

SETTLEMENT OF PILED RAFTS:  
A CRITICAL REVIEW OF  
THE CASE HISTORIES AND CALCULATION METHODS

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NESLİHAN SAĞLAM

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---

Prof. Dr. Canan ÖZGEN  
Director

I certify that this thesis satisfies all the requirements as a thesis for the degree of Master of Science.

---

Prof. Dr. Erdal ÇOKCA  
Head of Department

This is to certify that we have read this thesis and that in our opinion it is fully adequate, in scope and quality, as a thesis for the degree of Master of Science.

---

Prof. Dr. Ufuk ERGUN  
Supervisor

Examining Committee Members

Prof. Dr. Orhan EROL

---

Prof. Dr. Yıldız WASTI

---

Prof. Dr. Erdal ÇOKCA

---

Prof. Dr. Ufuk ERGUN

---

Dr. Mutlu AKDOĞAN

---

## **ABSTRACT**

# **SETTLEMENT OF PILED RAFTS: A CRITICAL REVIEW OF THE CASE HISTORIES AND CALCULATION METHODS**

Neslihan SAĞLAM

M.S. Thesis, Department of Civil Engineering

Supervisor: Prof. Dr. M. Ufuk ERGUN

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In this study, settlement analysis of pile groups by hand calculation methods were investigated. Settlement ratio, equivalent pier, and equivalent raft methods were studied. Variations in some of the calculation methods were noted, and some suggestions were given.

More than thirty piled raft foundation case histories whose foundation and soil properties known have been found. The settlement of piled foundation in each case was solved by these methods. Results obtained from the calculations following different methods were presented for each case in the form of tables and

graphs. Measured and calculated values were compared by making use of graphs and tables. Effect of type of piles was shown.

It was tried to find out that which method is suitable under different conditions. In conclusion, suggestions for methods and calculation procedures were given.

Keywords: Settlement ratio, equivalent pier, equivalent raft, settlement, pile raft foundation.

## ÖZ

# KAZIKLI RADYE TEMELLERİN OTURMASI: HESAP METODLARININ VE GERÇEK PROBLEMLERİN ELEŞTİREL YAKLAŞIMLA TEKRAR İNCELENMESİ

Neslihan SAĞLAM

Yüksek Lisans Tezi, İnşaat Mühendisliği Bölümü

Tez Yöneticisi: Prof. Dr. M. Ufuk ERGUN

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Bu çalışmada kazık guruplarının oturma analizlerinin elde çözüm metodları incelenmiştir. Oturma oranı, eşdeğer ayak, eşdeğer radye metodları çalışılmıştır. Bazı hesap yöntemlerindeki değişikliklere dikkat çekilmiştir ve önerilerde bulunulmuştur.

Otuzun üzerinde, zemin ve temel özellikleri belirli kazıklı radye temel bulunmuştur. Her bir kazıklı temelin oturması bu metodlarla çözülmüştür. Her bir durum için sonuç tabloları ve grafikler hazırlanmıştır. Farklı yöntemlerle elde edilen neticeler her temel için tablo ve grafikler ile sunulmuştur. Bu tablo ve

grafikler kullanılarak, ölçülen ve hesaplanan değerler karşılaştırılmıştır. Kazık tipinin etkileri de gösterilmiştir.

Farklı durumlar için hangi metodun uygun olduğu bulunmaya çalışılmıştır. Sonuç olarak değişik tipteki hesap yöntemleri hakkında önerilerde bulunulmuştur.

Anahtar kelimeler: Otuma oranı, eşdeğer ayak, eşdeğer radye, oturma, kazıklı radye temel.

To My Mother

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## **LIST OF SYMBOLS**

### LATIN SYMBOLS

$A_G$	plan area of pile group
$A_P$	total cross-sectional area of the piles in the group
$B$	overall width of the group
$D$	depth of foundation
$d$	pile diameter
$d_e$	equivalent pier diameter
$E_b$	soil modulus of bearing stratum
$E_d$	modulus of deformation at $(H+D)$ level
$E_e$	equivalent pier modulus
$E_f$	modulus of deformation at foundation level
$E_p$	pile modulus
$E_s'$	drained soil modulus
$E_u$	undrained soil modulus
$G_l$	soil shear modulus at the level of pile base
$G_{l/2}$	soil shear modulus at the $l/2$ level
$G_b$	soil shear modulus below the level of pile base
$H$	thickness of the soil layer
$I_p$	influence factor for equivalent raft method
$I_\delta$	influence factor for equivalent pier method

$k$	stiffness of a single pile
$K$	stiffness of pile group
$L$	overall length of the group for equivalent raft method Pile length for settlement ratio and equivalent pier method
$L_e$	equivalent pier length
$\mu_d$	depth factor
$\mu_g$	geological factor
$m_v$	coefficient of volume compressibility
$n$	number of piles in the group
$P$	load
$P_b$	base load
$P_s$	shaft load
$P_t$	total load
$q_n$	net foundation pressure
$R_A$	area ratio
$r_b$	radius of pile base
$r_m$	maximum radius
$r_0$	pile radius
$R_s$	settlement ratio
$s$	pile spacing
$w_b$	base settlement
$w_s$	shaft settlement
$w_t$	pile head settlement
$z$	depth

## GREEK SYMBOLS

$\zeta$	measure of radius of influence of pile
$\eta$	ratio of underream for underreamed piles
$\lambda$	pile-soil stiffness ratio
$\xi$	ratio of end-bearing for end-bearing piles
$\xi_h$	correction factor for effect of finite layer
$\xi_v$	correction factor for effect of Poisson's ratio
$\rho$	variation of soil modulus with depth
$\nu_s$	Poisson's ratio for drained conditions
$\nu_u$	Poisson's ratio for undrained conditions
$\eta_w$	efficiency of pile group
$\delta$	settlement
$\delta_i$	immediate settlement
$\delta_c$	consolidation settlement
$\delta_{\text{oed}}$	oedometer settlement
$\sigma_z$	average effective vertical stress
$\mu_0$	influence factor related to the depth of the equivalent raft
$\mu_1$	influence factor related to the thickness of the compressible soil layer

## **CHAPTER 1**

### **INTRODUCTION**

Several techniques have been proposed for analyzing the settlement of pile groups. These techniques can usually be classified into one of the following three categories.

- a. Estimates of settlement of pile groups are based on purely empirical data. Among the empirical approaches are those for groups in sand proposed by Skempton (in Poulos 1980) on the basis of limited number of field observations. Meyerhof (in Poulos 1980) suggests a method for a square group for driven piles and displacement caissons in sand.
- b. Simplified techniques which reduce a pile group to an equivalent simpler form of foundation for analysis purposes.

Simplified procedures, which reduce a group to an equivalent raft are used. There are variations in the suggested procedures (Tomlinson (1986), Ordemir (1984)). The depth at which the equivalent raft is located depends on the nature of the soil profile.

Simplified methods which reduce the group to an equivalent pier are suggested by Poulos and Davis (1980), Poulos (1993). Two types of approximations may be made:

1. An equivalent single pier of the same circumscribed plan area as the group and of some equivalent length,  $L_e$ .
2. An equivalent single pier of the same length,  $L$ , as the piles, but having an equivalent diameter,  $d_e$ .

In the so called settlement ratio method, the settlement of a single pile at the average load level is multiplied by settlement ratio  $R_s$  to calculate group settlement. The interaction factor approach can be used to derive theoretical values of  $R_s$ , and some values of  $R_s$  so derived are tabulated (Poulos and Davis (1980)). Randolph, and Fleming et al. (1992), has developed a very useful approximation for  $R_s$ . (Poulos (1989), Fleming et al. (1992))

- c. Analytical methods which consider interaction between the piles and surrounding soil.

Methods which compute the response of a single pile and which consider pile-soil-pile interaction via interaction factors make use of some form of elastic theory ( Poulos 1968, Randolph and Wroth 1979). The analysis is based on elastic soil characterized by shear modulus  $G$  which may vary with depth and a Poisson's ratio  $\nu$ . To analyze the settlement behaviour of a general pile group, superposition of the two-pile interaction factors may be employed.

Finite element method is a powerful analytical tool that can be used in settlement analyses. Non-linear soil behaviour can be modelled. Also the complete history of the pile can be simulated, i.e. the processes of installation, reconsolidation of the soil following installation, and subsequent loading of the pile. Such analyses are valuable in leading to a better understanding of the details of pile behaviour, but are unlikely to be readily applicable to practical piling

problems because of their complexity and the considerable number of geotechnical parameters required (e.g. Ottoviani 1975).

Complete boundary element method, in which each pile is divided into discrete elements and pile-soil-pile interaction is considered between each of these elements is another way of analyzing settlement of pile foundation (Poulos and Davis (1980)). The boundary element methods are more economical than the finite element method in pile group analysis, but these methods require double integration of analytical point load solution that may be cumbersome and relatively time-consuming.

A modification of complete boundary element analysis, “the hybrid method”, has been developed by Chow (1986) and Lee (1993). Here, a load transfer analysis is used to determine the response of a single pile, and continuum theory is employed to determine the influence of adjacent piles on this response.

This study is focused on the simpler methods namely settlement ratio, equivalent pier, and equivalent raft methods. Over thirty case histories are studied to examine them thoroughly and some suggestions are given about the use of these methods.

In Chapter 2 the simpler methods are reviewed in some detail. Case histories are presented in Chapter 3 and Appendix. All parameters used and calculations are summarized in each case. Settlement ratio, equivalent pier and equivalent raft solutions are made for all cases.

Conclusions reached and obversations made in the calculation of settlement of piled raft foundations are given in a compact form in Chapter 4.

## CHAPTER 2

### SIMPLIFIED DESIGN METHODS

#### **2.1. Settlement Ratio Method**

A convenient way of regarding the effects of interaction within a pile group has been suggested by Butterfield and Douglas (in Fleming, W. et al, 1992). The stiffness,  $K$ , of the pile group may be expressed as fraction  $\eta_w$  of the sum of the individual pile stiffness,  $k$ . Thus for a group of piles ( $n$ : number of piles),

$$K = \eta_w n k \quad \dots(2.1)$$

The factor  $\eta_w$  is the inverse of the settlement ratio,  $R_s$ , and may be thought of as an efficiency. For no interaction between piles,  $\eta_w$  would equal unity. The efficiency may be written as

$$\eta_w = n^{-e} \quad \dots(2.2)$$

Where the exponent  $e$  will lie between 0.4 and 0.6 for most pile groups (Poulos (1993)). The actual value of  $e$  will depend on

pile slenderness ratio,  $L/d$  (pile length/pile diameter)

