI Streamflow Data v.s. TRMM Catchment Average Precipitation Data Anomaly Component Data set Predictions........................................86

Figure 3.20 Station E23A020 DSI Streamflow Data v.s. Meteorology Precipitation Data Complete Data set Predictions.................................................................88

Figure 3.21 Station E23A020 DSI Streamflow Data v.s. Meteorology Precipitation Data Anomaly Component Data set Predictions..................................................89

Figure 3.22 Station E23A020 DSI Streamflow Data v.s. TRMM Single Pixel Precipitation Data Complete Data set Predictions............................................................91

Figure 3.23 Station E23A020 DSI Streamflow Data v.s. TRMM Single Pixel Precipitation Data Anomaly Component Data set Predictions..........................................92

Figure 3.24 Station E23A020 DSI Streamflow Data v.s. TRMM Catchment Average Precipitation Data Complete Data set Predictions.................................................94

Figure 3.25 Station E23A020 DSI Streamflow Data v.s. TRMM Catchment Average Precipitation Data Anomaly Component Data set Predictions.......................................95

Figure 3.26 Station E23A021 DSI Streamflow Data v.s. Meteorology Precipitation Data Complete Data set Predictions .................................................................97

Figure 3.27 Station E23A021 DSI Streamflow Data v.s. Meteorology Precipitation Data Anomaly Component Data set Predictions..................................................98

Figure 3.28 Station E23A021 DSI Streamflow Data v.s. TRMM Single Pixel Precipitation Data Complete Data set Predictions.......................................................100

Figure 3.29 Station E23A021 DSI Streamflow Data v.s. TRMM Single Pixel Precipitation Data Anomaly Component Data set Predictions.............................................101

Figure 3.30 Station E23A021 DSI Streamflow Data v.s. TRMM Catchment Average Precipitation Data Complete Data set Predictions...............................................103

Figure 3.31 Station E23A021 DSI Streamflow Data v.s. TRMM Catchment Average Precipitation Data Anomaly Component Data set Predictions.......................................104
Figure 3.32 Station E23A023 DSI Streamflow Data v.s. Meteorology Precipitation Data Complete Data set Predictions ................................................................. 106

Figure 3.33 Station E23A023 DSI Streamflow Data v.s. Meteorology Precipitation Data Anomaly Component Data set Predictions ......................................................... 107

Figure 3.34 Station E23A023 DSI Streamflow Data v.s. TRMM Single Pixel Precipitation Data Complete Data set Predictions ................................................................. 109

Figure 3.35 Station E23A023 DSI Streamflow Data v.s. TRMM Single Pixel Precipitation Data Anomaly Component Data set Predictions ......................................................... 110

Figure 3.36 Station E23A023 DSI Streamflow Data v.s. TRMM Catchment Average Precipitation Data Complete Data set Predictions ................................................................. 112

Figure 3.37 Station E23A023 DSI Streamflow Data v.s. TRMM Catchment Average Precipitation Data Anomaly Component Data set Predictions ......................................................... 113

Figure 3.38 Overall Average Model Correlations of Complete Data set Predictions .................................................................................................................. 117

Figure 3.39 Overall average model correlations of Anomaly Component Data set Predictions .................................................................................................................. 117
ABBREVIATIONS

ANN: .................................................................Artificial Neural Network
DSI: .................................................................General Directorate of State Hydraulic Works
FC: ..................................................................Frank Copula
JAXA: ...............................................................Japan Aerospace Exploration Agency
MGM: .................................................................Turkish State Meteorological Service
MLP: .................................................................Multi-Layer Perceptron ANN
MLR: .................................................................Multiple Linear Regression
NASA: .............................................................National Aeronautics and Space Administration
NC: ..................................................................Normal Copula
SLR: ..................................................................Simple Linear Regression
TRMM: .............................................................Tropical Rainfall Measurement Mission
CHAPTER 1

INTRODUCTION

1.1 Problem Definition and Motivation of the Study

Streamflow predictions in a specific catchment are desirable and have a major role in many industrial and scientific fields such as flood risk management for flood-sensitive areas, energy optimization and planning purposes for hydroelectric energy production, irrigation water management for agricultural fields, droughts, culture fishing, etc. Therefore, acquisition of reliable predictions of streamflow has a crucial importance, especially for human life and economy. Improved hydrological predictions are useful tools for management of water resources, disaster planning, and agriculture.

Hydropower is the most important renewable energy source in the world. Approximately 17% of world’s electricity demand is supplied by the hydropower (IEA, 2006). In Turkey, 32% of the electricity demand is supplied from the hydropower (EPDK, 2012). In this aspect efficient use of water resources is critical for the economy. Under many uncertain hydrologic and climatologic conditions, hydropower energy optimization and reservoir operation become very challenging. Having knowledge about the discharge of the river provides a vision for planning and maximization of the energy generation. Optimal hydropower energy generation in dams can be achieved with different approaches. Constructing a rule curve for optimal reservoir operation is one of them where rule curves describe how much storage must be maintained in a reservoir at different times in a year to ensure that discharge requirements can always be met (U.S. Army Corps of Engineers, 1985). Therefore,
having skillful streamflow data predictions are very important in long-term reservoir operations and management in the context of hydropower generation.

Floods are one of the most threatening disasters of all as it may cause loss of lives and property very quickly. Misuse of the land, destruction of the forest for a variety of reasons, wrong selection of the settlement and industrial area, infrastructure failure, rapid population growth, the corrupted balance between soil, water and plants are contributing factors to the damage of the floods, particularly in developing countries. Every year, over one million people are affected by floods and 40% of the damage of goods in the world is caused by the floods (World Disaster Report (2012), The International Federation of Red Cross and Red Crescent Societies). Therefore, skillful streamflow data predictions are very critical for accurate flood predictions and early warning systems.

However, the hydrological cycle is one of the most complex processes to understand. The composition of streamflow contains many different variables within itself e.g., precipitation, groundwater, soil moisture which may have to be estimated accurately over large regions. Most particularly precipitation rate is strongly non-Gaussian, discontinuous and at most weakly predictable at larger time scales (Yilmaz 2010) and runoff predictions are very difficult due to the existence of many uncertainties.

It has been around 40 years since remote sensing-based data sets have been used in hydrological data analysis studies. Today, many of the satellites can observe the earth surface for the purpose of retrieving information about rainfall, runoff, soil moisture content etc., while observation of the same variables using ground stations could be impractical. On the other hand, the added utility of remote sensing data in hydrological applications should be explicitly tested.

Stations are seemed to be the most accurate way of obtaining ground through data. However, it may not always be feasible to obtain good quality station-based data sets that represent large regions. On the other hand, remote sensing-based data sets are in many aspects very useful in estimation of ground conditions. It is known that predicted streamflow values obtained only rainfall data may not yield accurate predictions because streamflow composition has many other components like groundwater, soil
moisture, evaporation rate, snow melting etc. Models that are using only one component as an input cannot explain the complete variability. Despite, no precipitation falls during dry periods of the year, streamflow can be still observed, while the variability in streamflow may not be explained with only rainfall component. Potentially snow melting or groundwater feeds the streamflow on these periods. Addition of other data sets into the data driven approach may increase the model accuracy but the availability of additional data sets might be problematic to acquire over certain regions.

Actually, streamflow data itself in long-term comprises that unexplainable phenomenon in itself due to the strong seasonality. Climatology (long-term mean) component for a certain month or a season of streamflow can explain the phenomena because streamflow value in dry periods comprises snow melting or groundwater data. It is thought that, in a sort of way, the addition of climatology component of streamflow as an input to a rainfall-runoff prediction model will significantly increase the model accuracy.

1.2 Literature Review

1.2.1 Review on Earlier Studies on Runoff Prediction Methods

Streamflow prediction models based on precipitation data can be classified according to randomness, spatial variation, and time variability. These models can be grouped as deterministic, stochastic or statistic, neural network, conceptual or simplified physical models, and distributed physical models. Because the data sets might be problematic to acquire for constructing and calibrating conceptual and physical models (Kokkonen and Jakeman, 2001), data-driven hydrological methods have been begun to use in the field of hydrology (Besaw et al. 2009).

Conceptual models are simplified versions of hydrological processes (Chiew and McMahon, 1994). Physics-based rainfall-runoff models need huge amounts of data to train, validate and (VanderKwaak and Loague, 2001). Multiple linear regression
(MLR) and artificial neural networks (ANNs) are commonly used conceptual methods (Wang et al., 2008).

Various methods were developed in the past to simulate and predict the streamflow as the composition of historical rainfall and runoff recordings. Method accuracy is gaining importance, the core of method selection depends on the availability and quality of the historical data. In the following section, a literature review on the application of various regression analysis, copula methods, and ANN modeling for some hydrological researches are summarized.

**Regression**-based rainfall-runoff models (SLR, MLR) are simple data driven models which make a prediction from the historical data. Regression techniques provide a fast way of calculating the precipitation-based streamflow predictions.

Garen (1992) proposed several techniques to obtain accurate results from regression models which are using only known at forecast time, cross validation, principal components regression and systematic searching for optimal or near-optimal combinations of variables.

Post et al. (1999) constructed a daily lumped conceptual rainfall-runoff model which consisted of 16 small catchments. For many reasons like the variability of catchment topology, temperature etc., results were varying from catchment to catchment.

Rasouli et al. (2011) used a Global Circulation Forecasting model (NOAA), climate indices with local meteorologic - hydrologic observations to make a comparison study on streamflow prediction with three models; a neural network model (Bayesian NN), a support vector model, and a Gaussian model. They compared the performance of these models with a multiple linear regression model. As a result, they showed that non-linear models generally outperformed. On the other hand, they showed that the best streamflow predictions come from local observations.

**ANN** has been widely accepted as useful tools only during the 1990’s (Callan, 2006). In this chapter, some of the applications of ANNs as a Rainfall-Runoff process calculation is summarized.
Minns et al. (1996) used a 3-layer feed-forward type ANN with a series of numerical experiments to test the closeness of fit that can be achieved. Models with one and two hidden layered ANN showed that an extra hidden layer improves the performance of model (Minns et al., 1996).

In the case study of Lineares-Rodriguez et al. (2015) a model for one day-ahead daily streamflow with ANN approach is presented. Different from early works, they used a new runoff index to test ANN input. This index obtained by combining two different variables which belong to the weather research and forecasting mesoscale model. ANN model simulation skills and model accuracy improved with this new index. With a persistence index (PI) of 0.81 and an $R^2$ value of 0.95 they proved that their model performance was satisfactory.

Birikundavyi et al. (2002) investigated the performance of neural networks as potential models capable of forecasting daily streamflow. By the mean square error and Nash coefficients-based comparison they showed that artificial neural networks results are superior to the ones obtained with a classic autoregressive model coupled with a Kalman filter.

Budu (2014) used artificial neural networks and multiple linear regression models with wavelets and moving average methods to predict daily reservoir inflows. In the study, real time observations are decomposed into subseries using different wavelet NN functions with discrete wavelet transform and then the proper subseries are taken as inputs to NN for forecasting reservoir inflow. Calibration is made by 7 years of data, and remaining data are used for the validation. The comparison made by the Nash–Sutcliffe efficiency coefficient, RMSE, and correlation coefficient with two NN models, one MLR model, and one moving average model. Results showed that wavelet model performance was the best and multiple linear regression approaches had efficient inflow hydrograph.

Garbrecht (2006) made Monthly Rainfall-Runoff Simulation and compared three alternative ANN design to investigate the effect of seasonal rainfall-runoff variations. The main difference of designs is the way in which the effects of seasonal climate and runoff variations were incorporated into the network. The important conclusion to the
investigation is that a separate network for each month reflects the seasonal rainfall runoff variations, ends up with better results (Garbrecht, 2006).

*A copula* is a multivariate distribution function. Recently, Copula functions have been a useful tool for various problems in hydrology and water resources studies and applications. Especially in the field of drought analysis copulas gives accurate results. Besides, copula functions have a significant role in the fields that flood frequency analysis, rainfall intensity-duration frequency analysis.

Lee et al. (2008) studied Copula usage in stochastic streamflow simulation. Different copula functions used in order to utilize non-parametric and parametric functions for fitting the distribution of the real time observed data and serial dependence structure. The advantages and disadvantages of different copula time series models were investigated by comparing the statistics of the generated data. The results showed that the benefits of using the copula functions are only marginally different from other method results.

Samaniego et al. (2010) find a procedure to measure dissimilarity that is estimated from coupled empirical copula functions of streamflow to calculate a metric. By using a multiscale parameter regionalization technique hydrologic model parameters were regionalized. Transfer function parameters were found via calibration of the model. The streamflow in an ungauged basin was found as an ensemble streamflow prediction. Reasonable results are obtained with the proposed technique in ungauged basins.

Sugimoto et al. (2016) used copulas as a tool to investigate the effect of climate change with existing long-term discharge records. They used copula asymmetry and copula distances to identify the nonsymmetrical property of discharge data and variability and interdependency. As a result of the study, they specified the climatic regime change periods of Neckar catchment.

Bezak et al. (2016) studied flash floods and rainfall. Copula-based IDF curves and empirical rainfall thresholds are used in the study. By using high-resolution rainfall data, they constructed an IDF curve on the Frank copula function for several rainfall
stations. After the analyses that showed rainfall characteristics triggering flash floods and landslides are different.

**Persistence** of streamflow indicates that sequences of river flow in the historical record that are similar to the recent past provide valuable information in the near future (Svensson, 2014). In the literature, there are several studies which are using persistence approach as a benchmark. Dralle et al. (2015), Glenn et al. (2004), Owens et al. (2003) made comprehensive discussion in their studies. Persistence approach is generally used for calculating the climatological indicators. Some meteorological studies of Namias J. (1952) and Van Den Dool (1982) are good examples on this topic.

Svensson (2014) studied on seasonal river flow forecast by using hydrological persistence and historical flow analogs. Results show that the forecasts based on the persistence of the previous month’s flow generally outperform the analogs approach in her study.

**Climatology** of the streamflow indicates the mean of specific time periods, gives insights about the seasonal variations. In this study, monthly mean of historical streamflow data is used. Mean is the most commonly used statistical starting point of comparison.

One of the probable future work of this study considered as the effect of regulations on the streamflow predictions. Data used in this study is chosen in unregulated time periods. In this aspect study of Sayama et al. (2006) must be mentioned. In their study, investigation of alteration of the hydrological cycle caused by environmental change according to the actual conditions would not be qualified for make predictions in an ungauged basin. The motivation of the study was to investigate the effects of dam reservoirs to the flow regime changes. They end up such a conclusion that human factors make an alteration in hydrological cycle in a catchment and flood potential. This makes the real time observations not directly applicable for future predictions.
1.2.2 Studies Focusing on Rainfall-Runoff Predictions over Turkey

A study from Turkey was made by Bakis and Goncu (2015). They used regression analysis as a tool for filling the missing data of Zab River obtained from the flow gauging stations related to the correlations and drainage area-ratio method. As a result, they concluded, when compared with the observed data; both filling methods resulted in large deviations.

Kisi (2003) used an ANN model and an Auto-Regressive Model to forecast daily river flow, investigated the appropriate ANN architecture for hydrologic modeling for Filyos Stream with a 2-year period of streamflow data. Three different ANN models are used and the results are compared with an AR model. In the study, the comparison showed that ANNs provide the better results for daily streamflow forecasting.

Kentel (2009) used past precipitation and associated river flow data in an ANN algorithm for Guvenc Basin and made predictions of future river flows. Also in her study, she investigated impacts of various input patterns, a number of training cycles, and initial values assigned to the weights of the connections identified direct mapping from inputs to outputs without consideration of the complex relationships among the dependent and independent variables of the hydrological process. Also, Kentel (2009) used a fuzzy c-means algorithm to cluster the training and validation input vectors with regular and extreme events. Main reason behind this usage is that the user will have an idea about the risk of the ANN model to generate unreliable results.

Another ANN study on rainfall-runoff modeling is performed by Gumus et al. (2010). In this study, authors have assessed the ability of MLR, ANN model to predict the runoff over Euphrates River Basin using gauged based precipitation data. They obtained promising results with ANN model and concluded that ANN models can be easily used in rainfall-runoff modeling.

Kara and Yildiz (2014) performed a bivariate analysis of the relation between precipitation and runoff over Hirfanli Dam Basin. Two elliptical and three Archimedean copula functions have been tested to model the dependence structure between the hydrological variables. They used different graphical tools and numerical techniques for the appropriate model selection, parameter estimation and goodness of
fit. Their results indicated that Clayton and Student-t class copula functions are more appropriate to model the dependence structure between the precipitation and the runoff over their study area.

1.3 Main Purpose of the Study

The main purpose of this study is to investigate the predictability of runoff using precipitation data over Coruh Basin using Simple and Multiple Linear Regression, ANN, and Copula methods and their predictive skills are compared against the commonly used benchmarks, climatology- and persistence-based predictions. More specifically in this study;

- Intercomparison of the predictive skill of simple linear regression, multiple linear regression, ANN, and copula methods is done.
- The predictive skills of methods are compared against climatology and persistence benchmarks to better understand the added skill via these methods, quantifying the predictive skill of climatology components compared to the anomaly components and filling the gap between the inter-comparison of Copula, climatology- and persistence-based predictions of streamflow over Turkey.
- The predictions using above methods are made both the remote–sensing and station-based precipitation data to quantify the added utility of remote sensing-based precipitation in runoff predictions compared with the predictions using gauge-based precipitation data. Moreover, by this investigation, added utility of areal average precipitation data sets to single point station data in streamflow predictions are performed and compared.
CHAPTER 2

METHODOLOGY

2.1. Prediction Models

In this study, runoff predictions utilizing precipitation data are made. A Simple Linear Regression Model (SLR) and a Multiple Linear Regression Model (MLR) is constructed to simplify the relationship between the rainfall-runoff process and to get benefit from the ability to gain simple results of the regression models. An Artificial Neural Network Model (MLP) is constructed to get benefit from its ability to deal with the complexity and learning algorithm. Two Copula Models (Normal Copula and Frank Copula) are constructed to get benefit from its ability to separate marginal distribution from the dependent nature of the variables. All of the results that gained from these models will be compared with hydrologic Climatology and Persistence characteristics of the monthly state of streamflow. The following section provides brief information about the history of data driven prediction models which are used in this study

Regression analysis is the most common analysis method in hydrology. Analysis based on a relation made between a dependent variable and one independent variable. Analysis process shows the impact of changes in an independent variable on the dependent variable that we wish to predict. It is also a tool for explaining the relations of a variable is affected directly by another or both variables affected by common factors that are unknown (Web-1). Regression analysis can be used for the filling of the missing data in a series on a polynomial relationship between the observations or validation of the series (Fung, 2006).
The term “Regression” firstly used at the eighteen century by Francis Galton, who has many studies on genetics. While he was studying on sweet pea plant and trying to explain the phenomenon about the relationship between heights of the descendants of the plant, the study laid the foundations of modern linear regression analysis. After Galton, his lab researcher Karl Pearson developed the correlation concept. An Early form of his work was the least squared error approach and he stated that the main problem in regression analysis is to establish most suitable description between the variables (Stanton, 2001).