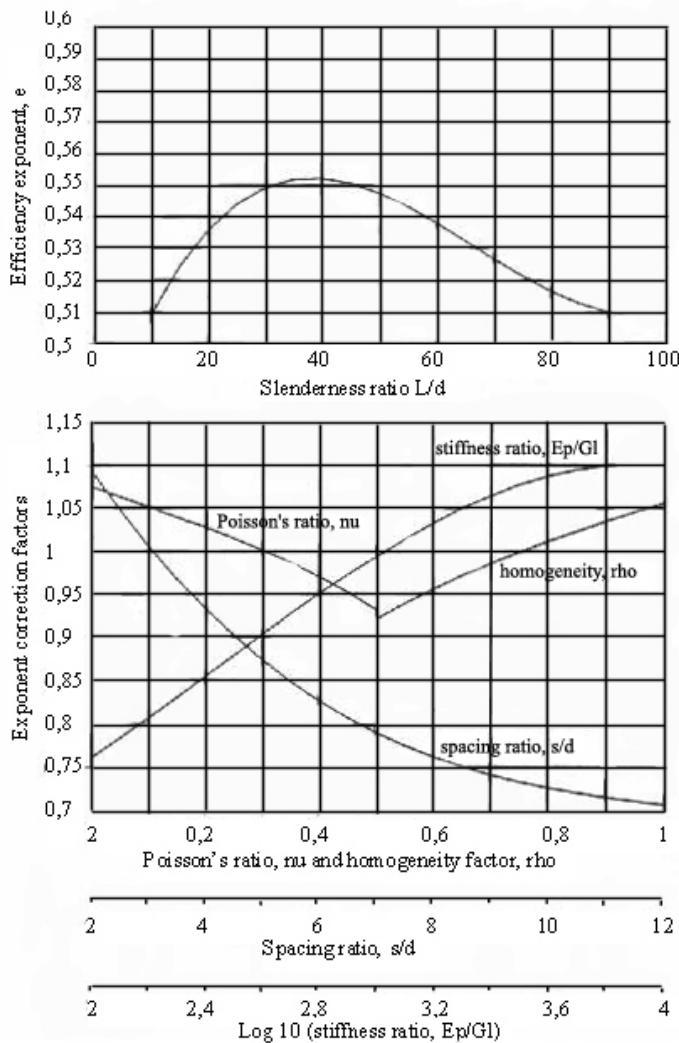
pile stiffness ratio,  $\lambda = E_p/G_l$  (pile modulus/soil shear modulus)

pile spacing ratio,  $s/d$  (pile spacing/pile diameter)

homogeneity of soil, characterised by  $\rho$ ,

Poisson's ratio,  $\nu$

For a given combination of the above factors, the value of  $e$  may be estimated using the curves shown in Figure 2.1 (Fleming et al, 1992). The upper part of the figure allows a base of  $e$  to be chosen, depending on pile slenderness ratio (assuming  $\lambda=1000$ ,  $s/d=3$ ,  $\rho=0.75$ ,  $\nu =0.3$ ). The four curves in lower part of the figure then modify this basic value of pile stiffness ratio,  $s$ ,  $\nu$  and  $\rho$ .



**Figure 2.1:** Charts for calculation of exponent  $e$  for efficiency of pile groups.  
(Fleming, et al, 1992)

The base settlement and shaft settlement will be similar to the settlement of pile head,  $w_t$  for a single stiff pile. The total load,  $P_t$ , may thus be written as

$$P_t = P_b + P_s = w_t \left( \frac{P_b}{w_b} + \frac{P_s}{w_s} \right) \quad \dots(2.3)$$

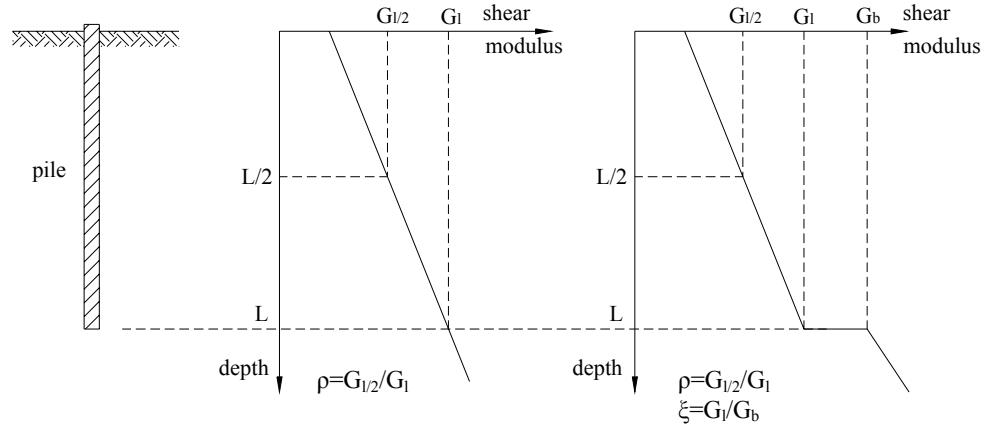
In developing a general solution for the axial response of a pile, it is convenient to introduce a dimensionless load settlement ratio for the pile. The stiffness is  $P_t/w_t$  and this may be made dimensionless by dividing by the radius of the pile and an appropriate soil modulus. It has been customary to use the value of soil modulus at the level of pile base for this purpose, written as  $G_l$ . Thus equation becomes

$$\frac{P_t}{w_t r_0 G_l} = \frac{4 r_b G_b}{(1-v) r_0 G_l} + \frac{2\pi G_{l/2}}{G_l} \frac{L}{r_0} \quad \dots(2.4)$$

The shear modulus variation with depth may be idealized as linear, according to  $G=G_0+mz$  (where  $z$  is depth), with the possibility of sharp rise to  $G_b$  below the level of pile base (Figure 2.2) (Fleming, W.G. et al, (1992)). Defining parameters  $\rho=G_{l/2}/G_l$  and  $\xi=G_l/G_b$ , the constant  $\zeta$  has been found to fit the expressions (Randolph and Wroth, (1978))

$$\zeta = \ln \{ [0.25 + (2.5\rho(1-v)-0.25) \xi] L/r_0 \} \quad \dots(2.5)$$

$$\zeta = \ln [2.5\rho(1-v)L/r_0] \text{ for } \xi = 1 \quad \dots(2.6)$$



**Figure 2.2:** Assumed variation of soil shear modulus with depth

Substituting in the appropriate boundary conditions at the pile base yields an expression for load settlement ratio of the pile head of

$$\frac{P_t}{G_l r_0 w_t} = \frac{\frac{4\eta}{(1-v)\xi}}{1 + \frac{4\eta}{\Pi\lambda(1-v)\xi}} + \frac{\frac{2\Pi\rho}{\zeta}}{\frac{4\eta}{\Pi\lambda(1-v)\xi}} \frac{\tanh(\mu L)}{\mu L} \frac{L}{r_0} \dots (2.7)$$

where, summarizing the various dimensionless parameters, (Randolph 1994, Birand 2001)

$\eta = r_b/r_0$  (ratio of underreamed for underreamed piles)

$\xi = G_l/G_b$  (ratio of end-bearing for end-bearing piles)

$\lambda = E_p/G_l$  (pile-soil stiffness ratio)

$\zeta = \ln(r_m/r_0)$  (measure of radius of influence of pile)

$\mu = (2/(\zeta\lambda))^{0.5} L/r_0$  (measure of pile compressibility)

Finally settlement of a group pile can be calculated as

$$\delta_{\text{group}} = \frac{P_{\text{group}}}{K} \quad \dots(2.8)$$

where  $K = \eta_w k n$

$$k = P_t / w_t$$

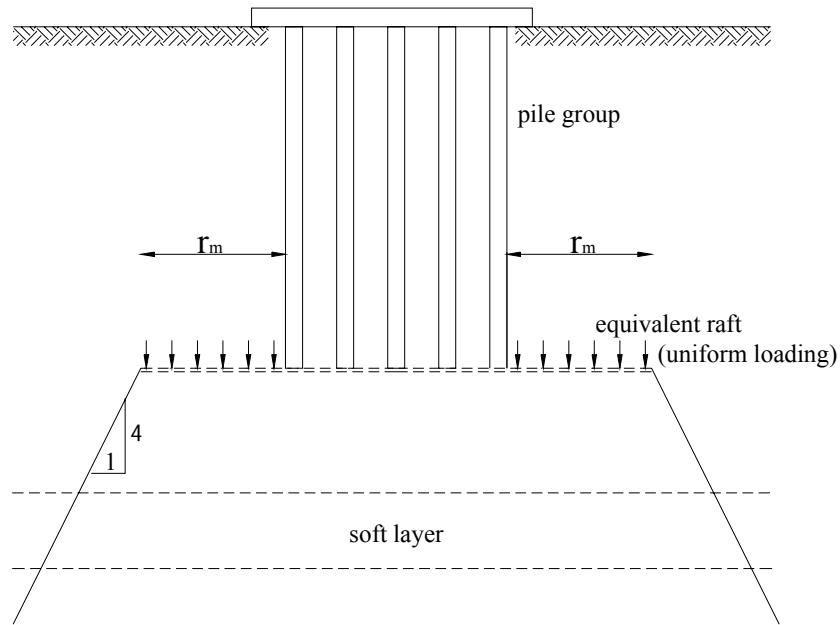
or

$$\delta_{\text{group}} = \delta_{\text{single}} R_s \quad \dots(2.9)$$

where  $\delta_{\text{single}} = P_{\text{single}} / k$

$$R_s = n^e$$

The effect of different layers of soil over the depth of penetration of the piles in a group may generally be dealt with adequately by adopting suitable values of the average shear modulus for the soil, and a value for the homogeneity factor,  $\rho$ , which reflects the general trend of stiffness variation with depth. However particular attention needs to be paid to the case where a soft layer of soil occurs at some depth beneath the pile group, as shown in Figure 2.3 (Fleming, W.G. et al, (1992)). In assessing how much additional settlement may occur due to the presence of soft layer, the average change in vertical stress caused by the pile group must be estimated.



**Figure 2.3:** Use of equivalent raft for calculating effect of soft layer underlying pile group

Implicit in the solution for the load settlement response of a single pile is the idea of the transfer of the applied load, by means of induced shear stresses in the soil, over a region of radius  $r_m$  (Randolph and Wroth, (1978)). The average vertical stress applied to the soil at the level of the base of a group of a piles may be estimated by taking the overall applied load and distributing it over the area of the group augmented by this amount, as shown in Figure 2.3. Below the level of the pile bases, the spread of the area over which the load assumed to be shared may be taken as the usual rate of 1:4 (Tomlinson 1986)

$$r_m = [ 0.25 + ( 2.5 \rho ( 1-v ) - 0.25 ) \xi ] L \quad \dots(2.10)$$

The interaction factor approach can be used to derive theoretical values of  $R_s$ . Table 2.2 (Poulos and Davis (1980)) shows the theoretical values of  $R_s$ , for floating-pile groups in a deep layer of uniform soil, and in Table 2.3 (Poulos and Davis (1980)) for pile groups bearing on rigid stratum. These values apply to square groups of piles with a rigid cap in which the center-to-center spacing between adjacent piles in a row is  $s$ , and the length and diameter of each pile are  $L$  and  $d$ , respectively. The pile stiffness factor is  $K$ .  $K$  is defined as

$$K = \frac{E_p}{E_s} R_A \quad \dots(2.11)$$

where  $R_A = A_p / (\pi d^2 / 4)$  (Ratio of area of pile section  $A_p$  to area bounded by outer circumference of pile) (Poulos and Davis (1980))

Average values of pile-stiffness factor  $K$ , calculated for various types of pile and soil, are given in Table 2.1 (Poulos and Davis (1980)).