The method of least squares is a procedure to determine the best fit line to data. The method gets its name from the way the unknown statistics are computed. The method estimates parameters by minimizing the sum of the squared deviations between the variables. Results are obtained using basic calculus and specifically the property of a quadratic expression’s minimum value. The point must be considered in the least squared estimates is its high sensitivity to the outliers. This is a consequence of squaring the variations between the variables (Encyclopedia of Research Design, vol.1, Method of Least Squares, 2010).

Artificial Neural Networks (ANN) are widely used prediction models in hydrological studies. Methodology originally comes from the struggle that understanding the information processing of the human nervous system. Despite there are still too many unknowns about the information processing of the human brain, neural network approach to problem-solving tries to mirror that process of the neurons. A neuron collects the information from other neurons with a structure called dendrites. Then a neuron sends this information signal as an output through the structure called axon, every neuron connects to many other neurons through synapses. Synapses convert the signal from the axon into electrical signal form and these electrical signals send to the brain for the purpose of processing by connections of thousands of neurons. Every neuron can be thought as a single processing section. By changing the effect of a neuron over the other, learning occurs. (Stufflebeam, 2008) Figure 2.1 shows the structure of the single neuron information process in the human brain.
Early understandings about neural networks belong to neurophysiologist Warren McCulloch (1943). After computers become advanced in the 1950s, it was possible to build some models which could imitate human neural network interactions and at 1980s ANN models started to use much scientific research. ANNs are the calculation tool of information through interactions among neurons (or nodes). Model runs inputs and outputs as variables of the nonlinear function. Mirroring the natural behavior of human neural network system ANN has the advantages of learning ability. Ability to response as a result of input data. Synapses in the biology known as the weights in the ANN.Weights are constants that use to calculate the output of the process. It is a practical tool to carry out complex hydrologic calculations (Reingold & Nightingale, 1999, History of Neural Networks).

ANN Models have a withstanding success in the use of rainfall-runoff modeling. A multilayer perceptron is the most commonly used ANN method which gives satisfactory results in modeling hydrologic process to predict the short run streamflow discharge.
Copula theory first appeared in Frechet’s study (1951). On his study about the given distribution function of two random variables defined on the same probability space, the bivariate distribution function of marginal of this two random variables. In Sklar’s 1959 study resulted in very important conclusions by constructing a new class of functions which he called as “Copula” for Frechet’s work (Durante and Sempi, 2009). The copula is a Latin word for “link”.

Sklar and Schweizer published the book “Probabilistic Metric Spaces” in 1983. This book considered the main source of basic information on copulas. At the end of the 90’s Copula Theory become popular (Durante and Sempi, 2009). Since the beginning of the 2000’s Copulas have become a tool for hydrological studies especially in the field of drought analysis. Over a decade many important results still are to be discovered and derived (Salvadori, 2007).

The predictive skills of these methods have to be compared against a benchmark so that their true skill can be understood. In this study, Climatology and Persistence of monthly state of streamflow are used as benchmarks. To further investigate the source of the predictive skills of these methods, separate predictions are made using the standardized anomaly components of data sets (after -climatology/long year monthly mean- components are removed and standardized by dividing the standard deviation of the data) and complete data sets (normal/non-standardized data sets retaining both anomaly and climatology components). 80% of the data is used for training and 20% of the data is used for validation. Long data sets (42 years of observations) are divided into 34 years of training and 8 years of validation and short data sets (12 years of observations) are divided into 9 years of training and 3 years of validation.
2.1.1. Linear Regression Model

Many problems in engineering and science involve exploring the relationships between two or more variables. While established relations are mostly used to predict the dependent variable using the independent one. Least squared based Linear Regression method (1806 Legendre, 1810 Gauss) is perhaps the oldest yet one of the most used prediction methods.

Regression analysis is a method to find a linear relationship between two variables. Figure 2.2 (also known as scatter plot) shows the linear relationship between the variables “streamflow” on the horizontal axis and “precipitation” on the vertical axis. The simplest relationship consists of a straight line.

![Figure 2.2 Sample regression line and observed data scatter plot](image)
Regression calculations find the optimum values of the regression parameters (slope and intercept) that minimize the sum of the squared errors. A form of the regression formula is as follows (Levine et al. 2013).

\[ Y_i = \beta_0 + \beta_1 X_i + \varepsilon_i \]  

(2.1)

Where; \( \beta_0 \) is intercepted for the population, \( \beta_1 \) is the slope for the population, \( \varepsilon_i \) is the random error in predictions \( i \), \( Y_i \) is the dependent variable (sometimes referred to as the response variable) for observation \( i \) and \( X_i \) is the independent variable (sometimes referred to as the explanatory variable) for observation \( i \).

The solution for the calculation of the slope \( \beta_1 \),

\[ \beta_1 = \frac{SSXY}{SSX} \]  

(2.2)

where;

\[ SSXY = \sum_{i=1}^{n}(X_i - \bar{X})(Y_i - \bar{Y}) \]  

(2.3)

\[ SSX = \sum_{i=1}^{n}(X_i - \hat{X})^2 \]  

(2.4)
Computation of the intercept $\beta_0$,

$$\beta_0 = \bar{Y} - \beta_1 \bar{X} \quad (2.5)$$

where,

$$\bar{Y} = \frac{\sum_{i=1}^{n} Y_i}{n} \quad (2.6)$$

$$\bar{X} = \frac{\sum_{i=1}^{n} X_i}{n} \quad (2.7)$$

2.1.2. Multiple Linear Regression Model

As in the SLR model, again the purpose in MLR is to obtain least square estimates which minimize the total sum squared error term. When more than one predictor variable included in the calculations, effects of all variables can be observed from the predictions. Once the relations between the multiple variables and the dependent variable we can make more accurate predictions and use all the information. Due to lack of data, in this study, squared values of precipitation is used as a second predictor.

General MLR model (Shedden, 2016);

$$Y_i = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \cdots + \beta_k X_k + \varepsilon_i \quad (2.8)$$

where $\beta_0$ is the “intercept,” $\beta_1$ ...... $\beta_k$ are “slopes” or “coefficients”. These coefficients are fixed or constant but unknown values. $\varepsilon$ is a random variable that is independent of Xs with “0” mean and variance of $\sigma^2$. Errors are not correlated with each other and not correlated with other predictors. Estimates can be calculated by using linear algebra;
By taking all observation into an n-dimensional vector, called “response vector” (Shedden, 2016);

\[
Y = \begin{pmatrix}
Y_1 \\
Y_2 \\
\vdots \\
Y_n
\end{pmatrix}
\]  \hspace{1cm} (2.9)

Then by putting all predictors into an n.p+1 matrix, design matrix is obtained;

\[
X = \begin{bmatrix}
1 & X_{11} & X_{1p} \\
1 & X_{21} & X_{2p} \\
\vdots & \vdots & \vdots \\
1 & X_n & X_{np}
\end{bmatrix}
\]  \hspace{1cm} (2.10)

It is important that first column of the design matrix be formed of 1s. After that packing the coefficients and intercepts into a p+1 dimensional matrix, we obtain a vector called slope vector.

\[
\beta = \begin{pmatrix}
\alpha \\
\beta_1 \\
\beta_2 \\
\vdots \\
\beta_p
\end{pmatrix}
\]  \hspace{1cm} (2.11)
At last, we put the error terms into an n-dimensional another vector called error vector.

$$\varepsilon = \begin{pmatrix} \varepsilon \\ \varepsilon_1 \\ \varepsilon_2 \\ \vdots \\ \varepsilon_n \end{pmatrix} \quad (2.12)$$

Model is become $Y_i = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \cdots + \beta_k X_k + \varepsilon_i$, can be written in algebraic form of;

$$Y_i = X\beta + \varepsilon_i \quad (2.13)$$

Note that $X\beta$ is the matrix vector product. For estimating the $\beta$ like in linear regression least squares approach will be used. By minimizing the error formulation;

$$\sum_i (Y_i - \alpha - \beta_1 X_{i,1} - \cdots - \beta_p X_{i,p}) \quad (2.14)$$

Obtained formulation is,

$$\hat{\beta} = (X'X)^{-1}X'Y \quad (2.15)$$

Where $X'X$ and $(X'X)^{-1}$ are p+1 x p+1 symmetric vectors. $X'Y$ is a p+1 dimensional vector. Then,

$$\hat{Y} = X\hat{\beta} = \{X(X'X)^{-1}X'Y \quad (2.16)$$
\hat{\gamma} is the best prediction obtained from the multiple linear regression calculations.

2.1.3. ANN Model

ANN Models mimic the neurons in the human brain. Connections generally called nodes or units. Information processing occurs in form of signals through these connections. Each unit has its own weight which shows the strength of the participation of the node into the calculation. Also, the weight of a node determines the effect of the variable on the process. In the process, a linear or nonlinear transformation function is applied to the nodes to determine its output signal. In this study, Multi-Layer Perceptron (MLP) is used. Figure 2.3 shows General Layout of an ANN Model (ASCE, 2000).

Figure 2.3 General layout of an ann model (ASCE, 2000)

Figure 2.4 shows the schematic diagram of a single node, \(b_i\) is the threshold value or generally called bias. \(W_{ij}\)s are weights and \(X_i\)s are inputs for the node. \(f\) is the threshold
function and lastly \( y_j \) is the net output signal of the node. The below function defines the operation.

\[
y_j = f(X.W_j - b_j)
\]  

\( f_t = \frac{1}{1+e^{-t}} \)  

MLP uses the back propagation algorithm for training, which is the most popular neural network type. In the algorithm, weights are iteratively changing to minimize the errors of the weights. The main strength of a network come to this capability of training. First, the input of the data set passes through the network then calculated output is compared with the measured or observed output. On this stage error calculation made and then this error term propagates backward through the network to each node. Weights are recalculated according to adjustment of the error term of each node.
Step by step calculations of a Feed Forward MLP algorithm as follows (ASCE, 2000), Input unit enters the process from the input layer and receives the signal, \( x_i \) (i = 1, 2, …..n) and sends this signal to the next layer. Every hidden unit (\( H_j, j =1, 2, ….. p \)) receives their weighted input values.

\[
H_{in_j} = v_{oj} + \sum x_i v_{ij}
\]  
(2.19)

Where \( v_{ij} \) is the connection weight and \( v_{oj} \) is the bias value, perform a sigmoid function to calculate their output value;

\[
H_j = f(H_{in_j})
\]  
(2.20)

Then these values transfer to the following layer. Each output nodes (\( Y_k, \) where \( k = 1, 2, …..m \)) sums its weighted input signals,

\[
Y_{in_j} = w_{ok} + \sum h_i w_{jk}
\]  
(2.21)

and then again performs its threshold function to compute output signals.

\[
Y_k = f(Y_{in_k})
\]  
(2.22)
At this stage Back-Propagation error calculated. Every output nodes that receive the desired value regarding the input value takes its error term.

\[ \delta = (t_k - y_k)f'(Y in_k) \] (2.23)

Weight correction and bias correction factors calculated,

Weight correction factor,

\[ \lambda w_{jk} = \partial \delta_k H_j \] (2.24)

Bias correction factor,

\[ \lambda w_{0k} = \alpha \delta_k \] (2.25)

Calculated \( \delta_k \) error information term sends to nodes in the previous layer. Each hidden unit gets its delta inputs from next layer,

\[ \delta in_j = \sum \delta_k w_{jk} \] (2.26)

and multiplies by the derivative of threshold function for calculation of error term. After that again weight correction term to update \( \nu_{ij} \) and bias correction term to update \( \nu_{oi} \) are calculated.

\[ \delta_j = \delta in_j f'(Hin_j) \] (2.27)
Each output node restores by adding these corrections (ASCE, 2000).

New weights,

\[ w_{jk}(\text{new}) = w_{jk}(\text{old}) + \lambda w_{jk} \tag{2.30} \]

New Bias,

\[ v_{ij}(\text{new}) = v_{ij}(\text{old}) + \lambda v_{ij} \tag{2.31} \]

After new weights and biases are calculated error term between the desired output and recalculated one compare to each other, if error term is not in the acceptable range, correction of weights and biases are iterated respectively.

2.1.4. Copula Models

Copulas have wide usage areas, such as risk management, biology and recently used in hydrology and water resources management related fields. Especially in the field of drought analysis and flood risk analysis, there are many promising studies made by using copulas.

Copulas are simply the joint distribution of random variables, and also an extremely beneficial technique that allows forming a multivariate distribution function from univariate distribution functions (Bloomfield, 2013). Copula theory uses the marginal distributions to create a joint distribution. This is the main power of the Copula Theory.
The core of the Copula Theory comes from the Sklar’s theorem (Bloomfield, 2013). Given two random variables $X$ and $Y$, estimation of their univariate CDFs are trivial and the sample data sets are often sufficient, while the analytical solution for the joint CDFs is not immediately clear. At this point, copula functions link univariate CDFs and create their multivariate (e.g., bivariate or trivariate) CDFs (Afsar, 2016). For variables $X, Y; F_{XY}(X, Y)$ represents the joint cumulative distribution, $F_X(X)$ and $F_Y(Y)$ are the marginal distribution of $X$ and $Y$, there exist a unique copula $C(F_X(X), F_Y(Y))$ (De Michelle, 2003).

$$F_{XY}(X, Y) = C(F_X(X), F_Y(Y)) \quad (2.32)$$

If there are $N$ different random variables than general form of the formula can be shown (De Michelle, 2003),

$$F_{X_1X_2......X_N}(X_1, X_2 \ldots \ldots X_N) = C(F_{X_1}(X_1), F_{X_2}(X_2) \ldots \ldots F_{X_N}(X_N)) \quad (2.33)$$

**Copula Density**:

Assume $F(X_1, X_2 \ldots \ldots X_N) = C[F_{X_1}(X_1), F_{X_2}(X_2) \ldots \ldots F_{X_N}(X_N)]$ and $F$ and $C$ are differentiable, joint probability density function of events (De Michelle, 2003),

$$\frac{F(x_1,x_2,\ldots, x_N)}{F_1(x_1)F_2(x_2)\ldots \ldots F_N(x_N)} = C[F_{X_1}(X_1), F_{X_2}(X_2) \ldots \ldots F_{X_N}(X_N)] \quad (2.34)$$

There are many classes of copulas available like Archimedean, Elliptic, Extreme Value etc. In this study, Normal Copula Function from the Elliptical copula family and Frank Copula Function from the Archimedean Copula Family are used.
**Normal Copula (NC) Function:**

\[
C^N(x, y) = \frac{F(x, y)}{F_x(x)F_y(y)} = \int_{-\infty}^{\Phi^{-1}(x)} \int_{-\infty}^{\Phi^{-1}(y)} \frac{1}{2\pi(1-\rho^2)^{1/2}} e^{-\frac{x^2-2\rho xy+y^2}{2(1-\rho^2)}} \, dx \, dy \tag{2.35}
\]

Where; \( \rho \) is the copula dependence parameter, \( x \) and \( y \) are two dependent univariate variables, \( \Phi \) is the CDF of standard univariate gaussian distribution, respectively.

**Frank Copula (FC) Function:**

\[
C^F(x, y) = \frac{F(x, y)}{F_x(x)F_y(y)} = \frac{-1}{\alpha} \ln\left(1 + \frac{(e^{-\alpha x} - 1)(e^{-\alpha y} - 1)}{e^{-\alpha} - 1}\right) \tag{2.36}
\]

Where; \( \alpha \) is the copula dependence parameter, \( x \) and \( y \) are two dependent univariate variables, respectively.

**2.2. Climatology and Persistence Benchmarks**

In the absence of reliable predictors, a good estimate that can be made is the mean of the random variable. For example, for a Gaussian white noise process with “0” mean and “0” autocorrelation, given the availability of the entire time series of this variable, the best guess for the future predictions is the mean value (here “0”). Another example; given only monthly streamflow observations are available over a region between January 1901 and December 2000. A climatological prediction for January 2001 could be obtained as the average of 100 values of all January observations between 1901 and 2000.

In this way, a separate prediction can be made for each month, while these monthly predictions would be constant for any given year. Such a prediction would be valuable particularly over regions with strong seasonality as a result of snow melting,
groundwater feed or seasonally changing rainfall variability. There except for streamflow data, no other data available is present.

2.2.1. Climatology

Climatology type forecast is a simple way of making hydrologic predictions. It is making forecasts by using simple statistics. The idea behind the climatology method is forecast the same value for every event that occurs in the same time periods (prediction for month “A” is the average of all observations of “A”s), the mean. (Web-2 can be checked on this topic).

Precipitation is random in time for a region, so as a result of randomness in hydrologic cycle streamflow has a tendency of vary over time. If there is no other prediction about streamflow, climatology concept gives the knowledge of basic variation of the streamflow over time. In lack of information, knowing the monthly streamflow variability provides efficient information. Figure 2.5 shows an example for monthly climatology time series.

![Figure 2.5 Example of a monthly climatology time series (E23A004)](image)

General formula of Mean,

\[ \mu = \frac{\sum_{i=1}^{n} x_i}{n} \]  \hspace{1cm} (2.37)

Where, \( x_i \) are the random values of same time periods, \( n \) is the number of observations.
2.2.2. Persistence

Among all of the forecasting methods, Persistence method is the easiest and most applicable one because the method predicts the tomorrow’s hydrological event as same as today’s event.

A disadvantage of persistence approach is it may not catch relationship between events as a rainfall-runoff model if the distribution of events has so much of variations in time. Persistence concept is very useful for short term predictions, but main power of persistence is to make long range forecasts when it used with the climatology of the event. In this study, observed standardized anomalies of the previous month is used to predict following month’s streamflow predictions (following month’s observed standardized anomaly taken as the following month’s observed standardized anomaly) (Web-3 can be checked on this topic). The following section provides brief information about calculation of persistence,

First step, calculation of the Mean $\mu$,

$$\mu_{i,t} = \frac{\sum_{i=1}^{n} x_{i,t}}{n} \quad t = 1, 2, 3, \ldots, 12 \quad (2.38)$$

Second step, calculation of the Standard Deviation,

$$\sigma_{i,t} = \sqrt{n} \frac{\sum_{i=1}^{n} (x_{i,t} - \mu_{i,t})^2}{n} \quad (2.39)$$

Third step, finding standardized anomalies of streamflow (Svensson, 2014),

$$a_{i,t} = \frac{x_{i,t} - \mu_{i,t}}{\sigma_{i,t}} \quad (2.40)$$
Fourth step, calculation of persistence-based prediction,

\[ p_{i,t+1} = a_{i,t} \times \sigma_{t+1} + \mu_{t+1} \]  

(2.41)

Where, \( p_{i,t+1} \) is the following month’s persistence-based prediction, \( a_{i,t} \) is the standardized anomaly of the previous month, \( \mu \) is the mean of the monthly observations, \( \sigma_{t+1} \) is the standard deviation of following month, \( n \) is the number of observations.

For example;

\[ p_{i,february} = a_{i,january} \times \sigma_{february} + \mu_{february} \]  

(2.42)

In general, autocorrelation coefficient greater than 0.50 for a streamflow time series, it is expected that the persistence approach would provide better results than the climatology approach.

2.3. Complete and Standardized Anomaly Data Set Predictions

To further investigate the source of the predictive skills of these methods, separate predictions are made using the standardized anomaly components of data sets (after - climatology/long year monthly mean- components are removed and standardized by dividing the standard deviation of the data) and complete data sets (normal/non-standardized data sets retaining both anomaly and climatology components). 80% of the data is used for training and 20% of the data is used for validation. Long data sets (42 years of observations) are divided into 34 years of training and 8 years of validation and short data sets (12 years of observations) are divided into 9 years of training and 3 years of validation. Following section provides detailed information about complete
data set prediction methodology and standardized anomaly component data set predictions.

2.3.1. Complete Data Set Predictions

In this prediction methodology traditional way in Rainfall-Runoff models are followed. First input data sets (DSI Flow Station data sets v.s. MGM and TRMM Precipitation data sets) are introduced to models (SLR, MLR, ANN, Copulas). Figure 2.6 shows the input time series of streamflow and precipitation data sets to the models. In the presentation, only 12 years (2000-2011) of data is shown as a time series but in the calculations, 42 years (1970-2011) of data is used. Figure 2.6 shows an example input time series in traditional rainfall-runoff models.

Figure 2.6 Example input time series of streamflow and precipitation to the models

80% of the data (34 years – 408 months) is used for training and 20% of the data (8 years – 96 months) of the data is used for validation.

Finally, predictions compared with climatology and hydrologic persistence of streamflow. Figure 2.7 shows an example of the complete data set predictions (results which are obtained from the data of this study as an example). In this figure, 3 years
of real observations, Climatology and Persistence validation time series and SLR and MLR validation time series are shown in the figure.

Figure 2.7 Example Complete Data set Predictions

2.3.2. Standardized Anomaly Data Set Predictions

In this methodology, predictions made with standardized anomaly components of data sets after –climatology (long year monthly mean), components are removed and standardized by dividing the standard deviation of the data. By this way, predictions are made with the deviations of the data. First monthly mean of 42 years of data (b) (12 years for short data sets) is calculated. Then, this monthly means of long years (climatology component) subtracted from the complete data set (a) (observations). Hereby, anomaly component of data has been calculated (c). Figure 2.8 shows an example of complete data and its climatology and anomaly components (i.e., complete dataset = climatology + anomaly).
Figure 2.8 Climatology (b) and anomaly (c) components of complete (a) streamflow time series

Then anomaly component of the data is divided by the standard deviations of the data and standardized anomalies of flow data have been obtained. Figure 2.9 shows the standardized anomaly component of flow data.
Same calculations made for the precipitation data as well. Figure 2.10 and Figure 2.11 shows calculations of climatology and anomaly components of precipitation data and precipitation anomalies of data ($c = a - b$).

Figure 2.10 Climatology (b) and anomaly (c) components of complete (a) precipitation time series

Figure 2.11 Precipitation data standardized anomalies
Once standardized anomalies of precipitation and flow data are obtained, in this methodology, these standardized anomalies introduced the models (SLR, MLR, ANN, Copulas) instead of the complete data sets. After predicted standardized anomalies of flow data obtained from models, next step is de-standardization. Predicted anomalies of flow data are de-standardized with multiplying with the standard deviation of the flow data. Figure 2.12 shows the acquiring steps of final predictions (only SLR output is used in the presentation).

![Image](image1.png)

**Figure 2.12** Anomaly (a) and climatology (b) components of predicted streamflow

Lastly, by adding the climatology component of flow data to predicted de-standardized anomalies of flow data (a+b), calculations are terminated. Figure 2.13 shows the SLR model final prediction with observations, climatology component, and persistence-based prediction together (results which are obtained from the data of this study as an example). Results show that predictions of SLR model which are using standardized data are improved when long-term climatology values added.
2.4. Study Area

2.4.1. General Layout of Basin

Coruh River Basin located in northeastern region of Turkey. The basin has 19.872 km² drainage area in Turkey and 2.090 km² drainage area in Georgia (Web-4). Figure 2.14 shows the location of the Coruh Basin in Turkey. As a result of the steep elevation change in the basin, the Coruh River is the fastest flowing river in Turkey and the third fastest in the world.

The total length of the Coruh River (412 km) and the steep topography change provides the basin one of the highest electricity generation potential in Turkey (27% of the total energy potential; Coruh River Basin Projects Report, 2009). In this study, Coruh Basin is selected as the study area because of its high hydropower generation potential (i.e., therefore prediction of streamflow is of interest for many users) while unregulated streamflow observations and long historical datasets are still available over the basin despite this potential.
Coruh River is born from Civilikaya Hill, part of the Mescit Mountains and is located in the north of the Erzurum Plateau. Coruh River later flows through the Eastern Anatolian and Eastern Black Sea region that flows into the Black Sea near the city of Batumi, Georgia (Web-4). The total length of Coruh River is 431km, while 410km flows through Turkey 21km flows in Georgia. Tortum and Oltu streams are the main streams of the Coruh River from Turkey and Adzharis from Georgia. Coruh River has a mean annual runoff of 6.824hm$^3$. Observed mean discharge of the river is 200m$^3$/s, maximum discharge is 2.431m$^3$/s and minimum discharge is 38 m$^3$/s (Web-4). Coruh basin has the highest erosion potential among all of the basins of Turkey. This high erosion potential is driven by the speed of the river, which is one of the fastest flowing rivers in the world. This study covers the upper and middle stream of the Coruh River and one tributary river called Berhal Creek. Figure 2.15 shows the general layout of the Coruh Basin.
2.4.2. Basin Geography and Slope Properties

Coruh Basin is located in the orogenic belt. Toward north-northeast lies the black sea mountains and in the line of northeast-southwest lies the Mescit and Yalnizcam Mountains. From east to the west direction this mountain has a formation which reaches 4000m height due to east direction. Morphology of the mountains is generally formed of metamorphic rocks, mica schists, quartzite, granite, and schist. Coruh Basin mountains subside from the north of the Kackar Mountains. Highest mountains of the region as follows, Karadag (2300m), Arafek (2300m), Karayol (2750m), Ziyaret (2000m), Geberet (2413m), Horasan (2830m), Kurdevan (3050m), Ayvan (2000m), Arsiyan (3160m), Morete (2500m), and Karcal (3428m). This mountainside has deep valley formation where the Coruh River lies through this deep valley formation. (Figure 2.16)
Figure 2.16 DEM Map of Coruh Basin
2.4.3. Vegetation Cover and Climatology

The Northern region of the basin has the characteristic of the black sea climate. Locations, that near East-Black Sea Region like Hopa and Kemalpasa have high annual precipitation. Average annual precipitation of this region is measured as 2754mm. Maximum streamflow values occur in May while maximum precipitation occur in April and October for any given year in Coruh Basin. Toward inland, the climate is in transition to continental climate characteristics. Some annual average meteorological station measurements are as follows; Borcka (1250mm), Artvin (689mm), Ardanuc (446mm), Yusufeli (295mm), Ispir (440mm), and Oltu (353mm) (Web-4). Figure 2.17 shows the general layout of the vegetation cover and heights of the basin.

Figure 2.17 General layout of vegetation cover of Coruh Basin
Coruh Basin located in Colchic Region of Euro-Siberian Region Flora Zone. Mediterranean originated endemic taxons are also seen between the 200-400 m elevations (Web-4). Forest formation of basin spreads as, perhumid mild broad-leaved trees (Chestnut Forests, Beech Forest, and Mountain Alder Forests), moist and cold sandarac trees, dry forest and some bush formations.

2.4.4. Regulated Regions of the Basin

Coruh River, with the remarkable energy potential, has been attracted attention and many projects have been developed since 1962 by the Electrical Works Study Administrations (EIÉ). The energy potential of the river was calculated as %27 of the total energy potential of Turkey. Total head of the river that can be used to product energy is 1420m. There are 10 dams on the main stream (6 of them locates upper and middle sections of the stream) and 17 different dams and runoff-river type hydroelectric power plant projects on the tributary streams. These dams and power plants will regulate the river flow in the basin when the ongoing projects will be completed (Coruh River Basin Projects Report, 2009).

Table 2.1 gives brief information about the upper and middle stream dams. The following section provides information about the regulated regions and dams on the river.

Table 2.1 Coruh Basin upper and middle stream dams

<table>
<thead>
<tr>
<th>Dams</th>
<th>Annual Mean Flow (m³/s)</th>
<th>Drenaige Area (km²)</th>
<th>Total Head (m)</th>
<th>Maximum Operation Level (m)</th>
<th>Installed Capacity (MW)</th>
<th>Annual Energy Production (GWh)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Laleli</td>
<td>879,16</td>
<td>4759,00</td>
<td>138,00</td>
<td>1480,00</td>
<td>102,00</td>
<td>244,55</td>
</tr>
<tr>
<td>Ispir</td>
<td>950,00</td>
<td>5100,00</td>
<td>195,00</td>
<td>1342,00</td>
<td>54,00</td>
<td>327,50</td>
</tr>
<tr>
<td>Gullubag</td>
<td>1288,00</td>
<td>5915,00</td>
<td>105,00</td>
<td>1147,00</td>
<td>96,00</td>
<td>284,50</td>
</tr>
<tr>
<td>Aksu</td>
<td>1492,00</td>
<td>6388,00</td>
<td>107,00</td>
<td>1042,00</td>
<td>130,00</td>
<td>344,40</td>
</tr>
<tr>
<td>Arkun</td>
<td>1743,56</td>
<td>6853,00</td>
<td>225,00</td>
<td>953,00</td>
<td>245,00</td>
<td>788,40</td>
</tr>
<tr>
<td>Yusufeli</td>
<td>3995,00</td>
<td>15250,00</td>
<td>196,30</td>
<td>712,00</td>
<td>558,00</td>
<td>1705,00</td>
</tr>
</tbody>
</table>
Upper Stream Projects of the Basin;

Laleli (Under Construction) Dam and HEPP:

Laleli Dam is the first dam on the river which is located in Bayburt province. The annual mean flow of the dam section is $879,16 \text{m}^3$ and area of the precipitation are $4759.00 \text{km}^2$. Total head of the project is $138.00 \text{m}$ and annual planned capacity is $244.55 \text{GWh}$ energy (Coruh River Basin Projects Report, 2009).

Ispir (2014) Dam and HEPP:

Ispir Dam is the second dam on the river which is located on the downstream of the Laleli Dam in Erzurum province. The annual mean flow of the dam section is $950.00 \text{m}^3$ and area of the precipitation are $5100.00 \text{km}^2$. Total head of the project is $195.00 \text{m}$ and annual planned capacity is $327.50 \text{GWh}$ energy (Coruh River Basin Projects Report, 2009).

Gullubag (2013) Dam and HEPP:

Gullubag Dam is the third dam on the river which is located in Erzurum province. The annual mean flow of the dam section is $1288.00 \text{m}^3$ and area of the precipitation are $5915.00 \text{km}^2$. Total head of the project is $105.00 \text{m}$ and annual planned capacity is $284.50 \text{GWh}$ energy (Coruh River Basin Projects Report, 2009).

Aksu (Under Construction) Dam and HEPP:

Aksu Dam is the fourth dam on the river which is located in Erzurum province. The annual mean flow of the dam section is $1492.00 \text{m}^3$ and area of the precipitation are $6388.00 \text{km}^2$. Total head of the project is $107.00 \text{m}$ and annual planned capacity is $344.40 \text{GWh}$ energy (Coruh River Basin Projects Report, 2009).

Arkun (2014) Dam and HEPP:

The fifth dam of the river, Arkun Dam, is located downstream of the Aksu Dam and located in Erzurum province. The annual mean flow of the dam section is $1743.56 \text{m}^3$ and area of the precipitation are $6853.00 \text{km}^2$. Total head of the project is $225.00 \text{m}$ and annual planned capacity is $788.40 \text{GWh}$ energy (Coruh River Basin Projects Report, 2009).
**Middle Stream Projects of the Basin:**

**Yusufeli (Under construction) Dam and HEPP:**

The first dam of the Middle Stream of the Basin, Yusufeli Dam, is located downstream of the Arkun Dam and located in Artvin province. The annual mean flow of the dam section is 3995.00m$^3$ and area of the precipitation are 15,250.00km$^2$. Total head of the project is 196.30m and annual planned capacity is 1705.00GWh energy (Coruh River Basin Projects Report, 2009).

### 2.5. Data Sets

In this study monthly runoff discharge predictions are made over 6 streamflow observation stations maintained by General Directorate of State Hydraulic Works (DSI) using precipitation data obtained from three ground-based stations that are maintained by Turkish State Meteorological Service (MGM) and remote sensing based precipitation data that are maintained by the Tropical Rainfall Measuring Mission (TRMM). MGM and DSI perform the measurement of meteorologic and hydraulic observations in Turkey. In this study, calculations made for monthly average of 42 years of MGM and DSI observations. Data period is chosen as 1970-2011. TRMM is a collective mission between National Aeronautics and Space Administration (NASA) and the Japan Aerospace Exploration (JAXA), provided 17 years of precipitation data. In this study, calculations made for monthly average of 12 years. The time interval is chosen as 2000-2011.

Coruh Basin is divided into 6 sub-basins with regarding the catchment areas of the observation stations. TRMM pixel grid and MGM precipitation data coupled with these flow observation stations. Figure 2.18 shows the Sub-Basins and locations of TRMM measurement pixels and ground-based observation stations. Information about the coupling the data sets are provided in the following section.
Figure 2.18 Sub-Basins and locations of TRMM measurement pixels and land observation stations
2.5.1. TRMM Precipitation Data

The Tropical Rainfall Measuring Mission (TRMM) is a collective mission between National Aeronautics and Space Administration (NASA) and Japan Aerospace Exploration (JAXA) provided 17 years of precipitation data. TRMM carried 5 instruments: 3-sensor rainfall and 2 related instruments. Names of sensors are as following; TMI – TRMM Microwave Imaging, VIRS – Visible Infrared Scanner, PR – Precipitation Radar, LIS – Lightning Imaging Sensor, CERES – Clouds and Earth’s Radiant Energy System. For seventeen years TRMM satellite helped to understand the hydrologic cycle of the climate system of the tropical and sub-tropical regions of the earth. Launched in November 1997 and stopped receiving observations on April 15, 2015. TRMM delivered valuable scientific data about global precipitation and lightning (Web-5).

In this study, TRMM 3B42 V7 daily precipitation product is used by converting into monthly average precipitation value. 25kmx25km Pixels size is used. Figure 2.19 shows the TRMM pixels which cover the Coruh Basin (indices shown in Figure 2.19 is only for demonstration purposes).

![Figure 2.19 TRMM pixels and sub-basins](image-url)
The TRMM data set became the standard satellite measurement for precipitation and improved our understanding of tropical cyclone structure and evolution, convective system properties, lightning-storm relationships, climate and weather modeling, and human impacts on rainfall. The data also added utility to calculations such as flood and drought risk mapping and weather forecasting.

2.5.2. MGM Gauge-based Precipitation Data

MGM performs the measurement of meteorologic observations in Turkey. MGM was founded in 1937 to make observations, provide forecast, climatological data and archive data. MGM provides meteorological data obtained from manual and automatic meteorologic observation stations all over the Turkey. In this study, daily precipitation data obtained from ground-based manual observation station data for the years 1970 to 2011 is used. Figure 2.20 shows the MGM observation station locations over digital elevation map.