**Table 2.1:** Average values of  $K$  for solid piles (Poulos and Davis, 1980)

Soil Type	Pile Material		
	Steel	Concrete	Timber
Soft clay	60.000	6.000	3.000
Medium clay	20.000	2.000	1.000
Stiff clay	3.000	300	150
Loose sand	15.000	1.500	750
Dense sand	5.000	500	250

**Table 2.2:** Theoretical Values of Settlement Ratio  $R_s$  Friction Pile Groups, with Rigid Cap, in Deep Uniform Soil Mass  
(Poulos and Davis, 1980)

No of piles																			
in group				4				9				16				25			
L/d	s/d	K		10	100	1000	$\infty$	10	100	1000	$\infty$	10	100	1000	$\infty$	10	100	1000	$\infty$
10	2		1,83	2,25	2,54	2,62	2,78	3,80	4,42	4,48	3,76	5,49	6,40	6,53	4,75	7,20	8,48	8,68	
	5		1,40	1,73	1,88	1,90	1,83	2,49	2,82	2,85	2,26	3,25	3,74	3,82	2,68	3,98	4,70	4,75	
	10		1,21	1,39	1,48	1,50	1,42	1,76	1,97	1,99	1,63	2,14	2,46	2,46	1,85	2,53	2,95	2,95	
25	2		1,99	2,14	2,65	2,87	3,01	3,64	4,84	5,29	4,22	5,38	7,44	8,10	5,40	7,25	9,28	11,25	
	5		1,47	1,74	2,09	2,19	1,98	2,61	3,48	3,74	2,46	3,54	4,96	5,34	2,95	4,48	6,50	7,03	
	10		1,25	1,46	1,74	1,78	1,49	1,95	2,57	2,73	1,74	2,46	3,42	3,63	1,98	2,98	4,28	4,50	
50	2		2,43	2,31	2,56	3,01	3,91	3,79	4,52	5,66	5,58	5,65	7,05	8,94	7,26	7,65	9,91	12,66	
	5		1,73	1,81	2,10	2,44	2,46	2,75	3,51	4,29	3,16	3,72	5,11	6,37	3,88	4,74	6,64	8,67	
	10		1,38	1,50	1,78	2,04	1,74	2,04	2,72	3,29	2,08	2,59	3,73	4,65	2,49	3,16	4,76	6,04	
100	2		2,56	2,31	2,26	3,16	4,43	4,05	4,11	6,15	6,42	6,14	6,50	9,92	8,48	8,40	10,25	14,35	
	5		1,88	1,88	2,01	2,64	2,80	2,94	3,38	4,87	3,74	4,05	4,98	7,54	4,68	5,18	6,75	10,55	
	10		1,47	1,56	1,76	2,28	1,95	2,17	2,73	3,93	2,45	2,80	3,81	5,82	2,95	3,48	5,00	7,88	

**Table 2.3:** Theoretical Values of Settlement Ratio  $R_s$  End-Bearing Pile Gr., with Rigid Cap, Bearing on a Rigid Stratum  
(Poulos and Davis, 1980)

No of piles in group			4				9				16				25			
L/d	s/d	K	10	100	1000	$\infty$	10	100	1000	$\infty$	10	100	1000	$\infty$	10	100	1000	$\infty$
10	2		1,52	1,14	1,00	1,00	2,02	1,31	1,00	1,00	2,38	1,49	1,00	1,00	2,70	1,63	1,00	1,00
	5		1,15	1,08	1,00	1,00	1,23	1,12	1,02	1,00	1,30	1,14	1,02	1,00	1,33	1,15	1,03	1,00
	10		1,02	1,01	1,00	1,00	1,04	1,02	1,00	1,00	1,04	1,02	1,00	1,00	1,03	1,02	1,00	1,00
25	2		1,88	1,62	1,05	1,00	2,84	2,57	1,16	1,00	3,70	3,28	1,33	1,00	4,48	4,13	1,50	1,00
	5		1,36	1,36	1,08	1,00	1,67	1,70	1,16	1,00	1,94	2,00	1,23	1,00	2,15	2,23	1,28	1,00
	10		1,14	1,15	1,04	1,00	1,23	1,26	1,06	1,00	1,30	1,33	1,07	1,00	1,33	1,38	1,08	1,00
50	2		2,49	2,24	1,59	1,00	4,06	3,59	1,96	1,00	5,83	5,27	2,63	1,00	7,62	7,06	3,41	1,00
	5		1,78	1,73	1,32	1,00	2,56	2,56	1,72	1,00	3,28	3,38	2,16	1,00	4,04	4,23	2,63	1,00
	10		1,39	1,43	1,21	1,00	1,78	1,87	1,46	1,00	2,20	2,29	1,71	1,00	2,62	2,71	1,97	1,00
100	2		2,54	2,26	1,81	1,00	4,40	3,95	3,04	1,00	6,24	5,89	4,61	1,00	8,18	7,93	6,40	1,00
	5		1,85	1,84	1,67	1,00	2,71	2,77	2,52	1,00	3,54	3,74	3,47	1,00	4,33	4,68	4,45	1,00
	10		1,44	1,44	1,46	1,00	1,84	1,99	1,98	1,00	2,21	2,48	2,53	1,00	2,53	2,98	3,10	1,00

$R_s$  values for other numbers of piles may be interpolated from Table 2.2 and 2.3. For groups containing more than 16 piles, it has been found that  $R_s$  varies approximately linearly with the square root of the number of piles in the group. Thus, for a given value of pile spacing,  $K$  and  $L/d$ ,  $R_s$  may be extrapolated from the values for a 16-pile group and a 25-pile group as follows:

$$R_s = (R_{25} - R_{16}) (n^{0.5} - 5) + R_{25} \quad \dots(2.12)$$

where  $R_{25}$ : value of  $R_s$  for 25-pile group

$R_{16}$ : value of  $R_s$  for 16-pile group

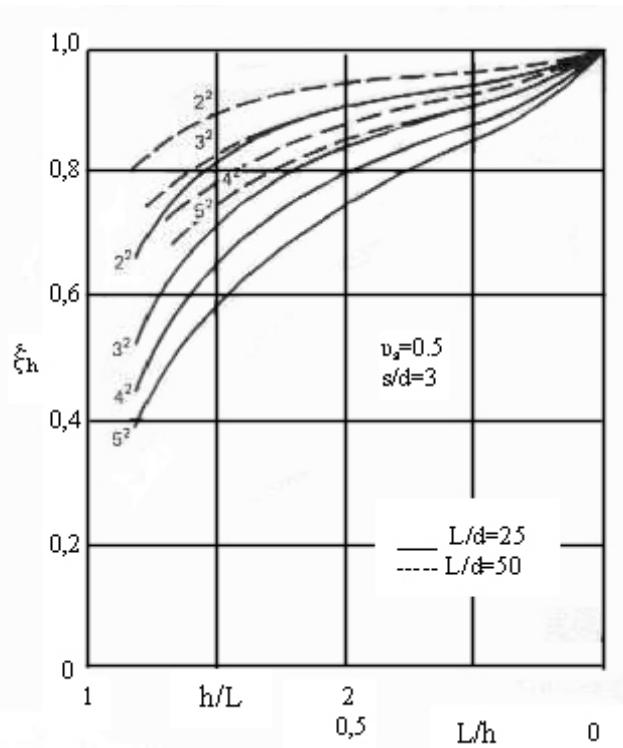
n: number of piles in group

For floating pile groups, the underlying rigid base below the soil layer tends to reduce the settlement ratio  $R_s$ . An indication of the extent of this decrease is given in Figure 2.4 (Poulos and Davis (1980)), in which, for typical groups, a reduction coefficient,  $\xi_h$ , is plotted against the ratio of layer depth  $h$  to pile-length  $L$ ,  $\xi_h$  being defined as,

$$\xi_h = R_s \text{ for finite layer of depth} / R_s \text{ for infinitely deep layer}$$

The effect of finite layer is more pronounced as the size of the group increases. As  $L/d$  increases, the effect of the finite layer becomes less significant.

As the relative stiffness of the bearing stratum  $E_b/E_s$  (modulus of bearing stratum/modulus of the soil along the pile shaft) increases  $R_s$  decreases, this effect being most pronounced for shorter stiffer piles. For slender piles (e.g.  $L/d = 100$ ) unless the piles are quite stiff ( $K > 1000$ ), the bearing stratum has little effect on settlements, because little load reaches the pile tip under normal working load conditions.



**Figure 2.4:** Reduction coefficient  $\xi_h$  for effect of finite layer (Poulos and Davis, 1980)

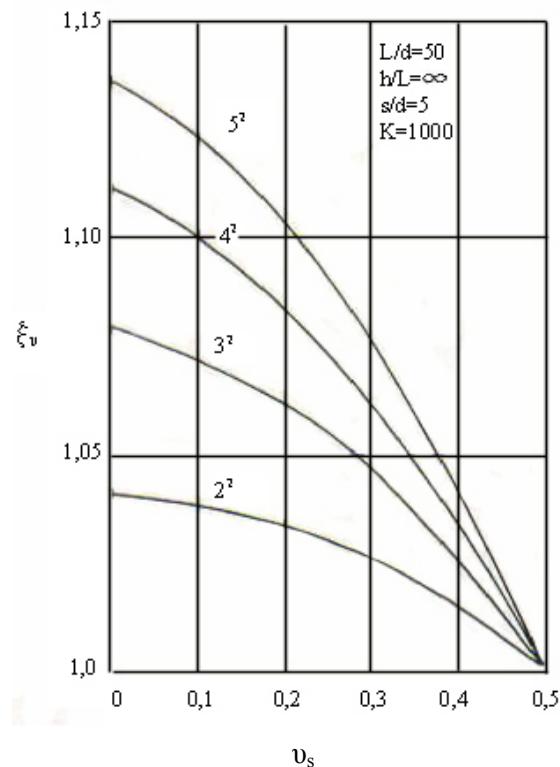
The effect of  $v_s$  on  $R_s$  is shown in Figure 2.5 (Poulos and Davis (1980)), in which factor  $\xi_v$  is plotted for a typical case,  $\xi_v$  being defined as

$$\xi_v = R_s \text{ for specified value of } v_s/R_s \text{ for } v=0.5$$

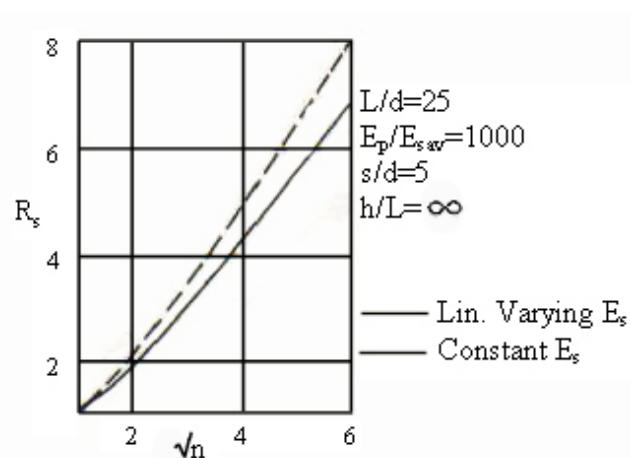
The effect of  $v_s$  becomes more pronounced as the number of piles in the group increases.

Figure 2.6 (Poulos and Davis (1980)) shows the effect of the distribution of soil modulus on  $R_s$  for typical case. Larger values of  $R_s$  occur for the uniform soil, the difference becoming greater as the number of piles increases.

As the spacing increases, the pile cap has an increasing effect, but for practical pile spacing, the influence of the cap appears to be negligible.



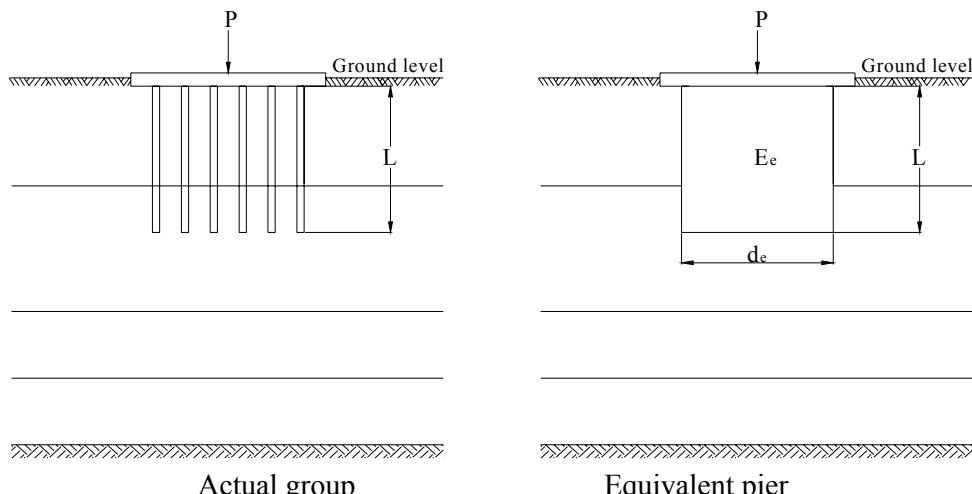
**Figure 2.5:** Correction factor  $\xi_v$  for effect of  $v_s$  (Poulos and Davis, 1980)



**Figure 2.6:** Effect of distribution of  $E_s$  on settlement ratio (Poulos and Davis, 1980)

## 2.2. Equivalent Pier Method

This method has been suggested by Poulos and Davis (1980) and illustrated in Figure 2.7. (Poulos (1993)). The pile group is replaced by a single pier of equivalent diameter,  $d_e$  (or length,  $L_e$ ) and equivalent stiffness.