<table>
<thead>
<tr>
<th>Station No</th>
<th>longitude</th>
<th>latitude</th>
<th>Elevation(m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>17086</td>
<td>40.25</td>
<td>40.22</td>
<td>1584</td>
</tr>
<tr>
<td>17666</td>
<td>40.40</td>
<td>41.00</td>
<td>1221</td>
</tr>
<tr>
<td>17668</td>
<td>40.55</td>
<td>42.00</td>
<td>1312</td>
</tr>
</tbody>
</table>

Figure 2.20 MGM meteorological station locations over DEM map
- 17089 – Bayburt Center Meteorologic Observation Station Data
- 17666 – Erzurum Oltu Meteorologic Observation Station Data
- 17668 – Erzurum Tortum Meteorologic Observation Station Data

### 2.5.3. DSI Gauge-based Streamflow Data

DSI performs the measurement of hydrologic observations in Turkey. DSI was founded in 1954 and has a vision about protection, management, and development of water resources and responsible for providing hydrologic data sets to the public (www.DSI.gov.tr). In this study six DSI streamflow observation station data that covers the years 1970 to 2011 is used. Figure 2.21 shows DSI Streamflow Observation Station Locations.

![Figure 2.21 DSI streamflow observation station locations](image-url)
• E23A004 – Bayburt Coruh River Flow Observation Station
• E23A005 – Peterek Coruh River Flow Observation Station
• E23A016 – Ispir Bridge Coruh River Flow Observation Station
• E23A020 – Laleli Coruh River Flow Observation Station
• E23A021 – Dutdere Parhal Creek Flow Observation Station
• E23A023 – Ishan Bridge Oltu Creek Flow Observation Station

2.6. Runoff Predictions

Monthly runoff predictions over each of six DSI stations are made using three different data sets. These data sets are respectively; DSI streamflow observation station data coupled with nearest MGM Station rainfall data, DSI streamflow observation station data coupled with TRMM Single Pixel (only pixel which covers the DSI streamflow observation station location) precipitation data and lastly DSI streamflow observation station data coupled with TRMM Catchment Average (all TRMM measurement pixels which cover the sub-basin of DSI streamflow observation station) rainfall.

Figure 18 shows the Sub-Basins and locations of TRMM measurement pixels and land observation stations. Following sections provide detailed information about the data coupling with respect to DSI observation stations.
2.6.1. Station E23A004

Three different rainfall-runoff data sets are coupled for the flow predictions of DSI streamflow observation station E23A004. Figure 2.22 shows the catchment area of the DSI streamflow observation station E23A004 and location, TRMM measurement pixels and MGM rainfall observation station locations. Below three scenarios are performed to investigate the relationship between precipitation and runoff in detail.

- DSI E23A004 Streamflow Data coupled with MGM 17089 station rainfall data
- DSI E23A004 Streamflow Data coupled with TRMM Pixel no 1.5 data (Pixel no 1.5 covers the station E23A004)
- DSI E23A004 Streamflow Data coupled with average of TRMM Pixels no 1.5, 1.6, 2.5, 2.6, 3.5, 3.6, 4.5, 4.6, 5.5 data (Pixels cover the catchment area of E23A004 station)

Figure 2.22 Location map of Station E23A004 and related MGM Station and TRMM Pixels
2.6.2. Station E23A005

Three different rainfall-runoff data sets are coupled for the flow predictions of DSI streamflow observation station E23A005. Figure 2.23 shows the catchment area of the DSI streamflow observation station E23A005 and location, TRMM measurement pixels and MGM rainfall observation station locations. Below three scenarios are performed to investigate the relationship between precipitation and runoff in detail.

- DSI E23A005 Streamflow Data coupled with MGM 17666 station rainfall data
- DSI E23A005 Streamflow Data coupled with TRMM Pixel no 6.3 data (Pixel no 6.3 covers the station E23A005)
- DSI E23A005 Streamflow Data coupled with average of TRMM Pixels no 0.4, 0.5, 0.6, 1.4, 1.5, 1.6, 2.4, 2.5, 2.6, 3.4, 3.5, 3.6, 4.3, 4.4, 4.5, 5.3, 5.4, 6.3, 6.4 data (Pixels cover the catchment area of E23A005 station)

Figure 2.23 Location map of Station E23A005 and related MGM Station and TRMM Pixels
2.6.3. Station E23A016

Three different rainfall-runoff data sets are coupled for the flow predictions of DSI streamflow observation station E23A016. Figure 2.24 shows the catchment area of the DSI streamflow observation station E23A016 and location, TRMM measurement pixels and MGM rainfall observation station locations. Below three scenarios are performed to investigate the relationship between precipitation and runoff in detail.

- DSI E23A016 Streamflow Data coupled with MGM 17666 station rainfall data
- DSI E23A016 Streamflow Data coupled with TRMM Pixel no 4.4 data (Pixel no 4.4 covers the station E23A016)
- DSI E23A016 Streamflow Data coupled with average of TRMM Pixels no 0.4, 0.5, 0.6, 1.4, 1.5, 1.6, 2.4, 2.5, 2.6, 3.4, 3.5, 3.6, 4.3, 4.4, 4.5, data (Pixels cover the catchment area of E23A016 station)

Figure 2.24 Location map of Station E23A016 and related MGM Station and TRMM Pixels
2.6.4. Station E23A020

Three different rainfall-runoff data sets are coupled for the flow predictions of DSI streamflow observation station E23A020. Figure 2.25 shows the catchment area of the DSI streamflow observation station E23A020 and location, TRMM measurement pixels and MGM rainfall observation station locations. Below three scenarios are performed to investigate the relationship between precipitation and runoff in detail.

- DSI E23A020 Streamflow Data coupled with MGM 17089 station rainfall data
- DSI E23A020 Streamflow Data coupled with TRMM Pixel no 3.5 data (Pixel no 3.5 covers the station E23A020)
- DSI E23A020 Streamflow Data coupled with average of TRMM Pixels no 0.4, 0.5, 0.6, 1.4, 1.5, 1.6, 2.4, 2.5, 2.6, 3.4, 3.5, 3.6, 4.5, data (Pixels cover the catchment area of E23A020 station)

Figure 2.25 Location map of Station E23A020 and related MGM Station and TRMM Pixels
2.6.5. Station E23A021

Three different rainfall-runoff data sets are coupled for the flow predictions of DSI streamflow observation station E23A021. Figure 2.26 shows the catchment area of the DSI streamflow observation station E23A021 and location, TRMM measurement pixels and MGM rainfall observation station locations. Below three scenarios are performed to investigate the relationship between precipitation and runoff in detail.

- DSI E23A021 Streamflow Data coupled with MGM 17668 station rainfall data
- DSI E23A021 Streamflow Data coupled with TRMM Pixel no 6.3 data (Pixel no 6.3 covers the station E23A021)
- DSI E23A021 Streamflow Data coupled with average of TRMM Pixels no5.2, 5.3, 6.2, 6.3 data (Pixels cover the catchment area of E23A021 station)

![Location map of Station E23A021 and related MGM Station and TRMM Pixels](image)

Figure 2.26 Location map of Station E23A021 and related MGM Station and TRMM Pixels
2.6.6. **Station E23A023**

Three different rainfall-runoff data sets are coupled for the flow predictions of DSI streamflow observation station E23A023. Figure 2.27 shows the catchment area of the DSI streamflow observation station E23A023 and location, TRMM measurement pixels and MGM rainfall observation station locations. Below three scenarios are performed to investigate the relationship between precipitation and runoff in detail.

- DSI E23A023 Streamflow Data coupled with MGM 17668 station rainfall data
- DSI E23A023 Streamflow Data coupled with TRMM Pixel no 7.3 data (Pixel no 7.3 covers the station E23A023)
- DSI E23A023 Streamflow Data coupled with average of TRMM Pixels no 5.4, 5.5, 6.4, 6.5, 7.3, 7.4, 7.5, 8.3, 8.4, 8.5, 9.3, 9.4, 9.5, 10.3, 10.4 data (Pixels cover the catchment area of E23A023 station)

![Figure 2.27 Location map of Station E23A023 and related MGM Station and TRMM Pixels](image)

53
2.7. Performance Statistics

Generally, in statistical analysis, data split into two parts where some are reserved for the training while the remaining part is reserved for the validation. Statistician must be sure about the data set is the best set, which, lead the statistician to reliable results. This is really difficult and critical for forecasting. The point must be taken into consideration is that the training data set must include all kind of observation in it. The following section gives brief information on performance statistics to evaluate different model prediction performances.

**Correlation Coefficient**

The correlation coefficient is used to describe the relation between two or more variables. It is a degree of consistency between the variables. Correlation value between the observed and predicted streamflow data is calculated as follows;

\[
r_{o,p} = \frac{n(\Sigma op) - (\Sigma o)(\Sigma p)}{\sqrt{n(\Sigma o^2) - (\Sigma o)^2} \sqrt{n(\Sigma p^2) - (\Sigma p)^2}}
\]

(2.43)

Where, \( r_{o,p} \) is the correlation coefficient between the observed data and predicted values of streamflow “\( o \)” is the observation, “\( p \)” is the predicted value and \( n \) is number of data.

**Mean Error;**

Mean Error is used to describe the average of all errors between the observed and predicted streamflow data. Where “\( e \)” is the error.

\[
e_i = o_i - p_i
\]

(2.44)
\[ \mu_e = \frac{\sum_{i=1}^{n} e}{n} \]  \hspace{1cm} (2.45)

**Standard Deviation of Data and Standard Deviation of Error:**

Standard Deviation of Data and Standard Error of Predicted Data is used to describe standardized deviations of data and error terms. Greater standard deviation in error than the standard deviation of data indicates the unuseful predictions.

\[ \sigma_x = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (x_i - \mu_x)^2} \]  \hspace{1cm} (2.46)

**Root Mean Squared Error:**

Root Mean Squared Error is used to describe the square root of the mean of the square of all errors.

\[ RMSE = \sqrt{\frac{1}{n} \sum e^2} \]  \hspace{1cm} (2.47)
CHAPTER 3

RESULTS and DISCUSSIONS

3.1. Analysis of Precipitation Data

MGM ground-based precipitation data sets and related TRMM observation data sets compared and correlation coefficients between full-time series, climatology components, and anomaly components are given in Table 3.1.

Table 3.1 Correlations between MGM station data and TRMM product

<table>
<thead>
<tr>
<th>Stations</th>
<th>Correlations Between Precipitation Datasets</th>
</tr>
</thead>
<tbody>
<tr>
<td>MGM - TRMM Single Pixel (Climatology)</td>
<td>0.566</td>
</tr>
<tr>
<td>MGM - TRMM Single Pixel (Complete TimeSerie)</td>
<td>0.640</td>
</tr>
<tr>
<td>MGM - TRMM Single Pixel (Anomaly Component)</td>
<td>0.597</td>
</tr>
<tr>
<td>MGM - TRMM Catchment Average (Climatology)</td>
<td>0.659</td>
</tr>
<tr>
<td>MGM - TRMM Catchment Average (Complete TimeSerie)</td>
<td>0.584</td>
</tr>
<tr>
<td>MGM - TRMM Catchment Average (Anomaly Component)</td>
<td>0.541</td>
</tr>
</tbody>
</table>

In the calculations nearest MGM observation station data and TRMM pixel data which covers the related DSI streamflow stations are coupled. As the distance between the MGM station and TRMM Pixel (which covers the DSI Streamflow Station) increases, poor correlations are obtained. In that cases, TRMM Catchment Average data sets are provided relatively better correlations with the MGM ground-based precipitation observations.
On the other hand, correlation coefficient values between climatology components of data sets are expected to show higher values than the full-time series and anomaly component correlations. Anomaly component correlation coefficient values are expected to show lower values. In this aspect, MGM ground-based observations and TRMM satellite measurements show some inconsistency.

### 3.2. Analysis of Streamflow Data

Another correlation calculation is made for the DSI station observations between years 1970 and 2011. In the absence of data for a specific station or an ungauged region of the basin other station observations can provide insights about the region or can be used to complete missing data in the time series. Table 3.2 shows the correlations between the DSI Streamflow Observation stations.

<table>
<thead>
<tr>
<th>Correlations</th>
<th>E23A004</th>
<th>E23A005</th>
<th>E23A016</th>
<th>E23A020</th>
<th>E23A021</th>
<th>E23A023</th>
</tr>
</thead>
<tbody>
<tr>
<td>E23A004</td>
<td>1,000</td>
<td>0.968</td>
<td>0.967</td>
<td>0.973</td>
<td>0.828</td>
<td>0.941</td>
</tr>
<tr>
<td>E23A005</td>
<td>0.968</td>
<td>1,000</td>
<td>0.979</td>
<td>0.970</td>
<td>0.883</td>
<td>0.935</td>
</tr>
<tr>
<td>E23A016</td>
<td>0.967</td>
<td>0.979</td>
<td>1,000</td>
<td>0.985</td>
<td>0.810</td>
<td>0.909</td>
</tr>
<tr>
<td>E23A020</td>
<td>0.973</td>
<td>0.970</td>
<td>0.985</td>
<td>1,000</td>
<td>0.788</td>
<td>0.909</td>
</tr>
<tr>
<td>E23A021</td>
<td>0.828</td>
<td>0.883</td>
<td>0.810</td>
<td>0.788</td>
<td>1,000</td>
<td>0.805</td>
</tr>
<tr>
<td>E23A023</td>
<td>0.941</td>
<td>0.935</td>
<td>0.909</td>
<td>0.909</td>
<td>0.805</td>
<td>1,000</td>
</tr>
</tbody>
</table>

It is expected that Persistence-Based predictions would provide better correlation results for a streamflow time series with a lag-1 autocorrelation coefficient greater than 0.50 than the Climatology-Based Predictions. Table 3.3 shows the lag-1 autocorrelations, mean values, standard deviations and % of the variability of the DSI Streamflow Observation stations data.
Table 3.3 DSI streamflow observation stations data statistics and autocorrelation values

<table>
<thead>
<tr>
<th>Stations</th>
<th>Lag-1 Auto Correlation</th>
<th>Mean</th>
<th>Standard Deviation</th>
<th>% of Variability of Data</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Full TimeSerie</td>
<td>Climatology</td>
<td>Anomaly</td>
<td>Full TimeSerie</td>
</tr>
<tr>
<td>E23A004</td>
<td>0.60</td>
<td>15,512</td>
<td>15,959</td>
<td>-0.447</td>
</tr>
<tr>
<td>E23A005</td>
<td>0.67</td>
<td>69,194</td>
<td>69,194</td>
<td>0.000</td>
</tr>
<tr>
<td>E23A016</td>
<td>0.63</td>
<td>38,983</td>
<td>38,983</td>
<td>0.000</td>
</tr>
<tr>
<td>E23A020</td>
<td>0.62</td>
<td>29,387</td>
<td>29,387</td>
<td>0.000</td>
</tr>
<tr>
<td>E23A021</td>
<td>0.70</td>
<td>14,058</td>
<td>14,058</td>
<td>0.000</td>
</tr>
<tr>
<td>E23A023</td>
<td>0.55</td>
<td>33,506</td>
<td>32,708</td>
<td>0.798</td>
</tr>
</tbody>
</table>

Deviations of streamflow data show that climatology component of streamflow data contains more than 80% of variability while anomaly component contains approximately 20% of total variability.

The hypsometric curve of the basin (Figure 3.1) shows that the elevation of the basin changes between the 0m and 4000m and approximately 40% of the basin surface area is above the 2000m elevation. This condition causes great temperature changes between higher and lower places of the basin. Precipitation that falls to the basin is preserved in form of snow due to this temperature changes on the higher grounds and, with the increasing temperatures in April and May, melting snow participates to the streamflow forming peak values of streamflow.

![Hypsometric Curve](image)

Figure 3.1 Hypsometric curve of the Coruh Basin
3.3. Streamflow Predictions

Streamflow predictions are made for each of 6 available streamflow observations. These predictions are made using 3 different precipitation data sets (MGM ground-based observations, TRMM Single Pixel and TRMM Catchment Average measurements). 6 different methods (SLR, MLR, ANN, Copula, Climatology, and Persistence) used with 2 different data set components (complete data sets and anomaly components only). Climatology and Persistence predictions form the benchmarks that the predictions are compared against.
3.3.1. Station E23A004

3.3.1.1. Predictions Using Meteorology Data

Figure 3.2 shows the validation time series of the predictions and performance statistics of validation time series are provided in Table 3.4. Overall correlations and RMSE values show a consistent pattern; the methods with higher correlation values have lower RMSE value. Among all the complete data set predictions, Persistence-Based predictions provided the best result for the streamflow data while Climatology-Based predictions of the streamflow have approximately 0.90 correlations with the validation data.

![Figure 3.2 Station E23A004 DSI streamflow data v.s. meteorology precipitation data complete dataset predictions](image-url)

Figure 3.2 Station E23A004 DSI streamflow data v.s. meteorology precipitation data complete dataset predictions
Table 3.4 Performance statistics of station E23A004 with meteorology data - complete data set predictions

<table>
<thead>
<tr>
<th>Performance Statistics</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Correlations</td>
<td>0.919</td>
<td>0.919</td>
<td>0.531</td>
<td>0.531</td>
<td>0.545</td>
<td>0.453</td>
<td>0.551</td>
</tr>
<tr>
<td>Mean Error</td>
<td>2.110</td>
<td>-0.094</td>
<td>1.436</td>
<td>1.415</td>
<td>1.244</td>
<td>8.790</td>
<td>9.227</td>
</tr>
<tr>
<td>Mean of Observations</td>
<td>15.512</td>
<td>15.512</td>
<td>15.512</td>
<td>15.512</td>
<td>15.512</td>
<td>15.512</td>
<td>15.512</td>
</tr>
</tbody>
</table>

Similar results are obtained from the SLR, MLR and MLP models but showing under 0.60 correlation. Copula functions couldn’t identify a skillful relationship for complete data sets as the other models. To further investigate the source of the predictive skills of these methods, additional predictions are made using the standardized anomaly components of data sets. Figure 3.3 shows the validation time series of the anomaly component predictions.

![Figure 3.3 Station E23A004 DSI streamflow data v.s. meteorology precipitation data anomaly component data set predictions](image-url)
Addition of climatology component to the standardized anomaly component predictions showed above 0.90 correlations, these improved predictions are showing heavy majority of the predictive skill and the relation between the precipitation and the streamflow data sets are due to the strong seasonality.

Correlations of predictions which are obtained from the SLR, MLR, MLP and Copula models increased from 0.50 to above 0.90 with decreasing RMSE values and mean error. Performance statistics of validation time series are provided in Table 3.5.

Table 3.5 Performance statistics of station E23A004 with meteorology data – anomaly component data set predictions

<table>
<thead>
<tr>
<th>Performance Statistics</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Correlations</td>
<td>0.915</td>
<td>0.910</td>
<td>0.948</td>
<td>0.916</td>
<td>0.913</td>
<td>0.927</td>
<td>0.920</td>
</tr>
<tr>
<td>Mean Error</td>
<td>2.110</td>
<td>-0.094</td>
<td>3.023</td>
<td>2.916</td>
<td>0.009</td>
<td>3.356</td>
<td>3.658</td>
</tr>
<tr>
<td>Mean of Observations</td>
<td>15.512</td>
<td>15.512</td>
<td>15.512</td>
<td>15.512</td>
<td>15.512</td>
<td>15.512</td>
<td>15.512</td>
</tr>
</tbody>
</table>
3.3.1.2. Predictions Using TRMM Single Pixel Data

Figure 3.4 shows the validation time series of the predictions and performance statistics of validation time series are provided in Table 3.6. Overall correlations and RMSE values show a consistent pattern; the methods with higher correlation values have lower RMSE value. Among all the complete data set predictions, Persistence-Based predictions provided the best result for the streamflow data while Climatology-Based predictions of the streamflow have over 0.90 correlations with the validation data.

Figure 3.4 Station E23A004 DSI streamflow data v.s. TRMM single pixel precipitation data complete data set predictions
<table>
<thead>
<tr>
<th>Model</th>
<th>Performance Statistics</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Climatology</td>
</tr>
<tr>
<td>Correlations</td>
<td>0.962</td>
</tr>
<tr>
<td>Mean Error</td>
<td>-0.518</td>
</tr>
<tr>
<td>Mean of Observations</td>
<td>15.512</td>
</tr>
</tbody>
</table>

Similar results are obtained from the SLR, MLR, MLP and Copula models but showing under 0.30 correlation and some artificial skills. These models could not identify a skillful relationship between the Rainfall and Runoff mainly due to lack of data. 9 years of monthly streamflow data and precipitation data could not train the models.

![Figure 3.5 Station E23A004 DSI streamflow data v.s. TRMM single pixel precipitation data anomaly component data set predictions](image-url)
Additional predictions are made using the standardized anomaly components of data sets. Figure 3.5 shows the validation time series of the anomaly component predictions.

Addition of Climatology component to the standardized anomaly component predictions showed above 0.90 correlations, these improved predictions are showing heavy majority of the predictive skill and the relation between the precipitation and the streamflow data sets are due to the strong seasonality.

Correlations of predictions which are obtained from the SLR, MLR, MLP and Copula models increased from 0.20 to above 0.90 with decreasing RMSE values and mean error. Performance statistics of validation time series are provided in Table 3.7.

Table 3.7 Performance statistics of station E23A004 with TRMM single pixel data – anomaly component data set predictions

<table>
<thead>
<tr>
<th>Model</th>
<th>Performance Statistics</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Climatology</td>
</tr>
<tr>
<td>Correlations</td>
<td>0.963</td>
</tr>
<tr>
<td>Mean Error</td>
<td>-0.528</td>
</tr>
<tr>
<td>Mean of Observations</td>
<td>15.512</td>
</tr>
</tbody>
</table>
3.3.1.3. Predictions Using TRMM Catchment Average Data

Figure 3.6 shows the validation time series of the predictions and performance statistics of validation time series are provided in Table 3.8. Overall correlations and RMSE values show a consistent pattern; the methods with higher correlation values have lower RMSE value. Among all the complete data set predictions, Persistence-Based predictions provided the best result for the streamflow data while Climatology-Based predictions of the streamflow have over 0.90 correlations with the validation data.

![Figure 3.6 Station E23A004 DSI streamflow data v.s. TRMM catchment average precipitation data complete data set predictions](image)

Figure 3.6 Station E23A004 DSI streamflow data v.s. TRMM catchment average precipitation data complete data set predictions
Table 3.8 Performance statistics of station E23A004 with TRMM catchment average data - complete data set predictions

<table>
<thead>
<tr>
<th>Model</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Correlations</td>
<td>0.903</td>
<td>0.903</td>
<td>0.198</td>
<td>0.250</td>
<td>-0.043</td>
<td>0.196</td>
<td>0.166</td>
</tr>
<tr>
<td>Mean Error</td>
<td>-0.518</td>
<td>-0.178</td>
<td>-0.994</td>
<td>-0.793</td>
<td>-0.889</td>
<td>-8.119</td>
<td>-8.109</td>
</tr>
<tr>
<td>Mean of Observations</td>
<td>15.512</td>
<td>15.512</td>
<td>15.512</td>
<td>15.512</td>
<td>15.512</td>
<td>15.512</td>
<td>15.512</td>
</tr>
</tbody>
</table>

Similar results are obtained from the SLR, MLR, MLP and Copula models but showing under 0.30 correlation. These models could not identify a skillful relationship between the Rainfall and Runoff mainly due to lack of data. 9 years of monthly streamflow data and precipitation data could not train the models.

Additional predictions are made using the standardized anomaly components of data sets. Figure 3.7 shows the validation time series of the anomaly component predictions.

Figure 3.7 Station E23A004 DSI streamflow data v.s. TRMM catchment average precipitation data anomaly component data set predictions

68
Addition of Climatology component to the standardized anomaly component predictions showed above 0.90 correlations, these improved predictions are showing heavy majority of the predictive skill and the relation between the precipitation and the streamflow data sets are due to the strong seasonality.

Correlations of predictions which are obtained from the SLR, MLR, MLP and Copula models increased from 0.20 to above 0.90 with decreasing RMSE values and mean error term. Performance statistics of validation time series are provided in Table 3.9.

Table 3.9 Performance statistics of station E23A004 with catchment average data – anomaly component data set predictions

<table>
<thead>
<tr>
<th>Performance Statistics</th>
<th>Performance Statistics</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model</td>
<td>Climatology</td>
</tr>
<tr>
<td>Correlations</td>
<td>0.962</td>
</tr>
<tr>
<td>Mean Error</td>
<td>-0.518</td>
</tr>
<tr>
<td>RMSE</td>
<td>4.145</td>
</tr>
<tr>
<td>Mean of Observations</td>
<td>15.512</td>
</tr>
</tbody>
</table>
3.3.2. Station E23A005

3.3.2.1. Predictions Using Meteorology Data

Figure 3.8 shows the validation time series of the predictions and performance statistics of validation time series are provided in Table 3.10. Overall correlations and RMSE values show a consistent pattern; the methods with higher correlation values have lower RMSE value. Among all the complete data set predictions, Climatology-Based predictions provided the best result for the streamflow data while Persistence-Based predictions of the streamflow have approximately 0.90 correlations with the validation data.

Figure 3.8 Station E23A005 DSI streamflow data v.s. meteorology precipitation data complete data set predictions
Table 3.10 Performance statistics of station E23A005 with meteorology data - complete data set predictions

<table>
<thead>
<tr>
<th>Performance Statistics</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Correlations</td>
<td>0.931</td>
<td>0.886</td>
<td>0.604</td>
<td>0.605</td>
<td>0.437</td>
<td>0.432</td>
<td>0.427</td>
</tr>
<tr>
<td>Standard Deviation of Observation</td>
<td>84.275</td>
<td>84.275</td>
<td>84.275</td>
<td>84.275</td>
<td>84.275</td>
<td>84.275</td>
<td>84.275</td>
</tr>
<tr>
<td>Standard Deviation of Errors</td>
<td>32,639</td>
<td>42,381</td>
<td>67,181</td>
<td>67,111</td>
<td>76,470</td>
<td>83,714</td>
<td>83,661</td>
</tr>
<tr>
<td>Mean Error</td>
<td>13,073</td>
<td>2,448</td>
<td>5,049</td>
<td>4,519</td>
<td>9,650</td>
<td>51,692</td>
<td>51,675</td>
</tr>
<tr>
<td>RMSE</td>
<td>35,279</td>
<td>42,231</td>
<td>67,020</td>
<td>66,914</td>
<td>76,681</td>
<td>98,016</td>
<td>97,962</td>
</tr>
<tr>
<td>Mean of Observations</td>
<td>69,194</td>
<td>69,194</td>
<td>69,194</td>
<td>69,194</td>
<td>69,194</td>
<td>69,194</td>
<td>69,194</td>
</tr>
</tbody>
</table>

Similar results are obtained from the SLR and MLR models but showing 0.60 correlation. MLP model seems to identify the relationship but showing 0.40 correlation. Copula functions couldn’t identify a skillful relationship for complete data sets.

Figure 3.9 Station E23A005 DSI streamflow data v.s. meteorology precipitation data anomaly component data set predictions
To further investigate the source of the predictive skills of these methods, additional predictions are made using the standardized anomaly components of data sets. Figure 3.9 shows the validation time series of the anomaly component predictions.

Addition of Climatology component to the standardized anomaly component predictions showed above 0.90 correlations, these improved predictions are showing heavy majority of the predictive skill and the relation between the precipitation and the streamflow data sets are due to the strong seasonality.

Correlations of predictions which are obtained from the SLR, MLR, MLP, and Copula models increased from 0.40 to above 0.90 with decreasing RMSE values and mean error term. Performance statistics of validation time series are provided in Table 3.11.

Table 3.11 Performance statistics of station E23A005 with meteorology data – anomaly component data set predictions

<table>
<thead>
<tr>
<th>Model</th>
<th>Performance Statistics</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Climatology</td>
</tr>
<tr>
<td>Correlations</td>
<td>0.939</td>
</tr>
<tr>
<td>Standard Deviation of Observation</td>
<td>84.27%</td>
</tr>
<tr>
<td>Standard Deviation of Errors</td>
<td>32.93%</td>
</tr>
<tr>
<td>Mean Error</td>
<td>13,073</td>
</tr>
<tr>
<td>RMSE</td>
<td>35.279</td>
</tr>
<tr>
<td>Mean of Observations</td>
<td>69.154</td>
</tr>
</tbody>
</table>
3.3.2.2. Predictions Using TRMM Single Pixel Data

Figure 3.10 shows the validation time series of the predictions and performance statistics of validation time series are provided in Table 3.12. Overall correlations and RMSE values show a consistent pattern; the methods with higher correlation values have lower RMSE value. Among all the complete data set predictions, Climatology-Based predictions provided the best result for the streamflow data while Persistence-Based predictions of the streamflow have approximately 0.90 correlations with the validation data.

![Figure 3.10 Station E23A005 DSI streamflow data v.s. TRMM single pixel precipitation data complete data set predictions](image-url)
Table 3.12 Performance statistics of station E23A005 with TRMM single pixel data - complete data set predictions

<table>
<thead>
<tr>
<th>Performance Statistics</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Correlations</td>
<td>0.943</td>
<td>0.938</td>
<td>0.228</td>
<td>0.269</td>
<td>0.238</td>
<td>0.139</td>
<td>0.152</td>
</tr>
<tr>
<td>Standard Deviation of Observation</td>
<td>77.820</td>
<td>77.820</td>
<td>77.820</td>
<td>77.820</td>
<td>77.820</td>
<td>77.820</td>
<td>77.820</td>
</tr>
<tr>
<td>Standard Deviation of Errors</td>
<td>26.538</td>
<td>29.092</td>
<td>75.828</td>
<td>74.980</td>
<td>75.759</td>
<td>77.144</td>
<td>80.474</td>
</tr>
<tr>
<td>Mean Error</td>
<td>8.732</td>
<td>-3.210</td>
<td>2.980</td>
<td>4.332</td>
<td>0.546</td>
<td>38.938</td>
<td>8.002</td>
</tr>
<tr>
<td>RMSE</td>
<td>27.585</td>
<td>28.864</td>
<td>74.827</td>
<td>74.058</td>
<td>74.703</td>
<td>85.452</td>
<td>79.750</td>
</tr>
<tr>
<td>Mean of Observations</td>
<td>69.194</td>
<td>69.194</td>
<td>69.194</td>
<td>69.194</td>
<td>69.194</td>
<td>69.194</td>
<td>69.194</td>
</tr>
</tbody>
</table>

Similar results are obtained from the SLR, MLR, MLP and Copula models but showing under 0.30 correlation. These models could not identify a skillful relationship between the Rainfall and Runoff mainly due to lack of data. 9 years of monthly streamflow data and precipitation data could not be enough to train the models.

Figure 3.11 Station E23A005 DSI streamflow data v.s. TRMM single pixel precipitation data anomaly component data set predictions
Additional predictions are made using the standardized anomaly components of data sets. Figure 3.11 shows the validation time series of the anomaly component predictions.

Addition of Climatology component to the standardized anomaly component predictions showed above 0.90 correlations, these improved predictions are showing heavy majority of the predictive skill and the relation between the precipitation and the streamflow data sets are due to the strong seasonality.

Correlations of predictions which are obtained from the SLR, MLR, MLP and Copula models increased from 0.20 to above 0.90 with decreasing RMSE values and mean error term. Performance statistics of validation time series are provided in Table 3.13.

Table 3.13 Performance statistics of station E23A005 with TRMM single pixel data – anomaly component data set predictions

<table>
<thead>
<tr>
<th>Performance Statistics</th>
<th>Model</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Correlation</td>
<td></td>
<td>0.945</td>
<td>0.945</td>
<td>0.945</td>
<td>0.945</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Standard Deviation of Observation</td>
<td>77.820</td>
<td>77.820</td>
<td>77.820</td>
<td>77.820</td>
<td>77.820</td>
<td>77.820</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Mean of Observations</td>
<td>69.194</td>
<td>69.194</td>
<td>69.194</td>
<td>69.194</td>
<td>69.194</td>
<td>69.194</td>
<td>69.194</td>
<td></td>
</tr>
</tbody>
</table>
3.3.2.3. Predictions Using TRMM Catchment Average Data

Figure 3.12 shows the validation time series of the predictions and performance statistics of validation time series are provided in Table 3.14. Overall correlations and RMSE values show a consistent pattern; the methods with higher correlation values have lower RMSE value. Among all the complete data set predictions, Climatology-Based predictions provided the best result for the streamflow data while Persistence-Based predictions of the streamflow have approximately 0.90 correlations with the validation data.

![Figure 3.12 Station E23A005 DSI streamflow data v.s. TRMM catchment average precipitation data complete data set predictions](image-url)

Figure 3.12 Station E23A005 DSI streamflow data v.s. TRMM catchment average precipitation data complete data set predictions
Table 3.14 Performance statistics of station E23A005 with TRMM catchment average data - complete data set predictions

<table>
<thead>
<tr>
<th>Model</th>
<th>Performance Statistics</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Climatology</td>
</tr>
<tr>
<td>Correlations</td>
<td>0.943</td>
</tr>
<tr>
<td>Standard Deviation of Observation</td>
<td>77.820</td>
</tr>
<tr>
<td>Standard Deviation of Errors</td>
<td>26.538</td>
</tr>
<tr>
<td>Mean Error</td>
<td>8.732</td>
</tr>
<tr>
<td>RMSE</td>
<td>27.585</td>
</tr>
<tr>
<td>Mean of Observations</td>
<td>69.154</td>
</tr>
</tbody>
</table>

Similar results are obtained from the SLR, MLR, MLP and Copula models but showing under 0.20 correlation. These models could not identify a skillful relationship between the Rainfall and Runoff mainly due to lack of data. 9 years of monthly streamflow data and precipitation data could not train the models.

Figure 3.13 Station E23A005 DSI streamflow data v.s. TRMM catchment average precipitation data anomaly component data set predictions
Additional predictions are made using the standardized anomaly components of data sets. Figure 3.13 shows the validation time series of the anomaly component predictions.

Addition of Climatology component to the standardized anomaly component predictions showed above 0.90 correlations, these improved predictions are showing heavy majority of the predictive skill and the relation between the precipitation and the streamflow data sets are due to the strong seasonality.

Correlations of predictions which are obtained from the SLR, MLR, MLP and Copula models increased from 0.20 to above 0.90 with decreasing RMSE values and mean error term. Performance statistics of validation time series are provided in Table 3.15.

Table 3.15 Performance statistics of station E23A005 with catchment average data – anomaly component data set predictions

<table>
<thead>
<tr>
<th>Model</th>
<th>Performance Statistics</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Climatology</td>
</tr>
<tr>
<td>Correlations</td>
<td>0.943</td>
</tr>
<tr>
<td>Standard Deviation of Observation</td>
<td>77.820</td>
</tr>
<tr>
<td>Mean of Observations</td>
<td>69.154</td>
</tr>
</tbody>
</table>
3.3.3. Station E23A016

3.3.3.1. Predictions Using Meteorology Data

Figure 3.14 shows the validation time series of the predictions and performance statistics of validation time series are provided in Table 3.16. Overall correlations and RMSE values show a consistent pattern; the methods with higher correlation values have lower RMSE value. Among all the complete data set predictions, Climatology-Based predictions provided the best result for the streamflow data while Persistence-Based predictions of the streamflow have approximately 0.90 correlations with the validation data.