**Figure 2.7:** Equivalent pier concept

$L_e$  is preferred for incompressible floating groups.  $d_e$  is more appropriate when the piles pass through layered soils or founded on very different material. For incompressible floating groups, for most practical cases,  $L_e/L$  lies between 0.9 and 0.6. For layered soils;

For friction piles;

$$d_e = 1.27 A_G^{0.5} \quad \dots(2.13)$$

For end-bearing piles;

$$d_e = 1.13 A_G^{0.5} \quad \dots(2.14)$$

where  $A_G$ : Plan area of pile group. Poulos (1993), Randolph (1994)

The equivalent pier modulus,  $E_e$ , is approximated as;

$$E_e = E_p \frac{A_p}{A_G} + E_s \left(1 - \frac{A_p}{A_G}\right) \quad \dots(2.15)$$

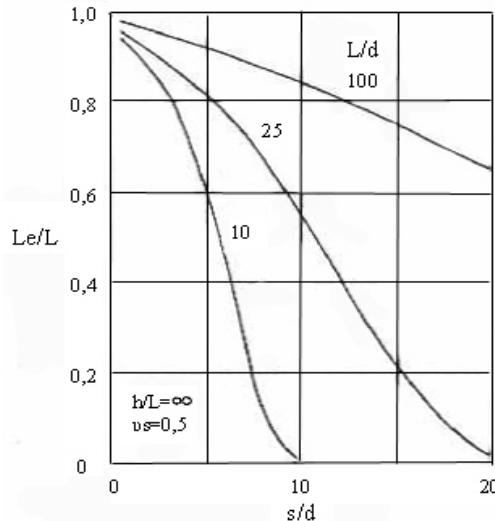
Where  $E_p$ : Young's modulus of piles

$E_s$ : average Young's modulus of soil within the group

$A_p$ : total cross-sectional area of the piles in the group.

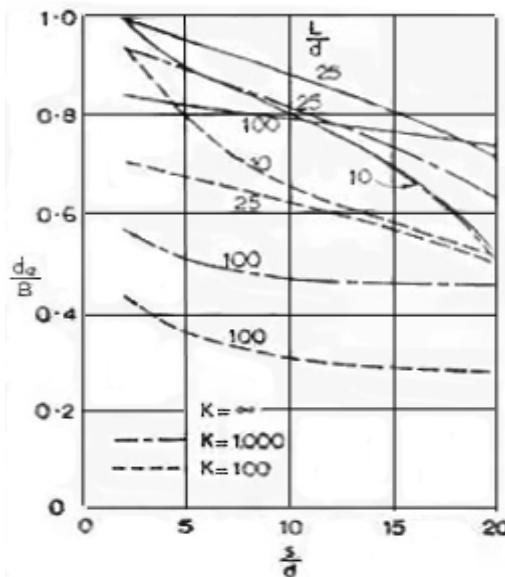
Having reduced the group to an equivalent pier, theoretical solutions for the settlement of a single pile may then be used to estimate the settlement (e.g. Randolph and Wroth, (1979); Poulos and Davis, (1980)).

For incompressible floating groups, values of  $L_e/L$  obtained by Poulos (1968), are shown in Figure 2.8. Poulos and Davis (1980).  $L_e/L$  depends both on spacing and  $L/d$ , but virtually independent of the number of piles in the group.



**Figure 2.8:** Equivalent length of single pier for same settlement as pile group (Poulos and Davis, 1980)

Relationships between  $d_e/B$  and  $s/d$  are plotted in Figure 2.9 (Poulos and Davis(1980)) for floating piles.  $B$  is the width of the raft. Like  $L_e/L$ ,  $d_e/B$  is almost independent of the group's size, but it does depend on  $L/d$ . The ratio  $d_e/B$  tends to decrease with increasing pile compressibility. It should be noted that the equivalent pier in Figure 2.9 has the same value of pile stiffness factor,  $K$  (equation 2.11) as the pile in the group.

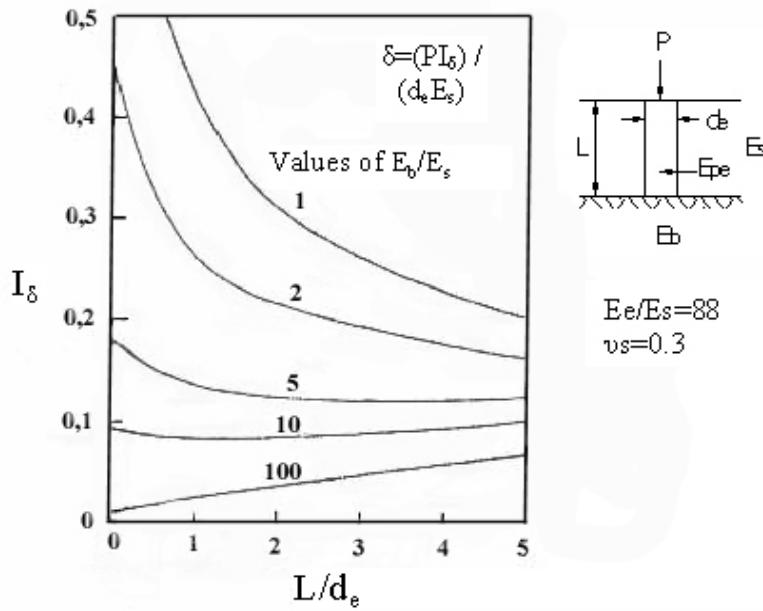


**Figure 2.9:** Diameter of equivalent pier to represent pile group (Poulos and Davis, 1980)

Figure 2.10 presents dimensionless solutions for a pier in a homogeneous soil, bearing on a stratum of equal or greater stiffness. The compressibility of the pier has been chosen to be representative of the average value of a pile and soil block with piles at spacing of about 3 diameters. For short

piers, the relative compressibility is unimportant unless the pier is very compressible, or unless it is founded on a very stiff stratum. Figure 2.10 may be used with sufficient accuracy for a pier in non-homogeneous soil, by using an average soil modulus along the shaft of the pier (Poulos (1972)) .

The  $I_\delta$ , displacement influence factor, depends on slenderness ratio, pile material, soil homogeneity and relative soil-pile stiffness which are given in equation 2.16 (Randolph and Wroth, (1978), (1979)).



**Figure 2.10:** Settlement of equivalent pier in soil layer (Poulos, 1972)

$$I_\delta = \frac{1 + \frac{1}{\Pi\lambda} \frac{8}{(1-v_s)} \frac{\eta}{\xi} \frac{\tanh(\mu L)}{\mu L} \frac{L}{d}}{\frac{4}{(1-v_s)} \frac{\eta}{\xi} + \frac{4\Pi\rho}{\zeta} \frac{\tanh(\mu L)}{\mu L} \frac{L}{d}} \quad \dots(2.16)$$

In deep homogeneous soil Randolph (1994) reported that, in order to improve the accuracy of equation 2.7 for relatively short and thick piers, the maximum radius of influence,  $r_m$ , should empirically be increased giving revised equation for  $\zeta$  of (Horikoshi and Randolph (1999)):

$$\zeta = \ln[A + 2,5(1-v)L_p/r_p] \quad (A=5, \text{ for small } L_p/r_p) \quad \dots(2.17)$$

Horikoshi (in Horikoshi and Randolph (1999)) discussed the applicability of equation 2.17 to piers in deep non-homogeneous soil where the soil modulus increase linearly with depth. He found that for piers installed in non-homogeneous soil, the following equation is suitable :

$$\zeta = \ln\{A + [0,25 + (2,5\rho(1-v)-0,25)\xi]L_p/r_p\} \quad (A=5 \text{ for small } L_p/r_p) \quad \dots(2.18)$$

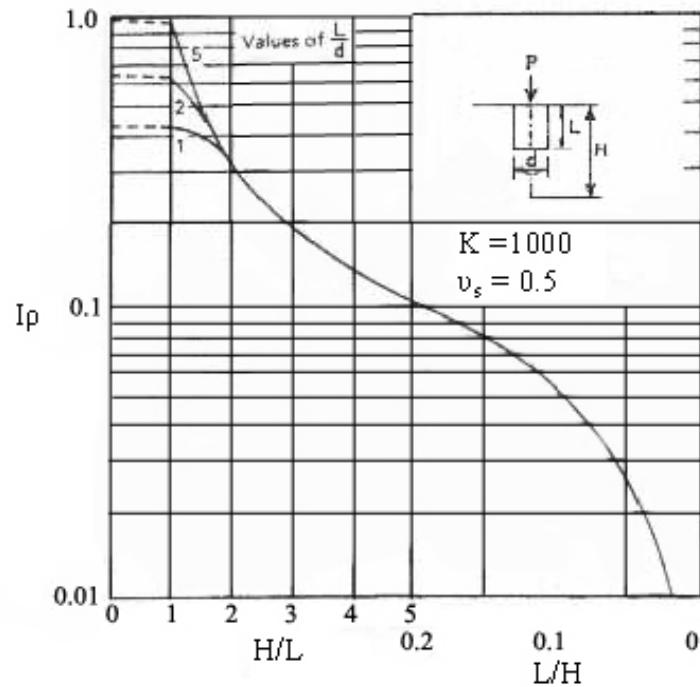
In practical cases in which the soil profile is layered and compressible strata are present below the piles, the settlement caused by these strata must be considered in calculating the overall settlement of the group. The settlement of compressible stratas are given approximately as;

$$\delta_{\text{layered}} = \frac{P}{L} \left( \sum_{k=2}^{m-1} \frac{I_k - I_{k+1}}{E_{sk}} \right) \quad \dots(2.19)$$

where  $I_k$ : displacement influence factor  $I_p$  on the pile axis at level of the top of layer  $j$ ;  $E_{sk}$ : Young modulus of layer  $k$ ;  $m$ : number of layers of different soils.

For application of equation (2.19), it is convenient to have values of influence factor  $I_p$  on the axis plotted against depth, and such a plot is shown in

Figure 2.11 (Poulos and Davis (1980)) for three values of  $L/d$  and for  $v_s=0.5$ . The effect of  $L/d$  becomes insignificant for  $H/L>1.75$ .

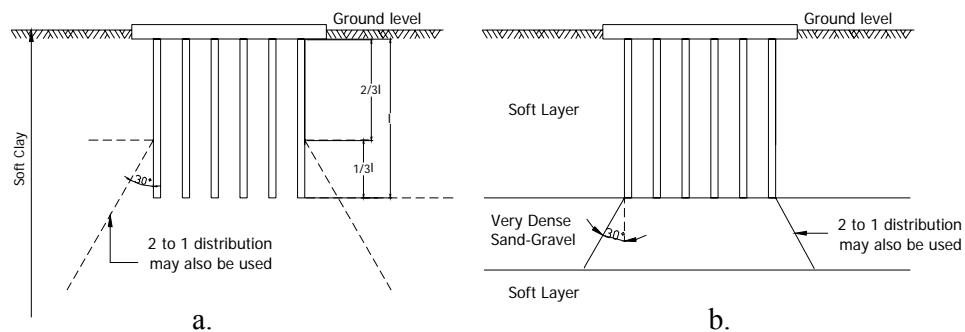


**Figure 2.11:** Influence factors for settlement beneath center of a pier. (Poulos and Davis, 1980)

### 2.3. Equivalent Raft Method

This approach is described in many foundation engineering texts, but there are some differences in the suggested procedure for reducing the group to an equivalent raft.

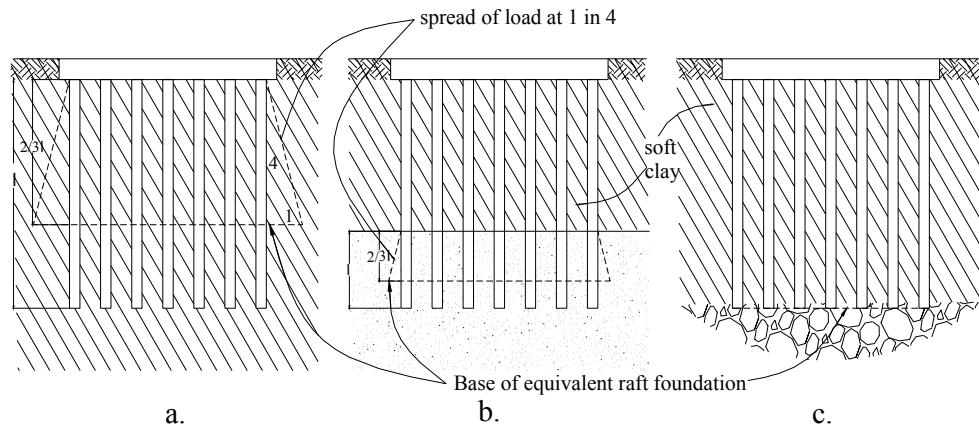
**a)** The depth at which the equivalent raft is located depends on the nature of the soil profile and ranges from  $2l/3$  for friction pile groups to  $l$  for end-bearing pile groups, where  $l$  is the pile length. It is assumed that pressure is distributed at 2V:1H slope (Figure 2.12). If the end-bearing piles rest on a rock or a very hard layer that is thick enough, the settlement analysis is not necessary Ordemir (1984).



**Figure 2.12:** Settlement of a group of piles. **a.** Settlement analysis of a group of friction piles in clay **b.** Stresses on top of a compressible layer for calculating settlement of a group of end-bearing piles.

**b)** The procedure suggested by Tomlinson (1986) is illustrated in Figure 2.13. (Poulos (1993). Load transfer in skin friction from the pile shaft to the surrounding soil is allowed for by assuming that the load is spread from the

shafts of friction piles at an angle of 1 in 4 from the vertical. Three cases of load transfer are shown in Figure 2.13.a to c.



**Figure 2.13:** Load transfer to soil from pile group. **a.** Group of piles supported predominantly by skin friction. **b.** Group of piles driven through soft clay to combined skin friction and end bearing in stratum of dense granular soil. **c.** Group of piles supported in end bearing on hard rock stratum

In order to obtain more accurate settlement prediction, Brzezinski (in Blanchet, Tavenas, and Garneau (1980)) suggested that the theoretical footing is assumed to be located at the tip of the piles if the pile spacing is large or if a significant number of the piles are battered.

The settlement of piles in cohesive soils primarily consists of the sum of the following two components:

1. Short-term settlement occurring as the load is applied.
2. Long-term consolidation settlement occurring gradually as the excess pore pressures generated by loads are dissipated.

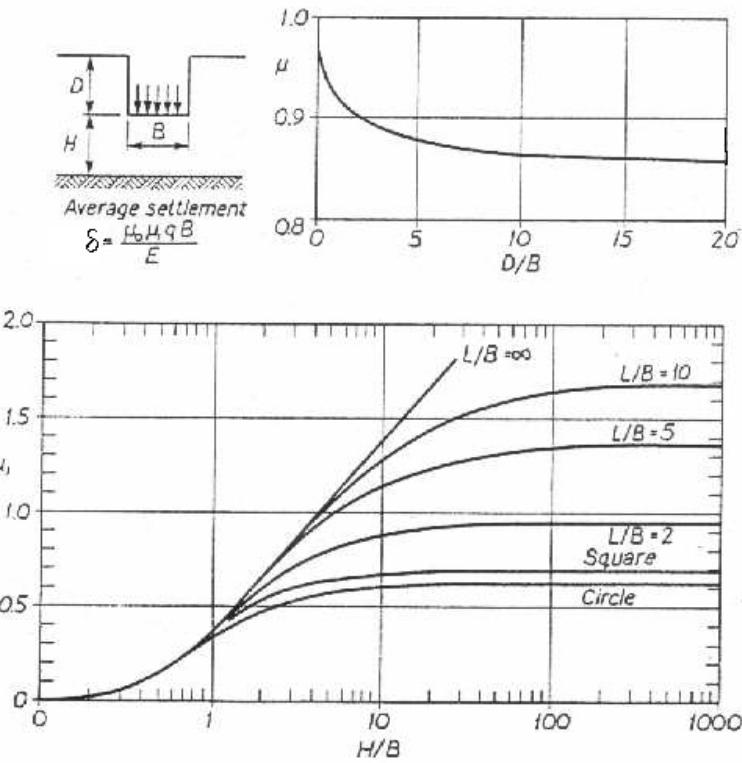
Long-term settlement will be computed by using the drained Young's modulus of the soil. For highly overconsolidated clays, long-term consolidation settlement does not occur. Calculation of short-term (undrained) settlements in clays would require the use of the undrained Young's modulus together with the strain factors for the undrained values of Poisson's ratio.

The average immediate settlement of a foundation at depth D below the surface is;

$$\delta_i = \frac{\mu_i \mu_0 q_n B}{E_u} \quad \dots(2.20)$$

In the above equation Poisson's ratio is assumed to be equal to 0.5. The factors  $\mu_i$  and  $\mu_0$ , which are related to the depth of equivalent raft, the thickness of compressible soil layer and the length/width ratio of the equivalent raft foundation, are shown in Figure 2.14.

The influence values in Figure 2.14 are based on the assumption that the deformation modulus is constant with depth. However, in most natural soil and rock formations the modulus increases with dept such that calculations for the conditions based on a constant modulus give exaggerated estimates of settlement.



**Figure 2.14:** Influence factors for calculating immediate settlements of flexible foundations of width  $B$  at depth  $D$  below ground surface (after Christian and Carrier, 1978)

Butler (1974) developed a method for settlement calculations for the conditions of a deformation modulus increasing linearly with depth within a layer of finite thickness. The value of modulus at a depth  $z$  below foundation level is given by the equation;

$$E_d = E_f (1 + k z / B) \quad \dots(2.21)$$

and

$$\delta_i = \frac{q_n B I_p}{E_f} \quad \dots(2.22)$$

where  $E_f$  is the modulus of deformation at foundation level (the base of the equivalent raft) and  $\delta_i$  is the settlement at the corner of the loaded area. Having obtained  $k$ , the appropriate factor for  $I'_p$  is obtained from Butler's curves shown in Figure 2.15. These are different ratios for  $L/B$  at the level of the equivalent raft, and are applicable for a compressible layer thickness not more than  $9*B$ . The curves are based on the assumption of a Poisson's ratio of 0.5 for undrained conditions, this is for immediate application of the load.

The consolidation settlement  $\delta_c$  is calculated from the results from oedometer tests made on clay samples in the laboratory. Having obtained a representative value of  $m_v$  for each soil layer stressed by the pile group, the oedometer settlement  $\delta_{oed}$  for this layer at the centre of the loaded area is calculated from the equation

$$\delta_{oed} = \mu_d m_v \sigma_z H \quad \dots(2.23)$$

where  $\mu_d$  is a depth factor,  $\sigma_z$  is the average effective vertical stress imposed on the soil layer due to the net foundation pressure  $q_n$  at the base of the equivalent raft foundation and  $H$  is the thickness of the soil layer. The depth factor is obtained from Fox's correction curves shown in Figure 2.16. To obtain the average vertical stress  $\sigma_z$  at the centre of each soil layer the coefficients in Figure 2.17 (Tomlinson (1986)) should be used. The oedometer settlement must now be corrected to obtain the field value of the consolidation settlement, where

$$\delta_c = \delta_{oed} \mu_g \quad \dots(2.24)$$

Published values of  $\mu_g$  have been based on comparisons of the settlement of actual structures with computations made from laboratory

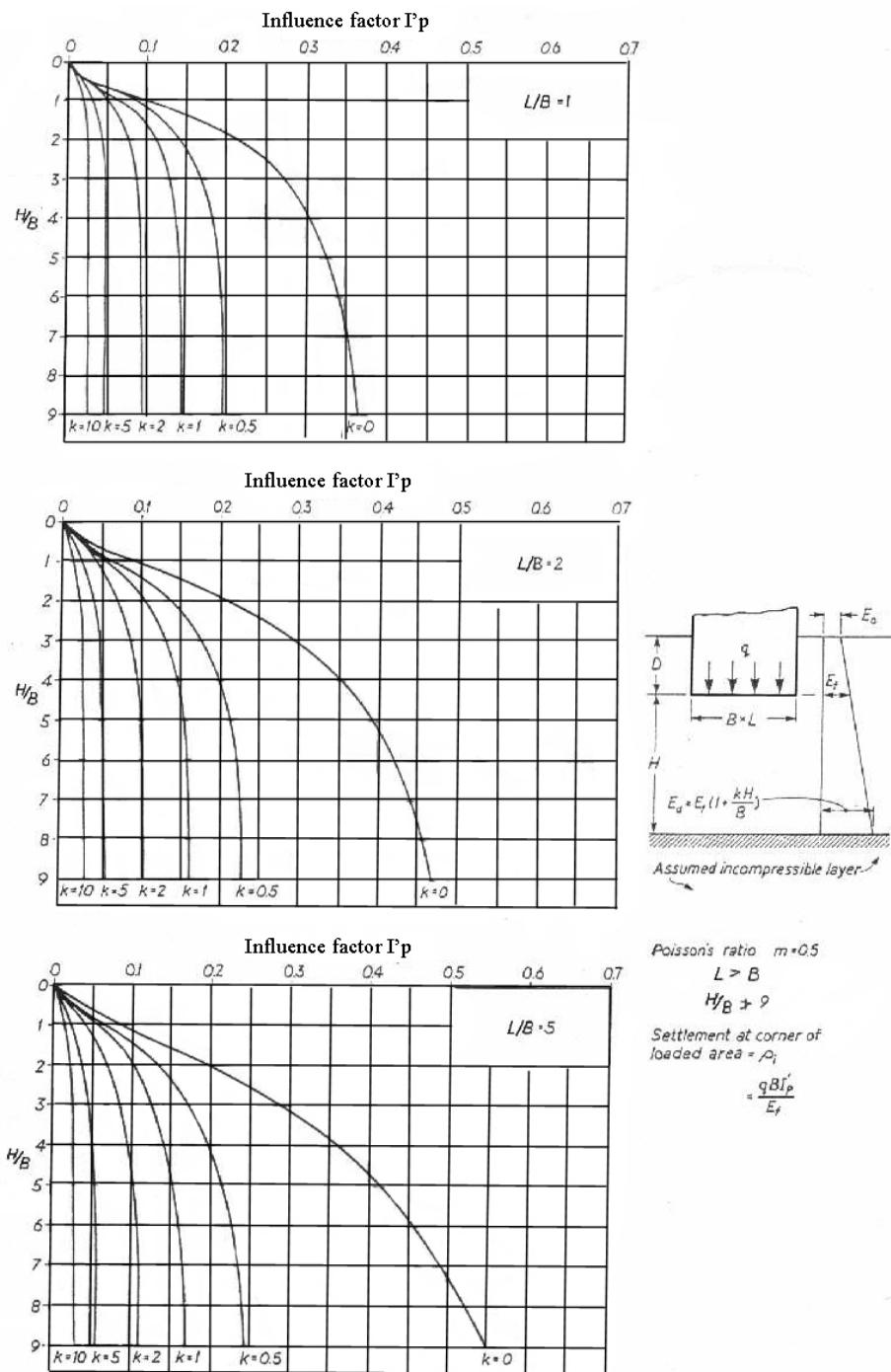
oedometer tests. Values established by Skempton and Bjerrum (1957) are shown in Table 2.4.