![Figure 3.14 Station E23A016 DSI streamflow data v.s. meteorology precipitation data complete dataset predictions](image)

Figure 3.14 Station E23A016 DSI streamflow data v.s. meteorology precipitation data complete dataset predictions
Table 3.16 Performance statistics of station E23A016 with meteorology data - complete data set predictions

<table>
<thead>
<tr>
<th>Model</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Correlations</td>
<td>0.922</td>
<td>0.859</td>
<td>0.253</td>
<td>0.253</td>
<td>0.458</td>
<td>0.431</td>
<td>0.441</td>
</tr>
<tr>
<td>Standard Deviation of Observation</td>
<td>54.960</td>
<td>54.960</td>
<td>54.960</td>
<td>54.960</td>
<td>54.960</td>
<td>54.960</td>
<td>54.960</td>
</tr>
<tr>
<td>Standard Deviation of Errors</td>
<td>23.663</td>
<td>30.152</td>
<td>53.485</td>
<td>53.479</td>
<td>49.453</td>
<td>54.731</td>
<td>54.695</td>
</tr>
<tr>
<td>Mean Error</td>
<td>7.927</td>
<td>-0.825</td>
<td>4.709</td>
<td>4.712</td>
<td>5.485</td>
<td>30.686</td>
<td>30.675</td>
</tr>
<tr>
<td>RMSE</td>
<td>24.829</td>
<td>30.004</td>
<td>53.413</td>
<td>53.408</td>
<td>49.499</td>
<td>62.497</td>
<td>62.460</td>
</tr>
<tr>
<td>Mean of Observations</td>
<td>38.983</td>
<td>38.983</td>
<td>38.983</td>
<td>38.983</td>
<td>38.983</td>
<td>38.983</td>
<td>38.983</td>
</tr>
</tbody>
</table>

Similar results are obtained from the SLR and MLR models but showing 0.20 correlation. Copula functions couldn’t identify a skillful relationship for complete data sets. MLP model is showed some artificial results. To further investigate the source of the predictive skills of these methods, additional predictions are made using the standardized anomaly components of data sets. Figure 3.15 shows the validation time series of the anomaly component predictions.

Figure 3.15 Station E23A016 DSI streamflow data v.s. meteorology precipitation data anomaly component data set predictions
Addition of Climatology component to the standardized anomaly component predictions showed above 0.90 correlations, these improved predictions are showing heavy majority of the predictive skill and the relation between the precipitation and the streamflow data sets are due to the strong seasonality.

Correlations of predictions which are obtained from the SLR, MLR, MLP and Copula models increased from 0.20 to above 0.90 with decreasing RMSE values and mean error term. Performance statistics of validation time series are provided in Table 3.17.

Table 3.17 Performance statistics of station E23A016 with meteorology data – anomaly component data set predictions

<table>
<thead>
<tr>
<th>Performance Statistics</th>
<th>Model</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>TC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Correlations</td>
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<td>0.922</td>
<td>0.859</td>
<td>0.930</td>
<td>0.921</td>
<td>0.930</td>
<td>0.929</td>
<td>0.928</td>
</tr>
<tr>
<td>Standard Deviation of Observation</td>
<td></td>
<td>54.960</td>
<td>54.960</td>
<td>54.960</td>
<td>54.960</td>
<td>54.960</td>
<td>54.960</td>
<td>54.960</td>
</tr>
<tr>
<td>Mean Error</td>
<td></td>
<td>7.927</td>
<td>-0.828</td>
<td>8.204</td>
<td>8.334</td>
<td>2.713</td>
<td>9.029</td>
<td>9.991</td>
</tr>
<tr>
<td>Mean of Observations</td>
<td></td>
<td>38.983</td>
<td>38.983</td>
<td>38.983</td>
<td>38.983</td>
<td>38.983</td>
<td>38.983</td>
<td>38.983</td>
</tr>
</tbody>
</table>
3.3.3.2. Predictions Using TRMM Single Pixel Data

Figure 3.16 shows the validation time series of the predictions and performance statistics of validation time series are provided in Table 3.18. Overall correlations and RMSE values show a consistent pattern; the methods with higher correlation values have lower RMSE value. Among all the complete data set predictions, Climatology-Based predictions provided the best result for the streamflow data while Persistence-Based predictions of the streamflow have approximately 0.90 correlations with the validation data.

![Figure 3.16 Station E23A016 DSI streamflow data v.s. TRMM single pixel precipitation data complete data set predictions](image-url)
Table 3.18 Performance statistics of station E23A016 with TRMM single pixel data - complete data set predictions

<table>
<thead>
<tr>
<th>Model</th>
<th>Climatology</th>
<th>Persistence</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Correlations</td>
<td>0.927</td>
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<td>0.125</td>
<td>0.138</td>
<td>0.157</td>
<td>0.040</td>
</tr>
<tr>
<td>Standard Deviation of Observation</td>
<td>50.746</td>
<td>50.746</td>
<td>50.746</td>
<td>50.746</td>
<td>50.746</td>
<td>50.746</td>
</tr>
<tr>
<td>Standard Deviation of Errors</td>
<td>20.073</td>
<td>24.869</td>
<td>49.565</td>
<td>50.266</td>
<td>51.582</td>
<td>51.231</td>
</tr>
<tr>
<td>Mean Error</td>
<td>5.679</td>
<td>-1.803</td>
<td>27.350</td>
<td>27.035</td>
<td>2.337</td>
<td>24.915</td>
</tr>
<tr>
<td>RMSE</td>
<td>20.591</td>
<td>24.588</td>
<td>56.004</td>
<td>56.457</td>
<td>50.914</td>
<td>56.325</td>
</tr>
<tr>
<td>Mean of Observations</td>
<td>38.983</td>
<td>38.983</td>
<td>38.983</td>
<td>38.983</td>
<td>38.983</td>
<td>38.983</td>
</tr>
</tbody>
</table>

Similar results are obtained from the SLR, MLR, MLP and Copula models but showing under 0.20 correlation. These models could not identify a skillful relationship between the Rainfall and Runoff mainly due to lack of data. 9 years of monthly streamflow data and precipitation data could not train the models.

Figure 3.17 Station E23A016 DSI streamflow data v.s. TRMM single pixel precipitation data anomaly component data set predictions
Additional predictions are made using the standardized anomaly components of data sets. Figure 3.17 shows the validation time series of the anomaly component predictions.

Addition of Climatology component to the standardized anomaly component predictions showed above 0.90 correlations, these improved predictions are showing heavy majority of the predictive skill and the relation between the precipitation and the streamflow data sets are due to the strong seasonality.

Correlations of predictions which are obtained from the SLR, MLR, MLP and Copula models increased from 0.20 to above 0.90 with decreasing RMSE values and mean error term. Performance statistics of validation time series are provided in Table 3.19.

Table 3.19 Performance statistics of station E23A016 with TRMM single pixel data – anomaly component data set predictions

<table>
<thead>
<tr>
<th>Performance Statistics</th>
<th>Model</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Correlations</td>
<td>0.927</td>
<td>0.892</td>
<td>0.929</td>
<td>0.925</td>
<td>0.945</td>
<td>0.928</td>
<td>0.930</td>
<td></td>
</tr>
<tr>
<td>Standard Deviation of Observation</td>
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<td>50.746</td>
<td>50.746</td>
<td>50.746</td>
<td>50.746</td>
<td>50.746</td>
<td></td>
</tr>
<tr>
<td>Mean of Observations</td>
<td>38.983</td>
<td>38.983</td>
<td>38.983</td>
<td>38.983</td>
<td>38.983</td>
<td>38.983</td>
<td>38.983</td>
<td></td>
</tr>
</tbody>
</table>
3.3.3.3. Predictions Using TRMM Catchment Average Data

Figure 3.18 shows the validation time series of the predictions and performance statistics of validation time series are provided in Table 3.20. Overall correlations and RMSE values show a consistent pattern; the methods with higher correlation values have lower RMSE value. Among all the complete data set predictions, Climatology-Based predictions provided the best result for the streamflow data while Persistence-Based predictions of the streamflow have approximately 0.90 correlations with the validation data.

![Figure 3.18 Station E23A016 DSI streamflow data v.s. TRMM catchment average precipitation data complete data set predictions](image)

Figure 3.18 Station E23A016 DSI streamflow data v.s. TRMM catchment average precipitation data complete data set predictions
Table 3.20 Performance statistics of station E23A016 with TRMM catchment average data - complete data set predictions

<table>
<thead>
<tr>
<th>Model</th>
<th>Performance Statistics</th>
<th>SLR</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Correlations</td>
<td>0.927</td>
<td>0.890</td>
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<td>0.215</td>
<td>0.084</td>
<td>0.063</td>
</tr>
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<td>Standard Deviation of Observation</td>
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<td>50.746</td>
<td>50.746</td>
<td>50.746</td>
<td>50.746</td>
<td>50.746</td>
</tr>
<tr>
<td>Standard Deviation of Errors</td>
<td>20.073</td>
<td>24.869</td>
<td>50.144</td>
<td>49.969</td>
<td>52.148</td>
<td>50.712</td>
</tr>
<tr>
<td>Mean Error</td>
<td>5.679</td>
<td>-1.803</td>
<td>28.245</td>
<td>28.382</td>
<td>2.765</td>
<td>26.771</td>
</tr>
<tr>
<td>RMSE</td>
<td>20.393</td>
<td>24.588</td>
<td>56.941</td>
<td>56.809</td>
<td>51.493</td>
<td>56.718</td>
</tr>
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<td>38.983</td>
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<td>38.983</td>
<td>38.983</td>
</tr>
</tbody>
</table>

Similar results are obtained from the SLR, MLR, MLP and Copula models but showing under 0.20 correlation. These models could not identify a skillful relationship between the Rainfall and Runoff mainly due to lack of data. 9 years of monthly streamflow data and precipitation data could not train the models.

Additional predictions are made using the standardized anomaly components of data sets. Figure 3.19 shows the validation time series of the anomaly component predictions.

Figure 3.19 Station E23A016 DSI streamflow data v.s. TRMM catchment average precipitation data anomaly component data set predictions
Addition of Climatology component to the standardized anomaly component predictions showed above 0.90 correlations, these improved predictions are showing heavy majority of the predictive skill and the relation between the precipitation and the streamflow data sets are due to the strong seasonality.

Correlations of predictions which are obtained from the SLR, MLR, MLP and Copula models increased from 0.20 to above 0.90 with decreasing RMSE values and mean error term. Performance statistics of validation time series are provided in Table 3.21.

Table 3.21 Performance statistics of station E23A016 with catchment average data – anomaly component data set predictions

<table>
<thead>
<tr>
<th>Performance Statistics</th>
<th>Model</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Correlations</td>
<td></td>
<td>0.927</td>
<td>0.892</td>
<td>0.921</td>
<td>0.927</td>
<td>0.922</td>
<td>0.922</td>
<td>0.928</td>
</tr>
<tr>
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<td>50.746</td>
<td>50.746</td>
<td>50.746</td>
<td>50.746</td>
<td>50.746</td>
<td>50.746</td>
</tr>
<tr>
<td>Mean Error</td>
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<td>-1.803</td>
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<td>12.271</td>
<td>4.767</td>
<td>11.787</td>
<td>11.840</td>
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<tr>
<td>Mean of Observations</td>
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<td>38.983</td>
<td>38.983</td>
<td>38.983</td>
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<td>38.983</td>
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<td>38.983</td>
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</tbody>
</table>

87
3.3.4. Station E23A020

3.3.4.1. Predictions Using Meteorology Data

Figure 3.20 shows the validation time series of the predictions and performance statistics of validation time series are provided in Table 3.22. Overall correlations and RMSE values show a consistent pattern; the methods with higher correlation values have lower RMSE value. Among all the complete data set predictions, Climatology-Based predictions provided the best result for the streamflow data while Persistence-Based predictions of the streamflow have approximately 0.90 correlations with the validation data.

Figure 3.20 Station E23A020 DSI streamflow data v.s. meteorology precipitation data complete data set predictions
Table 3.22 Performance statistics of station E23A020 with meteorology data - complete data set predictions

<table>
<thead>
<tr>
<th>Performance Statistics</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Correlations</td>
<td>0.931</td>
<td>0.882</td>
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<td>0.604</td>
<td>0.604</td>
<td>0.586</td>
<td>0.578</td>
</tr>
<tr>
<td>Standard Deviation of Observation</td>
<td>38.335</td>
<td>38.335</td>
<td>38.335</td>
<td>38.335</td>
<td>38.335</td>
<td>38.335</td>
<td></td>
</tr>
<tr>
<td>Mean Error</td>
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<td>-1.217</td>
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<td>1.994</td>
<td>2.114</td>
<td>13.478</td>
<td>14.694</td>
</tr>
<tr>
<td>RMSE</td>
<td>15.557</td>
<td>19.794</td>
<td>30.933</td>
<td>30.740</td>
<td>30.899</td>
<td>35.501</td>
<td>37.067</td>
</tr>
</tbody>
</table>

Similar results are obtained from the SLR, MLR and MLP models but showing 0.60 correlation. Copula functions couldn’t identify a skillful relationship for complete data sets. To further investigate the source of the predictive skills of these methods, additional predictions are made using the standardized anomaly components of data sets. Figure 3.21 shows the validation time series of the anomaly component predictions.

Figure 3.21 Station E23A020 DSI streamflow data v.s. meteorology precipitation data anomaly component data set predictions
Addition of Climatology component to the standardized anomaly component predictions showed above 0.90 correlations, these improved predictions are showing heavy majority of the predictive skill and the relation between the precipitation and the streamflow data sets are due to the strong seasonality.

Correlations of predictions which are obtained from the SLR, MLR, MLP and Copula models increased from 0.60 to above 0.90 with decreasing RMSE values and mean error term. Performance statistics of validation time series are provided in Table 3.23.

Table 3.23 Performance statistics of station E23A020 with meteorology data – anomaly component data set predictions

<table>
<thead>
<tr>
<th>Model</th>
<th>Performance Statistics</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Climatology</td>
</tr>
<tr>
<td>Correlations</td>
<td>0.931</td>
</tr>
<tr>
<td>Standard Deviation of Observation</td>
<td>38.335</td>
</tr>
<tr>
<td>Standard Deviation of Errors</td>
<td>14,913</td>
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<tr>
<td>Mean Error</td>
<td>4.685</td>
</tr>
<tr>
<td>RMSE</td>
<td>15,557</td>
</tr>
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</table>
3.3.4.2. Predictions Using TRMM Single Pixel Data

Figure 3.22 shows the validation time series of the predictions and performance statistics of validation time series are provided in Table 3.24. Overall correlations and RMSE values show a consistent pattern; the methods with higher correlation values have lower RMSE value. Among all the complete data set predictions, Climatology-Based predictions provided the best result for the streamflow data while Persistence-Based predictions of the streamflow have approximately 0.90 correlations with the validation data.

![Figure 3.22 Station E23A020 DSI streamflow data v.s. TRMM single pixel precipitation data complete data set predictions](image_url)
Table 3.24 Performance statistics of station E23A020 with TRMM single pixel data - complete data set predictions

<table>
<thead>
<tr>
<th>Performance Statistics</th>
<th>Model</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Correlations</td>
<td>0.951</td>
<td>0.923</td>
<td>0.214</td>
<td>0.258</td>
<td>0.131</td>
<td>0.106</td>
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</tr>
<tr>
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<td>33.128</td>
<td>33.128</td>
<td>33.128</td>
<td>33.128</td>
<td>33.128</td>
<td>33.128</td>
<td></td>
</tr>
<tr>
<td>Standard Deviation of Errors</td>
<td>10.289</td>
<td>15.124</td>
<td>32.379</td>
<td>32.007</td>
<td>33.667</td>
<td>32.944</td>
<td>32.852</td>
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</tr>
<tr>
<td>Mean Error</td>
<td>1.822</td>
<td>-2.379</td>
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<td>1.236</td>
<td>1.744</td>
<td>17.486</td>
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</tr>
</tbody>
</table>

Similar results are obtained from the SLR, MLR, MLP and Copula models but showing under 0.30 correlation. These models could not identify a skillful relationship between the Rainfall and Runoff mainly due to lack of data. 9 years of monthly streamflow data and precipitation data could not train the models.

Figure 3.23 Station E23A020 DSI streamflow data v.s. TRMM single pixel precipitation data anomaly component data set predictions

92
Additional predictions are made using the standardized anomaly components of data sets. Figure 3.23 shows the validation time series of the anomaly component predictions.

Addition of Climatology component to the standardized anomaly component predictions showed above 0.90 correlations, these improved predictions are showing heavy majority of the predictive skill and the relation between the precipitation and the streamflow data sets are due to the strong seasonality.

Correlations of predictions which are obtained from the SLR, MLR, MLP and Copula models increased from 0.30 to above 0.90 with decreasing RMSE values and mean error term. Performance statistics of validation time series are provided in Table 3.25.

Table 3.25 Performance statistics of station E23A020 with TRMM single pixel data – anomaly component data set predictions

<table>
<thead>
<tr>
<th>Performance Statistics</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Correlations</td>
<td>0.951</td>
<td>0.922</td>
<td>0.957</td>
<td>0.957</td>
<td>0.948</td>
<td>0.946</td>
</tr>
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<td>Standard Deviation of Observation</td>
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<td>33.128</td>
<td>33.128</td>
<td>33.128</td>
<td>33.128</td>
<td>33.128</td>
</tr>
<tr>
<td>Standard Deviation of Errors</td>
<td>10,289</td>
<td>15,124</td>
<td>9,593</td>
<td>9,673</td>
<td>10,566</td>
<td>12,485</td>
</tr>
<tr>
<td>Mean Error</td>
<td>1.822</td>
<td>-2.379</td>
<td>2.061</td>
<td>2.015</td>
<td>1.383</td>
<td>7.764</td>
</tr>
<tr>
<td>RMSE</td>
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<td>15,101</td>
<td>9,748</td>
<td>9,748</td>
<td>10,509</td>
<td>14,554</td>
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<tr>
<td>Mean of Observations</td>
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<td>29,387</td>
<td>29,387</td>
<td>29,387</td>
<td>29,387</td>
<td>29,387</td>
</tr>
</tbody>
</table>
3.3.4.3. Predictions Using TRMM Catchment Average Data

Figure 3.24 shows the validation time series of the predictions and performance statistics of validation time series are provided in Table 3.26. Overall correlations and RMSE values show a consistent pattern; the methods with higher correlation values have lower RMSE value. Among all the complete data set predictions, Climatology-Based predictions provided the best result for the streamflow data while Persistence-Based predictions of the streamflow have approximately 0.90 correlations with the validation data.

![Figure 3.24 Station E23A020 DSI streamflow data v.s. TRMM catchment average precipitation data complete data set predictions](image)

Figure 3.24 Station E23A020 DSI streamflow data v.s. TRMM catchment average precipitation data complete data set predictions
Similar results are obtained from the SLR, MLR, MLP and Copula models but showing under 0.20 correlation. These models could not identify a skillful relationship between the Rainfall and Runoff mainly due to lack of data. 9 years of monthly streamflow data and precipitation data could not train the models.

Additional predictions are made using the standardized anomaly components of data sets. Figure 3.25 shows the validation time series of the anomaly component predictions.

![Figure 3.25 Station E23A020 DSI streamflow data v.s. TRMM catchment average precipitation data anomaly component data set predictions](image-url)

**Table 3.26 Performance statistics of station E23A020 with TRMM catchment average data - complete data set predictions**

<table>
<thead>
<tr>
<th>Model</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Correlations</td>
<td>0.951</td>
<td>0.928</td>
<td>0.167</td>
<td>0.227</td>
<td>0.038</td>
<td>0.044</td>
<td>0.046</td>
</tr>
<tr>
<td>Standard Deviation of Observation</td>
<td>33,128</td>
<td>33,128</td>
<td>33,128</td>
<td>33,128</td>
<td>33,128</td>
<td>33,128</td>
<td>33,128</td>
</tr>
<tr>
<td>Standard Deviation of Errors</td>
<td>10,289</td>
<td>15,101</td>
<td>32,489</td>
<td>32,055</td>
<td>34,254</td>
<td>37,224</td>
<td>37,383</td>
</tr>
<tr>
<td>Mean Error</td>
<td>1,822</td>
<td>-2.379</td>
<td>1.314</td>
<td>1.890</td>
<td>0.315</td>
<td>17.719</td>
<td>18.187</td>
</tr>
<tr>
<td>RMSE</td>
<td>10,307</td>
<td>15,101</td>
<td>32,489</td>
<td>32,055</td>
<td>34,254</td>
<td>37,224</td>
<td>37,383</td>
</tr>
<tr>
<td>Mean of Observations</td>
<td>29,387</td>
<td>29,387</td>
<td>29,387</td>
<td>29,387</td>
<td>29,387</td>
<td>29,387</td>
<td>29,387</td>
</tr>
</tbody>
</table>
Addition of Climatology component to the standardized anomaly component predictions showed above 0.90 correlations, these improved predictions are showing heavy majority of the predictive skill and the relation between the precipitation and the streamflow data sets are due to the strong seasonality.

Correlations of predictions which are obtained from the SLR, MLR, MLP and Copula models increased from 0.20 to above 0.90 with decreasing RMSE values and mean error term. Performance statistics of validation time series are provided in Table 3.27.

Table 3.27 Performance statistics of station E23A020 with catchment average data – anomaly component data set predictions

<table>
<thead>
<tr>
<th>Performance Statistics</th>
<th>Model</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Correlations</td>
<td>0.951</td>
<td>0.923</td>
<td>0.950</td>
<td>0.953</td>
<td>0.942</td>
<td>0.952</td>
<td>0.951</td>
<td></td>
</tr>
<tr>
<td>Standard Deviation of Observation</td>
<td>33.128</td>
<td>33.128</td>
<td>33.128</td>
<td>33.128</td>
<td>33.128</td>
<td>33.128</td>
<td>33.128</td>
<td></td>
</tr>
<tr>
<td>Standard Deviation of Errors</td>
<td>10,289</td>
<td>15,124</td>
<td>9,956</td>
<td>10,110</td>
<td>11,253</td>
<td>12,140</td>
<td>12,254</td>
<td></td>
</tr>
<tr>
<td>Mean Error</td>
<td>1,822</td>
<td>-2.379</td>
<td>2,146</td>
<td>1,976</td>
<td>0.774</td>
<td>7,886</td>
<td>8,012</td>
<td></td>
</tr>
<tr>
<td>RMSE</td>
<td>10,307</td>
<td>15,104</td>
<td>10,048</td>
<td>10,163</td>
<td>11,123</td>
<td>14,335</td>
<td>14,498</td>
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</tr>
<tr>
<td>Mean of Observations</td>
<td>29,387</td>
<td>29,387</td>
<td>29,387</td>
<td>29,387</td>
<td>29,387</td>
<td>29,387</td>
<td>29,387</td>
<td></td>
</tr>
</tbody>
</table>

96
3.3.5. Station E23A021

3.3.5.1. Predictions Using Meteorology Data

Figure 3.26 shows the validation time series of the predictions and performance statistics of validation time series are provided in Table 3.28. Overall correlations and RMSE values show a consistent pattern; the methods with higher correlation values have lower RMSE value. Among all the complete data set predictions, Climatology-Based predictions provided the best result for the streamflow data while Persistence-Based predictions of the streamflow have approximately 0.90 correlations with the validation data.

![Station E23A021 DSI streamflow data v.s. meteorology precipitation data complete data set predictions](image)

Figure 3.26 Station E23A021 DSI streamflow data v.s. meteorology precipitation data complete data set predictions
Table 3.28 Performance statistics of station E23A021 with meteorology data - complete data set predictions

<table>
<thead>
<tr>
<th>Model</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Corelations</td>
<td>0.940</td>
<td>0.885</td>
<td>0.572</td>
<td>0.566</td>
<td>0.573</td>
<td>0.613</td>
<td>0.608</td>
</tr>
<tr>
<td>Mean Error</td>
<td>1.429</td>
<td>-0.189</td>
<td>-0.356</td>
<td>-0.526</td>
<td>-0.438</td>
<td>7.586</td>
<td>7.569</td>
</tr>
<tr>
<td>RMSE</td>
<td>5.073</td>
<td>6.817</td>
<td>11.668</td>
<td>11.785</td>
<td>11.619</td>
<td>15.651</td>
<td>15.610</td>
</tr>
</tbody>
</table>

Similar results are obtained from the SLR, MLR and MLP models but showing 0.60 correlation. Copula models couldn’t identify a skillful relationship for complete data sets. To further investigate the source of the predictive skills of these methods, additional predictions are made using the standardized anomaly components of data sets. Figure 3.27 shows the validation time series of the anomaly component predictions.

Figure 3.27 Station E23A021 DSI streamflow data v.s. meteorology precipitation data anomaly component data set predictions
Addition of Climatology component to the standardized anomaly component predictions showed above 0.90 correlations, these improved predictions are showing heavy majority of the predictive skill and the relation between the precipitation and the streamflow data sets are due to the strong seasonality.

Correlations of predictions which are obtained from the SLR, MLR, MLP and Copula models increased from 0.50 to above 0.90 with decreasing RMSE values and mean error term. Performance statistics of validation time series are provided in Table 3.29.

Table 3.29 Performance statistics of station E23A021 with meteorology data – anomaly component data set predictions

<table>
<thead>
<tr>
<th>Model</th>
<th>Performance Statistics</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Climatology</td>
</tr>
<tr>
<td>Correlations</td>
<td>0.940</td>
</tr>
<tr>
<td>Standard Deviation of Errors</td>
<td>4,881</td>
</tr>
<tr>
<td>Mean Error</td>
<td>1,429</td>
</tr>
<tr>
<td>RMSE</td>
<td>5,073</td>
</tr>
<tr>
<td>Mean of Observations</td>
<td>14,058</td>
</tr>
</tbody>
</table>
3.3.5.2. Predictions Using TRMM Single Pixel Data

Figure 3.28 shows the validation time series of the predictions and performance statistics of validation time series are provided in Table 3.30. Overall correlations and RMSE values show a consistent pattern; the methods with higher correlation values have lower RMSE value. Among all the complete data set predictions, Climatology-Based predictions provided the best result for the streamflow data while Persistence-Based predictions of the streamflow have approximately 0.90 correlations with the validation data.

![Figure 3.28 Station E23A021 DSI streamflow data v.s. TRMM single pixel precipitation data complete data set predictions](image)

Figure 3.28 Station E23A021 DSI streamflow data v.s. TRMM single pixel precipitation data complete data set predictions
Similar results are obtained from the SLR, MLR, MLP and Copula models but showing under 0.30 correlation. These models could not identify a skillful relationship between the Rainfall and Runoff mainly due to lack of data. 9 years of monthly streamflow data and precipitation data could not train the models.

Additional predictions are made using the standardized anomaly components of data sets. Figure 3.29 shows the validation time series of the anomaly component predictions.
Addition of Climatology component to the standardized anomaly component predictions showed above 0.90 correlations, these improved predictions are showing heavy majority of the predictive skill and the relation between the precipitation and the streamflow data sets are due to the strong seasonality.

Correlations of predictions which are obtained from the SLR, MLR, MLP and Copula models increased from 0.20 to above 0.90 with decreasing RMSE values and mean error term. Performance statistics of validation time series are provided in Table 3.31.

Table 3.31 Performance statistics of station E23A021 with TRMM single pixel data – anomaly component data set predictions

<table>
<thead>
<tr>
<th>Performance Statistics</th>
<th>Model</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Correlations</td>
<td></td>
<td>0.961</td>
<td>0.938</td>
<td>0.964</td>
<td>0.963</td>
<td>0.964</td>
<td>0.963</td>
<td>0.964</td>
</tr>
<tr>
<td>Standard Deviation of Observation</td>
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<td>13,879</td>
<td>13,879</td>
<td>13,879</td>
<td>13,879</td>
<td>13,879</td>
<td>13,879</td>
<td></td>
</tr>
<tr>
<td>Standard Deviation of Errors</td>
<td>3,920</td>
<td>4,858</td>
<td>3,701</td>
<td>3,847</td>
<td>3,699</td>
<td>4,283</td>
<td>4,239</td>
<td></td>
</tr>
<tr>
<td>Mean Error</td>
<td>0.979</td>
<td>-0.255</td>
<td>0.009</td>
<td>-0.108</td>
<td>0.625</td>
<td>2.823</td>
<td>2.968</td>
<td></td>
</tr>
<tr>
<td>RMSE</td>
<td>3.987</td>
<td>4.796</td>
<td>3.650</td>
<td>3.795</td>
<td>3.700</td>
<td>5.080</td>
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<td>Mean of Observations</td>
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<td>14,058</td>
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<td>14,058</td>
<td>14,058</td>
<td>14,058</td>
<td></td>
</tr>
</tbody>
</table>
3.3.5.3. Predictions Using TRMM Catchment Average Data

Figure 3.30 shows the validation time series of the predictions and performance statistics of validation time series are provided in Table 3.32. Overall correlations and RMSE values show a consistent pattern; the methods with higher correlation values have lower RMSE value. Among all the complete data set predictions, Climatology-Based predictions provided the best result for the streamflow data while Persistence-Based predictions of the streamflow have approximately 0.90 correlations with the validation data.

Figure 3.30 Station E23A021 DSI streamflow data v.s. TRMM catchment average precipitation data complete data set predictions
Table 3.32 Performance statistics of station E23A021 with TRMM catchment average data - complete data set predictions

<table>
<thead>
<tr>
<th>Model</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Correlations</td>
<td>0.961</td>
<td>0.938</td>
<td>0.033</td>
<td>0.148</td>
<td>0.118</td>
<td>0.172</td>
<td>0.172</td>
</tr>
<tr>
<td>Standard Deviation of Observation</td>
<td>13,879</td>
<td>13,879</td>
<td>13,879</td>
<td>13,879</td>
<td>13,879</td>
<td>13,879</td>
<td>13,879</td>
</tr>
<tr>
<td>Standard Deviation of Errors</td>
<td>3,520</td>
<td>4,858</td>
<td>13,902</td>
<td>13,730</td>
<td>13,879</td>
<td>13,700</td>
<td>13,700</td>
</tr>
<tr>
<td>Mean Error</td>
<td>0.978</td>
<td>-0.255</td>
<td>0.255</td>
<td>0.325</td>
<td>2.943</td>
<td>0.532</td>
<td>0.532</td>
</tr>
<tr>
<td>RMSE</td>
<td>3,987</td>
<td>4,797</td>
<td>13,710</td>
<td>13,541</td>
<td>13,998</td>
<td>13,519</td>
<td>13,519</td>
</tr>
<tr>
<td>Mean of Observations</td>
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<td>14,058</td>
<td>14,058</td>
<td>14,058</td>
<td>14,058</td>
<td>14,058</td>
<td>14,058</td>
</tr>
</tbody>
</table>

Similar results are obtained from the SLR, MLR, MLP and Copula models but showing under 0.20 correlation. These models could not identify a skillful relationship between the Rainfall and Runoff mainly due to lack of data. 9 years of monthly streamflow data and precipitation data could not train the models.

Additional predictions are made using the standardized anomaly components of data sets. Figure 3.31 shows the validation time series of the anomaly component predictions.

Figure 3.31 Station E23A021 DSI streamflow data v.s. TRMM catchment average precipitation data anomaly component data set predictions
Addition of Climatology component to the standardized anomaly component predictions showed above 0.90 correlations, these improved predictions are showing heavy majority of the predictive skill and the relation between the precipitation and the streamflow data sets are due to the strong seasonality.

Correlations of predictions which are obtained from the SLR, MLR, MLP and Copula models increased from 0.20 to above 0.90 with decreasing RMSE values and mean error term. Performance statistics of validation time series are provided in Table 3.33.

Table 3.33 Performance statistics of station E23A021 with catchment average data – anomaly component data set predictions

<table>
<thead>
<tr>
<th>Model</th>
<th>Performance Statistics</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Climatology</td>
</tr>
<tr>
<td>Correlations</td>
<td>0.961</td>
</tr>
<tr>
<td>Standard Deviation of Errors</td>
<td>3.920</td>
</tr>
<tr>
<td>Mean Error</td>
<td>0.979</td>
</tr>
<tr>
<td>Mean of Observations</td>
<td>14,058</td>
</tr>
</tbody>
</table>
3.3.6. Station E23A023

3.3.6.1. Predictions Using Meteorology Data

Figure 3.32 shows the validation time series of the predictions and performance statistics of validation time series are provided in Table 3.34. Overall correlations and RMSE values show a consistent pattern; the methods with higher correlation values have lower RMSE value. Among all the complete data set predictions, Climatology-Based predictions provided the best result for the streamflow data while Persistence-Based predictions of the streamflow have approximately 0.90 correlations with the validation data.

![Figure 3.32 Station E23A023 DSI streamflow data v.s. meteorology precipitation data complete data set predictions](image)

Figure 3.32 Station E23A023 DSI streamflow data v.s. meteorology precipitation data complete data set predictions
Similar results are obtained from the SLR and MLR models but showing 0.60 correlation. Copula functions couldn’t identify a skillful relationship for complete data sets. MLP model is also provided results that showing 0.60 correlation. To further investigate the source of the predictive skills of these methods, additional predictions are made using the standardized anomaly components of data sets. Figure 3.33 shows the validation time series of the anomaly component predictions.

Table 3.34 Performance statistics of station E23A023 with meteorology data - complete data set predictions

<table>
<thead>
<tr>
<th>Performance Statistics</th>
<th>Model</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Correlations</td>
<td>0.926</td>
<td>0.701</td>
<td>0.604</td>
<td>0.609</td>
<td>0.633</td>
<td>0.551</td>
<td>0.551</td>
<td></td>
</tr>
<tr>
<td>Standard Deviation of Errors</td>
<td>14,819</td>
<td>31,102</td>
<td>29,071</td>
<td>28,971</td>
<td>28,242</td>
<td>35,938</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Mean Error</td>
<td>7,582</td>
<td>3,709</td>
<td>2,812</td>
<td>2,225</td>
<td>1,962</td>
<td>22,071</td>
<td>22,060</td>
<td></td>
</tr>
<tr>
<td>RMSE</td>
<td>16,577</td>
<td>31,102</td>
<td>29,056</td>
<td>28,905</td>
<td>28,164</td>
<td>42,015</td>
<td>41,986</td>
<td></td>
</tr>
<tr>
<td>Mean of Observations</td>
<td>33,506</td>
<td>33,506</td>
<td>33,506</td>
<td>33,506</td>
<td>33,506</td>
<td>33,506</td>
<td>33,506</td>
<td></td>
</tr>
</tbody>
</table>

Figure 3.33 Station E23A023 DSI streamflow data v.s. meteorology precipitation data anomaly component data set predictions
Addition of Climatology component to the standardized anomaly component predictions showed above 0.90 correlations, these improved predictions are showing heavy majority of the predictive skill and the relation between the precipitation and the streamflow data sets are due to the strong seasonality.

Correlations of predictions which are obtained from the SLR, MLR, MLP and Copula models increased from 0.50 to above 0.90 with decreasing RMSE values and mean error term. Performance statistics of validation time series are provided in Table 3.35.

Table 3.35 Performance statistics of station E23A023 with meteorology data – anomaly component data set predictions
3.3.6.2. Predictions Using TRMM Single Pixel Data

Figure 3.34 shows the validation time series of the predictions and performance statistics of validation time series are provided in Table 3.36. Overall correlations and RMSE values show a consistent pattern; the methods with higher correlation values have lower RMSE value. Among all the complete data set predictions, Climatology-Based predictions provided the best result for the streamflow data while Persistence-Based predictions of the streamflow have approximately 0.90 correlations with the validation data.