**Table 2.4:** Value of geological factor  $\mu_g$  (Skempton and Bjerrum, 1957)

Type of Clay	$\mu_g$ value
Very sensitive clays (soft alluvial, estuarine and marine clays)	1,0-1,2
Normally-consolidated clays	0,7-1,0
Over-consolidated clays (London clay, Weald, Kimmeridge, Oxford and Lias clays)	0,5-0,7
Heavily over-consolidated clays (unweathered glacial till, Keuper Marl)	0,2-0,5

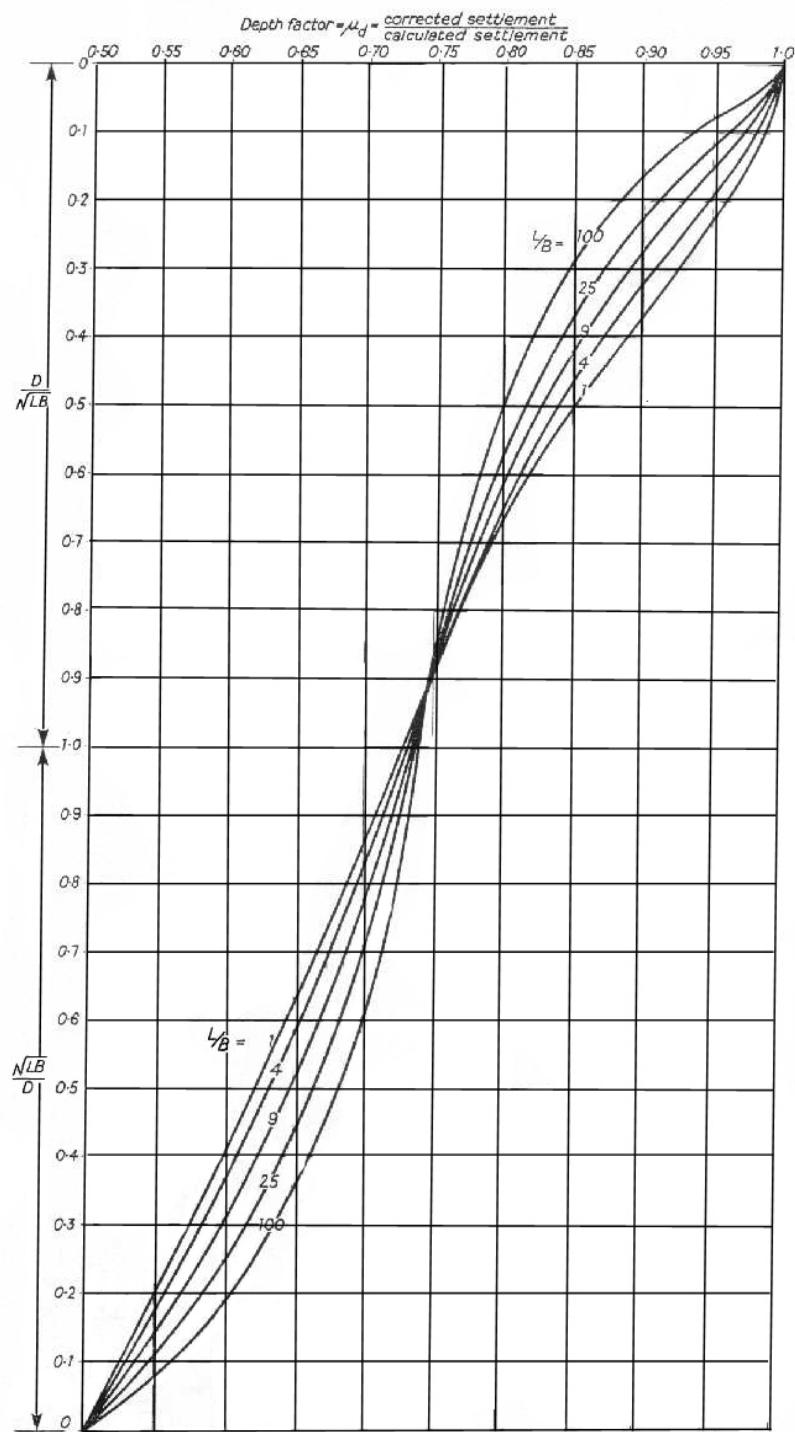
In layered soils with different values of the deformation modulus  $E_u$  in each layer or soils which show progressively increasing modulus with increases in depth, the strata below the base of the equivalent raft are divided into a number of representative horizontal layers and average value of  $E_u$  is assigned to each layer. The dimensions L and B in Figure 2.14 are determined on the assumption that the load is spread to the surface of each layer at an angle of 30° from the edges of the equivalent raft (Figure 2.18) (Tomlinson (1986). The total settlement of piled foundation is then sum of the average settlements calculated for each soil layer from equation 2.20.

Pile groups under compressive loading

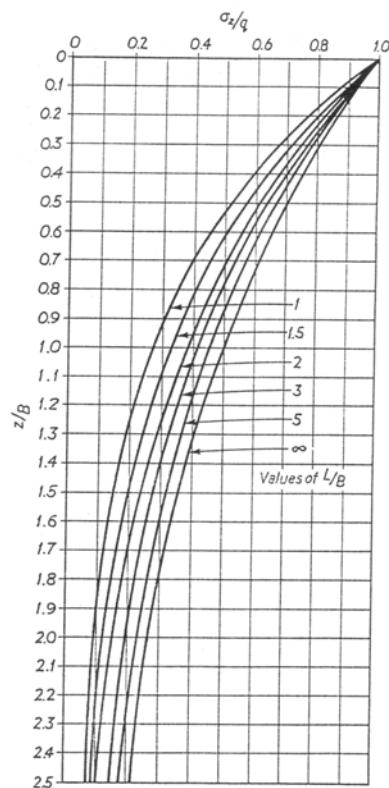


**Figure 2.15:** Values of the influence factor  $I_p$  for deformation modulus increasing linearly with depth and modular ratio of 0.5 (after Butler, 1974)

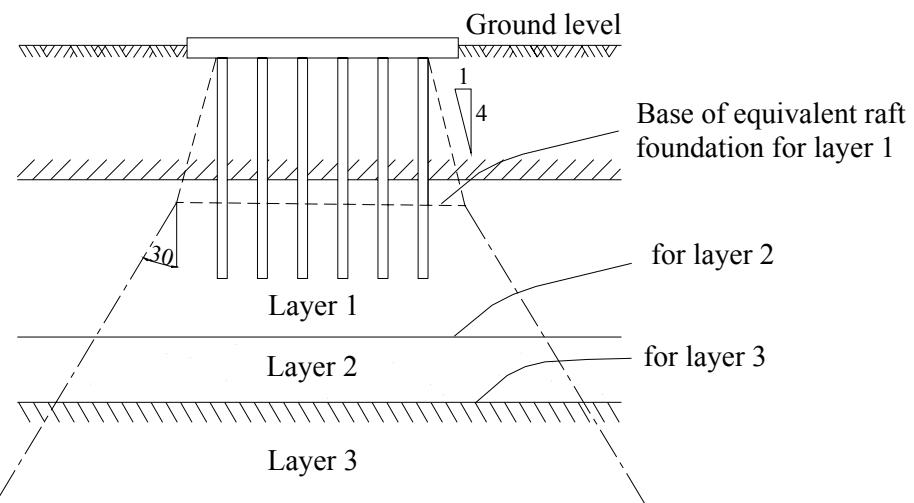
Pile groups under compressive loading



**Figure 2.16:** Depth factor  $\mu_d$  for calculating oedometer settlements (after Fox, 1948)



**Figure 2.17:** Calculating of mean vertical stress ( $\sigma_z$ ) at depth  $z$  beneath rectangular area  $a*b$  on surface loaded at uniform pressure  $q$  (Tomlinson, 1986)



**Figure 2.18:** Load distribution beneath pile group in layered soil formation

For friction piles driven into sand; the load settlement relationship of a single pile driven into coarse granular soils can be determined by pile load tests. If the settlement of the test pile is within permissible limits, the settlement of the pile group will also be within permissible limits, because the granular soil between the piles will be compacted by pile driving and the soil will be more dense and less compressible. Therefore, no settlement analysis for driven piles in sand is required. For the pile group terminating in rock, anticipated settlement is 0,01-0,05% of the group width.

## CHAPTER 3

### AN EXEMPLARY CASE HISTORY

#### **3.1. Messeturm Tower (n=64)**

The building has a basement with two underground floors, 58,8 m square in plan, and a 60-storey core shaft (41 m\* 41 m in plan) up to height of 210 m. The estimated total load of the building is 1880 MN. At the site of the Messeturm building there are gravels and sands with a thickness of 8 m, followed by Frankfurt Clay to a depth of more than 100 m below the ground surface.

In order to reduce settlements and tilt, the foundation system comprised a base slab or raft supported and stabilised against tilt by 64 large diameter bored piles. The raft is founded at a depth of 14 m below the ground surface on the Frankfurt Clay, and is 9 m below the groundwater table. The thickness of the raft decrease from 6.0 m at the centre to 3.0 m at the edges. The bored piles have a diameter of 1.3 m and are arranged in three concentric circles below the raft. The distance between the piles varies from 3,5 to 6 pile diameters. The pile length varies from 26.9 m for the 28 piles in the outer circle to 30.9 m for the 20 piles in the middle circle, and to 34.9 m for the 16 piles in the inner circle. Calculated range of settlement is 150-200 mm using different methods. (Katzenbach, R. et al., 2000, Poulos, H.G., 2000, Poulos, H.G., 2001)

### a) Settlement Ratio Method

$$n=64 \quad d=1,3 \text{ m} \quad r_0=0,65 \text{ m} \quad s=4,75 \text{ m}$$

$$P=1.880 \text{ MN} \quad L=30,9 \text{ m}$$

$$G=20+1,0z \text{ (MN/m}^2\text{)} \quad E_p=30000 \text{ MN/m}^2$$

$$v_s=0,1 \quad v_s=0,3 \quad \text{Frankfurt Clay}$$

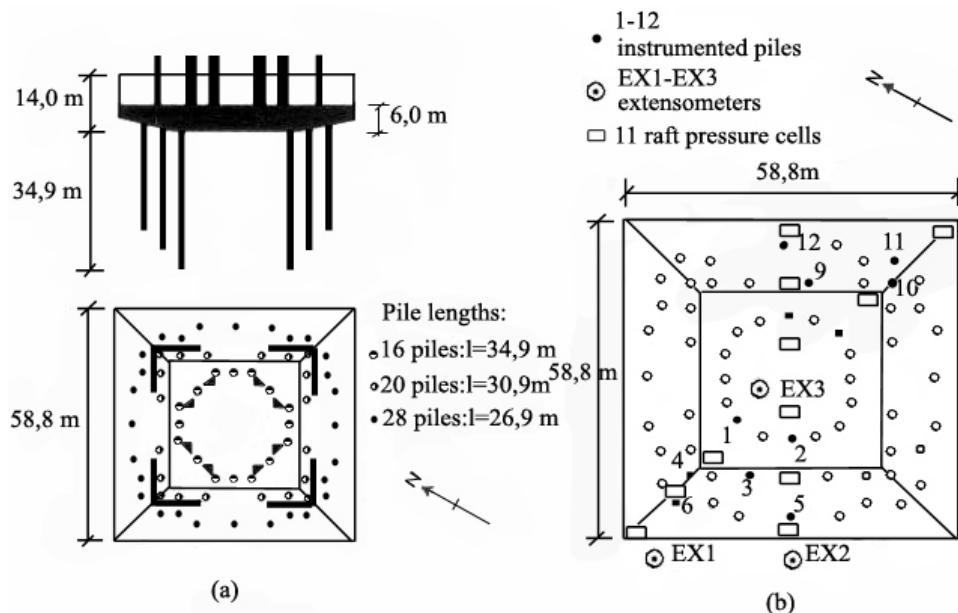
$$\lambda=E_p/G_l=30000/56,9 \approx 572,24$$

$$L/d=23,769 \rightarrow 0,54 \text{ (Fig. 2.1)}$$

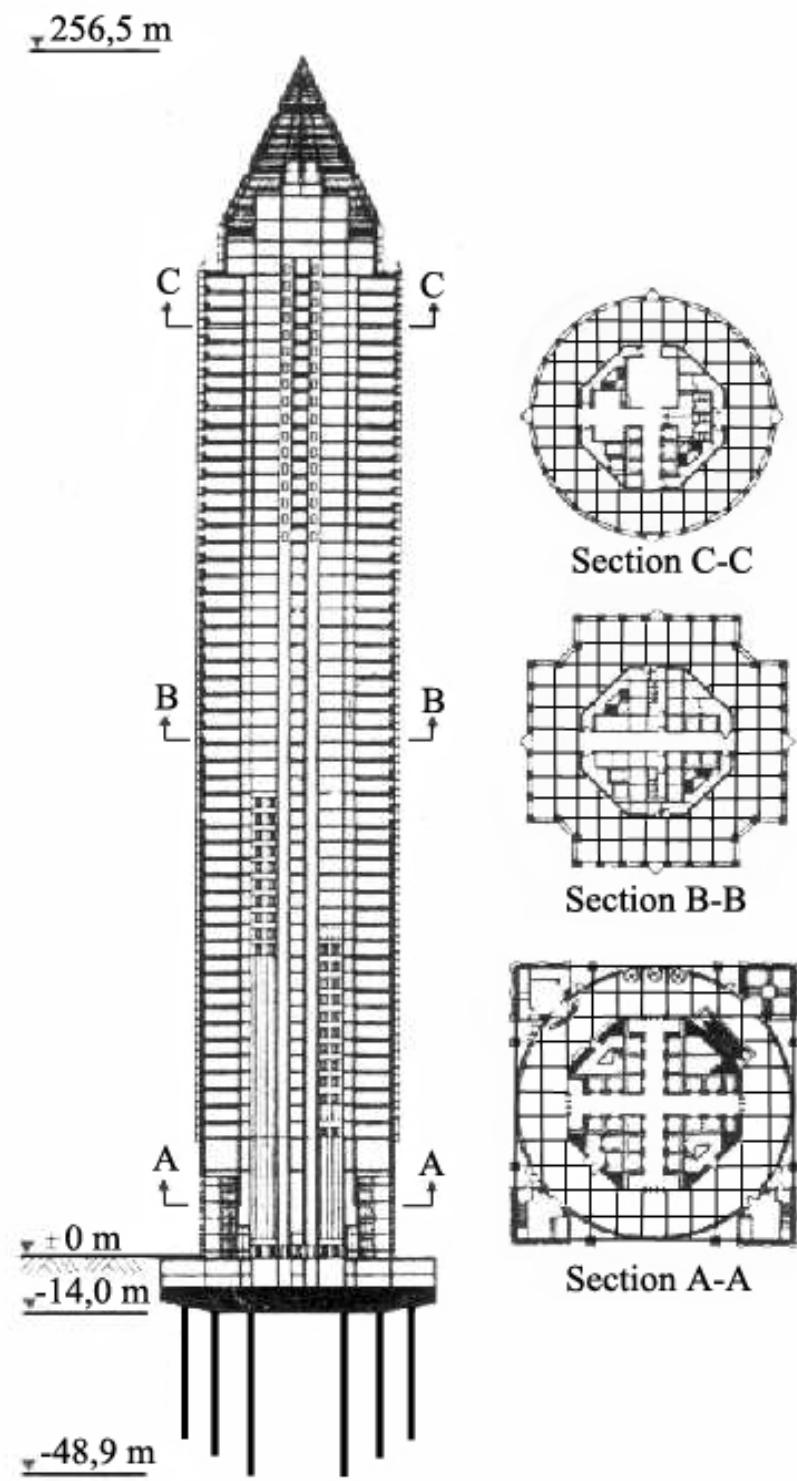
$$\rho=G_{l/2}/G_l=0,728 \rightarrow 0,99 \text{ (Fig. 2.1)}$$

$$\log \lambda=2,722 \rightarrow 0,93 \text{ (Fig. 2.1)}$$

$$s/d=4,75 \rightarrow 0,88 \text{ (Fig. 2.1)}$$



**Figure 3.1:** Piled raft foundation for Messeturm building, **(a)** plan and cross-section **(b)** location of instrumentation (Katzenbach, 2000, Poulos, 2000, Poulos, 2001)



**Figure 3.2:** Messeturm building, cross-sections (Katzenbach, 2000, Poulos, 2000, Poulos, 2001)

$v_s=0,1 \rightarrow 1,05$  (Fig. 2.1)

$v_s=0,3 \rightarrow 1$

$$\eta_w = n^{-e} \quad R_s = n^e$$

$$\zeta = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et al., 1992})$$

$$\eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 1$$

$$\mu L = (2/(\lambda \zeta))^{0.5} L/r_0$$

$$P_{\text{single}} = 1880000/64 = 29375 \text{ KN}$$

$$\delta_{\text{single}} = P_{\text{single}}/k \text{ (mm)}$$

	e	$\eta_w$	$R_s$	$\zeta$	$\mu L$	$\tan \mu L L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s=0,1$	0,459	0,147	6,756	4,356	1,403	30,022	33,309
$v_s=0,3$	0,437	0,162	6,169	4,104	1,445	29,431	34,983

	$P_t/w_t$	$K = n \eta_w k$	$\delta = P/K(\text{mm})$	$P_{\text{single}}/k$	$\delta = \delta_s R_s$
$v_s=0,1$	1231,954	11668,88	161,11	23,84	161,11
$v_s=0,3$	1293,872	13422,63	140,06	22,70	140,06

$$\delta_{\text{measured}} = 130 \text{ mm}$$

### b) Equivalent Pier Method

$$B = A_G^{0.5} = 58,8 \text{ m}$$

$$A_p = \pi d^2 n / 4 = 84,9487 \text{ m}^2$$

$$E_p = 30000 \text{ MPa}$$

$$E_s' = 125,18 \text{ MPa} \quad E_u = 170,7 \text{ MPa}$$

$$d_e = 1,27 \text{ A}_G^{0,5} = 74,676 \text{ (for friction piles)}$$

$$\rho = 0,728 \quad L = 30,9 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\lambda = E_e / G_l = 859,199 / 56,9 \approx 15,10$$

$$\zeta_1 = \ln(2,5 \rho (1-v) L / r_0) \text{ (W. Fleming, et al., 1992)}$$

$$\zeta_2 = \ln / \{ 5 + [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L / r_0 \} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s = 0,1$	859,199	15,100	0,304	0,545	0,377	0,298	60,08
			1,849	0,221	0,407	0,733	147,43
$v_s = 0,3$	881,4	15,49	0,053	1,285	0,276	0,104	17,80
			1,800	0,221	0,407	0,732	124,55

### Method 2

$$L/d_e = 30,9 / 74,676 = 0,413 \rightarrow I_\delta = 0,5 \text{ (Fig. 2.10)}$$

$\delta$ (mm)	$v_s = 0,1$	$v_s = 0,3$
	100,55	85,08

$$K \approx 200 \text{ (pile stiffness factor)} \quad s/d \approx 4,75 \quad L/d \approx 23,769 \quad B = 58,8 \text{ m}$$

$$d_e/B \approx 0,77 \text{ assumed, then } d_e \approx 45,276 \text{ m (Fig. 2.9)}$$

## Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,1$	859,199	15,100	0,805	0,553	0,620	0,427	141,70
			1,979	0,353	0,655	0,660	219,20
$v_s=0,3$	881,4	15,49	0,554	0,659	0,598	0,380	106,69
			1,908	0,355	0,655	0,677	190,12

## Method 2

$$L/d_e = 30,9/45,276 = 0,68 \rightarrow I_\delta = 0,47 \text{ (Fig. 2.10)}$$

$\delta$ (mm)	$v_s=0,1$	$v_s=0,3$
	155,90	131,91

$$\delta_{\text{measured}} = 130 \text{ mm}$$

## c) Equivalent Raft Method

L	B	H	L/B	H/B	D/B
62	62	40	1	0,645	0,558
82	82	40	1	0,487	0,909

$$P = 1880000 \text{ KN} \quad v_s = 0,1 \quad v_u = 0,5$$

$$\delta_{\text{ave}} = \mu_1 \mu_0 q_n B / E_u$$

$\mu_1, \mu_0 \rightarrow \text{Fig. 2.14}$

$\mu_0$	$\mu_1$	$E_{\text{uave}}$	q	$\delta_i$
0,93	0,23	199,8	489,07	32,46
0,92	0,18	320,4	279,59	11,84

$$\delta_{i\ ave} = 44,31 \text{ mm}$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)]$$

$$D/(LB)^{0,5} = 0,558 \rightarrow \mu_d = 0,83 \text{ (Fig. 2.16)}$$

$$\text{Frankfurt Clay} \rightarrow \mu_g = 0,7 \text{ (Table 2.4)}$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g$$

$E_{mid-dr}$	$m_v$	$\sigma_z$	$\delta_c$
146,52	0,0066	322,78	50,06
234,96	0,0041	134,49	13,00

$$\delta_c = 63,06 \text{ mm}$$

$$\delta_T = \delta_{i\ ave} + \delta_c = 107,38 \text{ mm}$$

$$\delta_{measured} = 130 \text{ mm}$$

Two different values were used for Poisson's ratio in the calculations. These were advised as upper and lower values for the soil. Results which were obtained by using lower Poisson's ratio were used in the graphs.

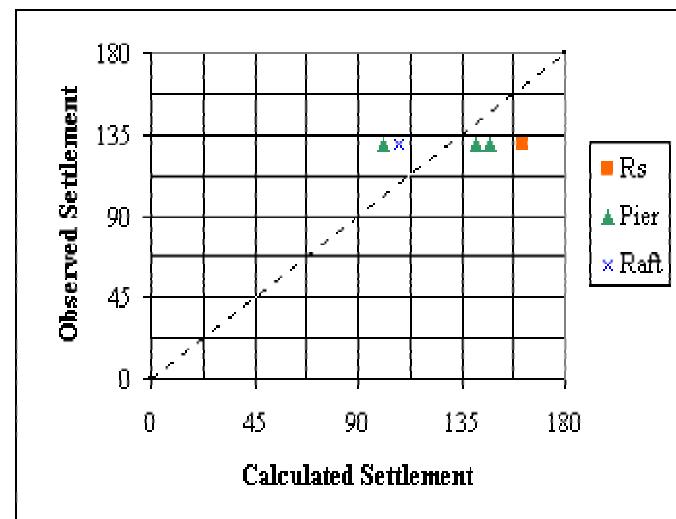
If  $L/r_e$  was greater than 1 results which were obtained from  $d_{e1}$  formulations (I (Fig. 2.10) and I (equation 2.16-A=0) were used in the graphs for equivalent pier method. If  $L/r_e$  was less than 1 then results which were obtained from formulations  $d_{e1}$  (I (Fig. 2.10) and I (equation 2.16-A=5) and  $d_{e2}$  (I (equation 2.16-A=0) were used in the graphs. For end bearing piles results for  $d_{e2}$  (I (equation 2.16-A=5) were used.