Figure 3.34 Station E23A023 DSI streamflow data v.s. TRMM single pixel precipitation data complete data set predictions

109
Table 3.36 Performance statistics of station E23A023 with TRMM single pixel data - complete data set predictions

<table>
<thead>
<tr>
<th>Model</th>
<th>Performance Statistics</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Climatology</td>
</tr>
<tr>
<td>Correlations</td>
<td>0.940</td>
</tr>
<tr>
<td>Standard Deviation of Errors</td>
<td>12,954</td>
</tr>
<tr>
<td>Mean Error</td>
<td>8,487</td>
</tr>
<tr>
<td>RMSE</td>
<td>15,335</td>
</tr>
<tr>
<td>Mean of Observations</td>
<td>33,506</td>
</tr>
</tbody>
</table>

Similar results are obtained from the SLR, MLR, MLP and Copula models but showing under 0.20 correlation. These models could not identify a skillful relationship between the Rainfall and Runoff mainly due to lack of data and showed artificial skills in predictions. 9 years of monthly streamflow data and precipitation data could not train the models.

Figure 3.35 Station E23A023 DSI streamflow data v.s. TRMM single pixel precipitation data anomaly component data set predictions
Additional predictions are made using the standardized anomaly components of data sets. Figure 3.35 shows the validation time series of the anomaly component predictions.

Addition of Climatology component to the standardized anomaly component predictions showed above 0.90 correlations, these improved predictions are showing heavy majority of the predictive skill and the relation between the precipitation and the streamflow data sets are due to the strong seasonality.

Correlations of predictions which are obtained from the SLR, MLR, MLP and Copula models increased from 0.20 to above 0.90 with decreasing RMSE values and mean error term. Performance statistics of validation time series are provided in Table 3.37.

Table 3.37 Performance statistics of station E23A023 with TRMM single pixel data – anomaly component data set predictions

<table>
<thead>
<tr>
<th>Performance Statistics</th>
<th>Model</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Correlations</td>
<td>0.940</td>
<td>0.865</td>
<td>0.926</td>
<td>0.925</td>
<td>0.925</td>
<td>0.925</td>
<td>0.934</td>
</tr>
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<td>Standard Deviation of Errors</td>
<td>12,955</td>
<td>20,468</td>
<td>15,807</td>
<td>15,852</td>
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<td>15,405</td>
<td>16,640</td>
</tr>
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<td>-0,660</td>
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<td>8,781</td>
<td>12,714</td>
<td>14,898</td>
</tr>
<tr>
<td>RMSE</td>
<td>15,336</td>
<td>20,192</td>
<td>19,594</td>
<td>19,619</td>
<td>15,917</td>
<td>19,808</td>
<td>22,162</td>
</tr>
<tr>
<td>Mean of Observations</td>
<td>33,506</td>
<td>33,506</td>
<td>33,506</td>
<td>33,506</td>
<td>33,506</td>
<td>33,506</td>
<td>33,506</td>
</tr>
</tbody>
</table>
3.3.6.3. Predictions Using TRMM Catchment Average Data

Figure 3.36 shows the validation time series of the predictions and performance statistics of validation time series are provided in Table 3.38. Overall correlations and RMSE values show a consistent pattern; the methods with higher correlation values have lower RMSE value. Among all the complete data set predictions, Climatology-Based predictions provided the best result for the streamflow data while Persistence-Based predictions of the streamflow have approximately 0.90 correlations with the validation data.

Figure 3.36 Station E23A023 DSI streamflow data v.s. TRMM catchment average precipitation data complete data set predictions
Similar results are obtained from the SLR, MLR, MLP and Copula models but showing under 0.40 correlation. These models could not identify a skillful relationship between the Rainfall and Runoff mainly due to lack of data. 9 years of monthly streamflow data and precipitation data could not train the models.

Additional predictions are made using the standardized anomaly components of data sets. Figure 3.37 shows the validation time series of the anomaly component predictions.

Figure 3.37 Station E23A023 DSI streamflow data v.s. TRMM catchment average precipitation data anomaly component data set predictions
Addition of Climatology component to the standardized anomaly component predictions showed above 0.90 correlations, these improved predictions are showing heavy majority of the predictive skill and the relation between the precipitation and the streamflow data sets are due to the strong seasonality.

Correlations of predictions which are obtained from the SLR, MLR, MLP and Copula models increased from 0.30 to above 0.90 with decreasing RMSE values and mean error term. Performance statistics of validation time series are provided in Table 3.39.

Table 3.39 Performance statistics of station E23A023 with catchment average data – anomaly component data set predictions

<table>
<thead>
<tr>
<th>Model</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Correlations</td>
<td>0.940</td>
<td>0.863</td>
<td>0.906</td>
<td>0.923</td>
<td>0.926</td>
<td>0.938</td>
<td>0.935</td>
</tr>
<tr>
<td>Standard Deviation of Observation</td>
<td>35.399</td>
<td>35.399</td>
<td>35.399</td>
<td>35.399</td>
<td>35.399</td>
<td>35.399</td>
<td>35.399</td>
</tr>
<tr>
<td>Standard Deviation of Errors</td>
<td>12,955</td>
<td>20,468</td>
<td>16,448</td>
<td>15,594</td>
<td>14,298</td>
<td>14,594</td>
<td>14,632</td>
</tr>
<tr>
<td>Mean Error</td>
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<td>-0.660</td>
<td>10,658</td>
<td>10,907</td>
<td>8,739</td>
<td>12,176</td>
<td>11,907</td>
</tr>
<tr>
<td>RMSE</td>
<td>15,336</td>
<td>20,192</td>
<td>19,407</td>
<td>18,851</td>
<td>16,587</td>
<td>18,849</td>
<td>18,705</td>
</tr>
<tr>
<td>Mean of Observations</td>
<td>33,506</td>
<td>33,506</td>
<td>33,506</td>
<td>33,506</td>
<td>33,506</td>
<td>33,506</td>
<td>33,506</td>
</tr>
</tbody>
</table>
3.4. Discussion of Predictions

The summary of the correlations of complete data set predictions and anomaly component predictions with the streamflow validation time series are shown in Table 3.40 and Table 3.41.

Table 3.40 Summary of the correlations of complete data set predictions with the streamflow validation time series

<table>
<thead>
<tr>
<th>Station</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>E23A004</td>
<td>0.919</td>
<td>0.919</td>
<td>0.531</td>
<td>0.531</td>
<td>0.545</td>
<td>0.453</td>
<td>0.551</td>
</tr>
<tr>
<td>E23A005</td>
<td>0.931</td>
<td>0.884</td>
<td>0.604</td>
<td>0.605</td>
<td>0.437</td>
<td>0.432</td>
<td>0.427</td>
</tr>
<tr>
<td>E23A016</td>
<td>0.922</td>
<td>0.859</td>
<td>0.253</td>
<td>0.253</td>
<td>0.458</td>
<td>0.431</td>
<td>0.441</td>
</tr>
<tr>
<td>E23A020</td>
<td>0.931</td>
<td>0.882</td>
<td>0.600</td>
<td>0.604</td>
<td>0.404</td>
<td>0.586</td>
<td>0.578</td>
</tr>
<tr>
<td>E23A021</td>
<td>0.940</td>
<td>0.885</td>
<td>0.572</td>
<td>0.566</td>
<td>0.573</td>
<td>0.613</td>
<td>0.608</td>
</tr>
</tbody>
</table>

Table 3.41 Summary of the correlations of anomaly component data set predictions with the streamflow validation time series

<table>
<thead>
<tr>
<th>Station</th>
<th>Climatology</th>
<th>Persistence</th>
<th>SLR</th>
<th>MLR</th>
<th>MLP</th>
<th>NC</th>
<th>FC</th>
</tr>
</thead>
<tbody>
<tr>
<td>E23A004</td>
<td>0.919</td>
<td>0.919</td>
<td>0.918</td>
<td>0.916</td>
<td>0.913</td>
<td>0.917</td>
<td>0.920</td>
</tr>
<tr>
<td>E23A005</td>
<td>0.931</td>
<td>0.884</td>
<td>0.928</td>
<td>0.924</td>
<td>0.938</td>
<td>0.939</td>
<td>0.941</td>
</tr>
<tr>
<td>E23A016</td>
<td>0.922</td>
<td>0.859</td>
<td>0.918</td>
<td>0.921</td>
<td>0.930</td>
<td>0.929</td>
<td>0.925</td>
</tr>
<tr>
<td>E23A020</td>
<td>0.931</td>
<td>0.882</td>
<td>0.935</td>
<td>0.934</td>
<td>0.934</td>
<td>0.931</td>
<td>0.934</td>
</tr>
<tr>
<td>E23A021</td>
<td>0.940</td>
<td>0.885</td>
<td>0.938</td>
<td>0.936</td>
<td>0.930</td>
<td>0.909</td>
<td>0.927</td>
</tr>
<tr>
<td>E23A023</td>
<td>0.925</td>
<td>0.701</td>
<td>0.921</td>
<td>0.918</td>
<td>0.903</td>
<td>0.894</td>
<td>0.918</td>
</tr>
</tbody>
</table>

115
Overall results show that the best predictions are obtained from the climatology-based predictions of the stations for the complete data sets while persistence-based predictions have approximately 0.90 correlations with the observations. However, predictions which are using standardized anomaly component with different models are improved when long-term climatological values added as it is expected. These improved predictions indicate that the relation between the precipitation and the streamflow data sets are due to the strong seasonality. The results that the perfect knowledge of seasonality of the streamflow (i.e., climatology-based predictions) yield much better prediction that the prediction models (regression, ANN, and copula) may be primarily because the prediction models fail to accurately estimate the seasonality component of the streamflow while perfect knowledge of seasonality yield a much better prediction because the variability of the seasonality component of the streamflow data is much higher (~80%, Table 3.3) than the anomaly component (~20%).

Supporting these results, the anomaly predictions are made and then the perfect knowledge of the seasonality is added to yield a quantitative streamflow forecast, the skill (i.e., correlations) of the predictions increase to above 0.90. These results signify the choice of prediction model has secondary importance compared to accurate knowledge of seasonality of the streamflow data; perfect knowledge of the higher variability component of streamflow data (i.e., seasonality) primarily drives the skill of the predictions, while the inter annual deviations from these climatological components (i.e., anomalies) only marginally impact the overall accuracy of the complete time series predictions.

On the other hand, for drought related studies and the secondary energy generation (i.e., additional energy that can be generated in case additional hydropower potential is available in addition to the firm energy that is guaranteed to be supplied 95% of the time) the streamflow data anomalies (i.e., deviations from the long term means) are more important particularly for future energy generation planning studies (i.e., the future decisions about the quantity of water to be used for electricity generation compared to other usages like irrigation or the decision to generate more electricity.
with excess water during high water seasons can be better done by using better anomaly predictions). This shows despite the seasonality component of the streamflow dominates the complete time series related statistics, anomaly component predictions have crucial effect for many applications. For such applications the skill and the choice of the prediction models (e.g., regression, ANN, copula) becomes very critical.

Correlations of real-time observations and predictions are improved from 0.20 to above 0.90 after long-term climatology values added. Added utility of climatology component show that the climatology component generates the main part of predictive skills. The main reason that streamflow climatology contains approximately 80% of total variability. These results showed that the main driver of the streamflow for the Coruh Basin is not the precipitation but snow-melting. Geological composition of the basin causes this condition. Despite, maximum streamflow values occur in May while maximum precipitation occurs in April and October for any given year in Coruh Basin. So, this condition shows that the main driver of streamflow of Coruh Basin is snow melting meaning that the temperature. Temperature data may provide better results than the precipitation data in streamflow predictions over Coruh Basin.

Among all the models that used for the calculations (SLR, MLR, MLP, NC, FC); MLR model provided the best results for the complete data set predictions while copula functions have the worst model performances. SLR and FC model performances are improved when the long-term climatology components added to the anomaly based predictions. Figure 3.38 and Figure 3.39 shows the averaged overall model correlation performances with different precipitation data sets and different components of the data sets.
Considering the complete time series correlations between the TRMM single pixel estimates and station-based datasets are between 0.50 and 0.66 and correlations between the TRMM catchment average estimates and station-based datasets are between 0.57 and 0.76 (Table 3.1), the averaging operator applied in the vicinity of ground station increasing the correlations between the TRMM estimates and the station observations. On the other hand, this performance improvement is reduced with the increase of catchment area size; for larger catchments the TRMM catchment average precipitation estimates are less skillful than the single pixel estimates. These results imply TRMM individual pixel estimates may have random errors that can be reduced via spatial filtering techniques over relatively small catchments.

Model streamflow prediction performances in general vary; however, for TRMM single pixel vs TRMM catchment average precipitation-based prediction results only
marginally improve even though the catchment average TRMM precipitation estimates considerably better represent the station-based precipitation datasets than single pixel TRMM estimates (Table 3.40). This result shows TRMM precipitation errors are not low enough to be skillfully utilized in streamflow predictions over Coruh basin using the prediction methods investigated here. This signifies the local station-based precipitation observations are important in streamflow predictions as they have the ability to catch the local climatic variability.

Stations with smaller drainage area, like E23A021, has improved predictions utilizing the catchment average precipitation than the single pixel precipitation observations. For the predictions using TRMM catchment average precipitation data sets, the prediction skills and the errors are not very sensitive to the drainage area size; the prediction results are only marginally different. But results show that the importance of remote sensing data usage in rainfall-runoff modeling. Despite, local observations provided the best results, anomaly-based predictions which are obtained from the remote sensing data also provided strong results as with the local observations. Having short time series (Total 12 years – 9 years for training) cause some problems to train the models with the TRMM data.

Over certain basins, the monthly streamflow discharge rates are dominated by the seasonality of the snow melt and the ground water contribution: during the early spring months the streamflow discharge rates are heavily impacted by the snow melt contribution while the low discharge rate during summer months as a direct result of the reduced precipitation rates and ground water levels. Considering the total streamflow discharge rates time series signal can be decomposed into seasonality (i.e., low frequency and slowly varying component) and anomaly (i.e., high frequency and frequently varying component) components, the knowledge of the seasonality alone may give valuable predictive information related with the streamflow discharge rate itself. Given there is heavy snow melt and the precipitation seasonality over some basins in Turkey (i.e., the highest and the lowest flows occur during the spring and the summer months respectively, while the difference between the highest and the lowest values is great compared to the overall variability of the time series), the climatology
of the snow melt (primarily driven by temperature) and the precipitation heavily dominates the streamflow discharge rates. Accordingly, the climatology of the streamflow rates alone may serve a skillful streamflow discharge rate predictor for any year given the climatology of the historical data are available. This is why the climatology-based predictions proved to be very skillful compared to predictions made using other methods.
CHAPTER 4

SUMMARY and CONCLUSION

Streamflow data sets are predicted using precipitation data sets utilizing Simple Linear Regression (SLR), Multiple Linear Regression (MLR), Artificial Neural Network Model (MLP) and Copula (Normal Copula and Frank Copula) methods. The predictions are compared with benchmarks obtained using climatology- and persistence-based streamflow predictions, where climatology of the streamflow is heavily dominated by the seasonality of the snow melt (early spring) and the temperature over Coruh basin. To further investigate the source of the predictive skills of these methods, separate predictions are made using the standardized anomaly components of data sets (after climatology components are removed) and complete data sets (non-standardized data sets retaining both anomaly and climatology components). Separate monthly predictions are made utilizing station- (total 42 years observations) and remote sensing TRMM-based (total 12 years estimations) monthly precipitation data sets over six streamflow observation station locations over Coruh Basin in Turkey.

Results show that climatology benchmark-based streamflow predictions for the complete data sets have the highest correlations (>0.90) with the actual observations while persistence-based predictions are only marginally lower than these predictions. In general, MLP and Copula functions could not identify a skillful relationship between rainfall-runoff processes for both predictions using the complete data sets; however, the prediction skills are improved when anomaly predictions are made and the true seasonality (i.e., the component with highest variability) component is added to these anomaly predictions. These poor results using the prediction models are
primarily because of the poor streamflow seasonality component prediction of the predictions models. These results imply the significance of the estimation of true climatology in the streamflow estimates over Coruh river basin where the streamflow time series complete data set variability is heavily dominated by the climatology component rather than anomaly component.

Predictions using the ground station-based precipitation are more skillful than the predictions using the remote sensing-based precipitation data sets using the complete streamflow data sets. These results signify the importance of true precipitation data sets reflecting the local climatology of the study area. When the true seasonality is added to the anomaly-based streamflow predictions, the skills of the predictions become closer to the highest obtained climatology- and persistence-based streamflow predictions.

Climatology is the component with the highest skill (because both precipitation and streamflow data sets have very strong seasonality). So, in the absence of any precipitation or any other data set that can be used as predictor, the use of climatology or the persistence-based predictions may provide skillful-enough estimates.

To make better predictions, if the true long-term seasonality of the streamflow data sets are known, then anomaly based predictions using regression, ANN, and Copula models can be implemented and then the true seasonality information can be added to these anomaly predictions.

Because there are only a few studies investigating Rainfall-Runoff relation on Coruh Basin this study has valuable results for the applications over the basin. Results are valuable for dams that are planning to be built for hydropower energy generation purposes. Knowing the amount of discharges that come in different time intervals to the reservoir area, results of this study can be used for the reservoir operations and energy optimization for the individual dams that located in the upper and middle stream of the basin. Minimization of the amount of the spilled water or maximization of the secondary energy generation particularly during wet seasons are topics of future energy generation plans; hence such studies may benefit from investigations presented
in this study that utilizes streamflow and precipitation information to predict streamflow rates.

In this study only precipitation data sets are used as predictors; as a follow up, future studies could also include temperature data sets as another predictor where temperature also show very strong seasonality and primarily drive the snow melt over Coruh basin.

Averaging the TRMM Pixels in order to obtain TRMM catchment average data may cause some loss of information. Alternatively, another study with ANN and Copula models can be made by not averaging the TRMM pixels but taking every pixel data as a separate input. For example, if there are n pixels that cover the sub-basin of ground streamflow observation station, then there will be n sets of precipitation data sets that can be used as input to predictive models (Meher, 2014).

Regulations of the streamflow over Coruh River Upper and Middle streams began in year of 2012. Another future study can be made in the context of investigation of the regulation effects on streamflow predictions over Coruh Basin, where the climatology-based predictions might still prove skillful.


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