Calculations were made for different pressure distributions and compressible layer thickness (H) values for equivalent raft method. For graphs  $\frac{1}{4}$  pressure distribution and  $H=2B$  ( $B$ :width of equivalent raft) results were used.

**Table 3.1:** Measured and computed settlements for Messeturm Building (mm)

Settlement (mm)										
Set. Ratio	Equivalent Pier				Equivalent Raft				Mea.	
	d <sub>e1</sub>		d <sub>e2</sub>		H=80 m	H=71 m (at the tip)	H=80 m (1/6)	H=80 m (1/8)		
	Met1	Met2	Met1	Met2	Ave.	Ave.	Ave.	Ave.		
vs=0,1	161,11	60,08	100,55	141,7	155,9	107,38	113,75	115,21	120,88	130
		147,43		219,2						
vs=0,3	140,06	17,8	85,08	106,69	131,91	84,85	90,75	91,24	95,91	
		124,55		190,12						

Messe Turn		
Rs	161,11	Mea.
Pier	147,43	
	100,55	
	141,70	
Raft	107,38	



**Figure 3.3:** Measured and computed settlements for Messeturn Building (mm)

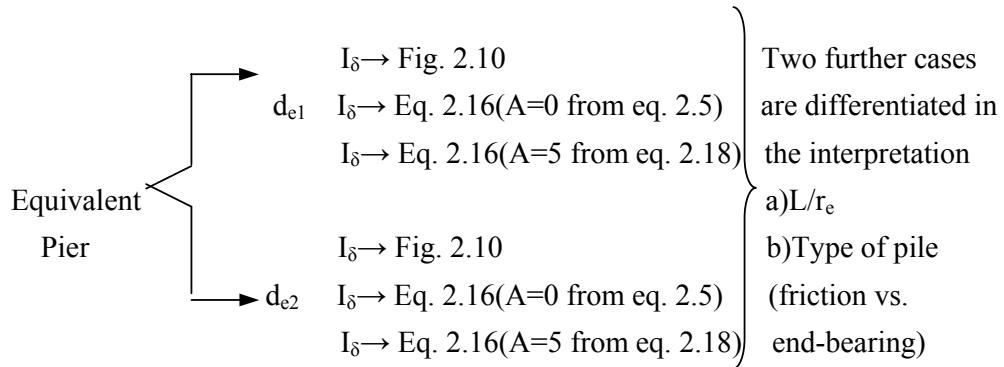
## **CHAPTER 4**

### **SUMMARY AND CONCLUSION**

The conclusions reached are enumerated below, but an explanatory introduction may be needed. The calculation methods have been summarized in some detail in Chapter 2. It is possible to calculate different settlement values by the equivalent pier method depending on the selection of displacement influence factor  $I_\delta$  and equivalent diameter  $d_e$ .  $I_\delta$  is either selected based on equation 2.16 (Method 1), or using Fig.2.10 (Method 2). Also two different equivalent pier diameters are obtained by using equations 2.13, 2.14 ( $d_{e1}$ ) and Figure 2.9 ( $d_{e2}$ ).  $\zeta$ , measure of radius of influence of pile, which is used in equation 2.16 to obtain  $I_\delta$ , can be calculated by equation 2.5 (inferred  $A=0$ ) and equation 2.18 ( $A=5$ ). As it is recalled coefficient  $A$  is an empirical coefficient. As a result there are three displacement influence factors  $I_\delta$  can be obtained for each equivalent pier diameter by using Figure 2.10 and equation 2.16 with equations 2.5 and 2.18 ( $A=0$ ,  $A=5$ ). Also  $L/r_e$  and type of the pile (friction vs. end -bearing) are the additional factors to be considered in the interpretation. Fig. 4.1 summarizes the types of solutions.

Total settlements by equivalent raft method are obtained by adding initial settlements and consolidation settlements. Average consolidation settlements are

estimated by the conventional procedure and the initial average settlements are estimated by Christian and Carrier (1978) for constant  $E_u$ .



**Figure 4.1:** Equivalent Pier Method - Summary variations in the calculation procedures.

A flow chart is provided in Fig. 4.2 to make an easier selection of the proper method for a case

1. In general settlement ratio method gives overestimated settlement values (Fig. 4.3 and Fig. 4.4).
2. It is not possible to get reasonable results by using settlement ratio method if number of piles is less than 16, (Table 4.3). For small pile groups, equivalent raft method gives better predictions (9-pile group, Test of Kaino). It may be possible to get an idea for small groups by using equivalent pier method.

3. It is proposed that a relationship can be described between settlements calculated by the settlement ratio method and p values (Figures 4.6 – 4.7) where

$$p = \frac{P_{\text{Total}} (\text{kN})}{1000 (\text{kN}) \cdot e} \quad \dots(4.1)$$

e: Efficiency exponent

$P_{\text{Total}}$ : Total load (kN)

p: Dimensionless parameter

It is observed that settlement ratio method gives better correlations when p is greater than 50 and less than 1000 (Fig. 4.6).

4. It is observed that the settlement ratio method is not suitable when the shape of the piled rafts is not regular and when the raft area is larger than plan area of pile group (Pollux, Kastor, etc.) (Fig. 4.5). For such pile groups, equivalent raft method gives better results.

5. Equivalent pier diameter from Fig. 2.9 ( $d_{e2}$ ) is always lower than  $d_{e1}$  from equation 2.13, 2.14. Therefore higher settlement values are calculated by using  $d_{e2}$ .

6. If  $L/r_e$  is less than 1,  $I_\delta$ , from Fig 2.10 for  $d_{e1}$  gives the best results (Fig. 4.8). Another alternative is to obtain  $I_\delta$  from equation 2.16 ( $A=0$  from 2.18) for  $d_{e2}$  (Fig. 4.9) and this correlation is not as good as the former.

7. For friction piles, when  $L/r_e$  is greater than 1,  $d_{el}$  formulation should be used. Reasonable results can be calculated by using  $I_\delta$ , from equation 2.16 with  $A=0$  and, from Fig. 2.10 (Figures 4.10 –4.11).

8. As it is seen in Figures 4.12 and 4.13 that for end-bearing piles, using  $d_{e2}$  formulation and  $I_\delta$  (equ. 2.16) with equation 2.18 ( $A=5$ ) is the only way to get reasonable results. The rest of the equivalent pier procedures give underestimated settlement values.

9. When a rock layer exists at the pile tip (Commerz Bank, Main Tower, Japan Centre) very high settlement values are calculated by the settlement ratio method (Table 4.3). On the other hand for the same situation, equivalent raft method tends to give underestimated results (Table 4.9).

10. It is observed that when  $L/r_e$  is greater than 5, equivalent pier method does not give reasonable results (Test of Kaino, Field test on five pile group, Frame type building 2-3-7).

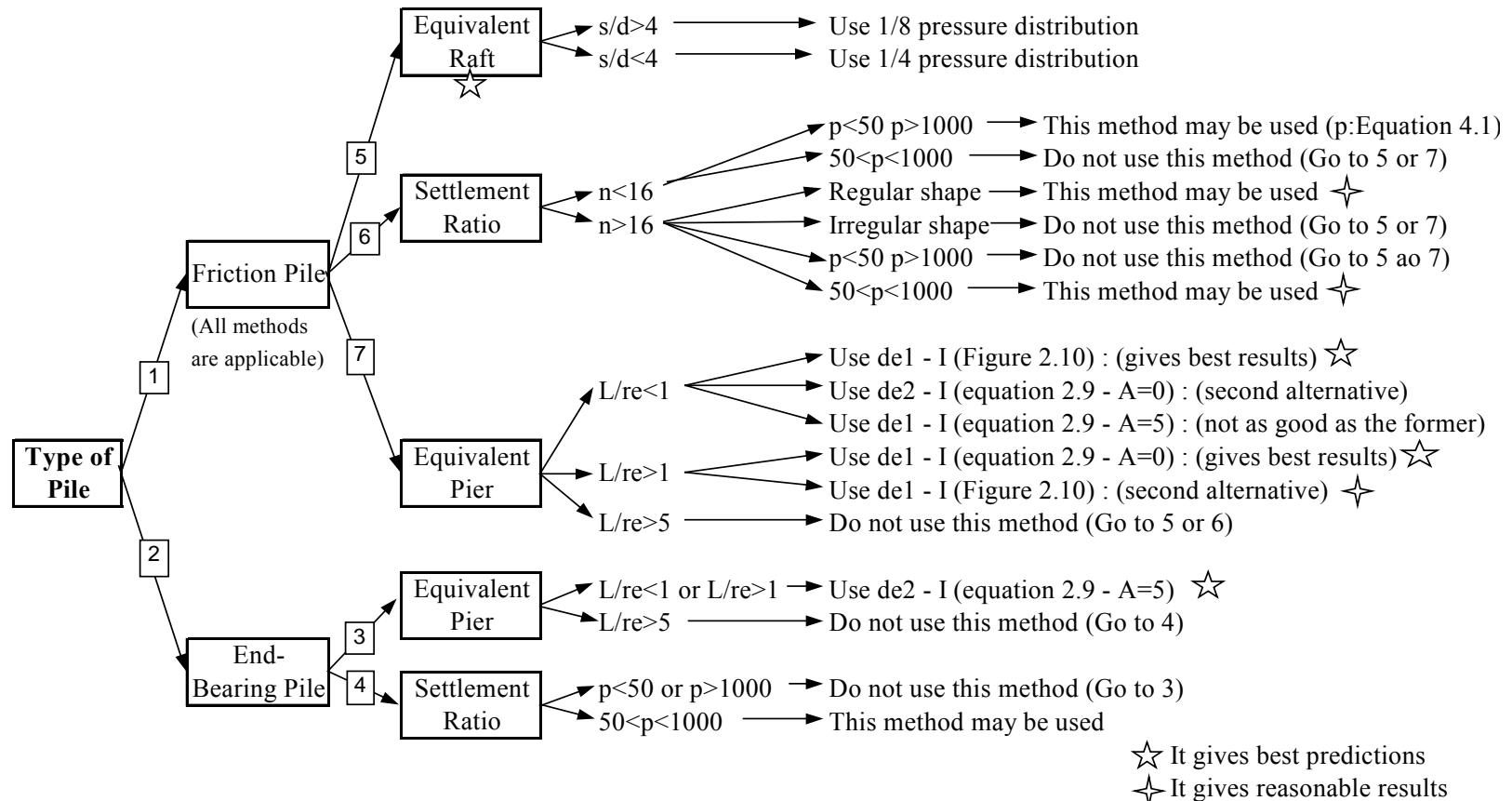
11. In general, the best correlations between calculated and observed settlements are obtained from the equivalent raft method (Fig. 4.14). Correlations for friction piles are better than those of end-bearing piles (Fig. 4.15-4.16).

12. It can be seen from Fig 4.17 that  $s/d$  is one of the important parameters for equivalent raft method. Calculated settlement values increase as  $s/d$  decreases for friction piles (Fig. 4.17).

13. If  $s/d$  greater is than 4 and either  $L_{pile}$  is greater than 25 m or  $B_{raft/L}$  pile is less than 1.2 then equivalent raft can be best assumed using 8V:1H pressure distribution (Fig. 4.18).

14. It is considered that practically consolidation settlement does not exist under lightly loaded small pile groups in sandy soils. Time dependent settlements are observed under heavily loaded large groups in sandy soils. Therefore settlement calculations for large groups may be performed like in clayey soils by equivalent raft method (Test of Kaino, Five Storey Building, 19-Storey, Hotel Japan, Treptowers).

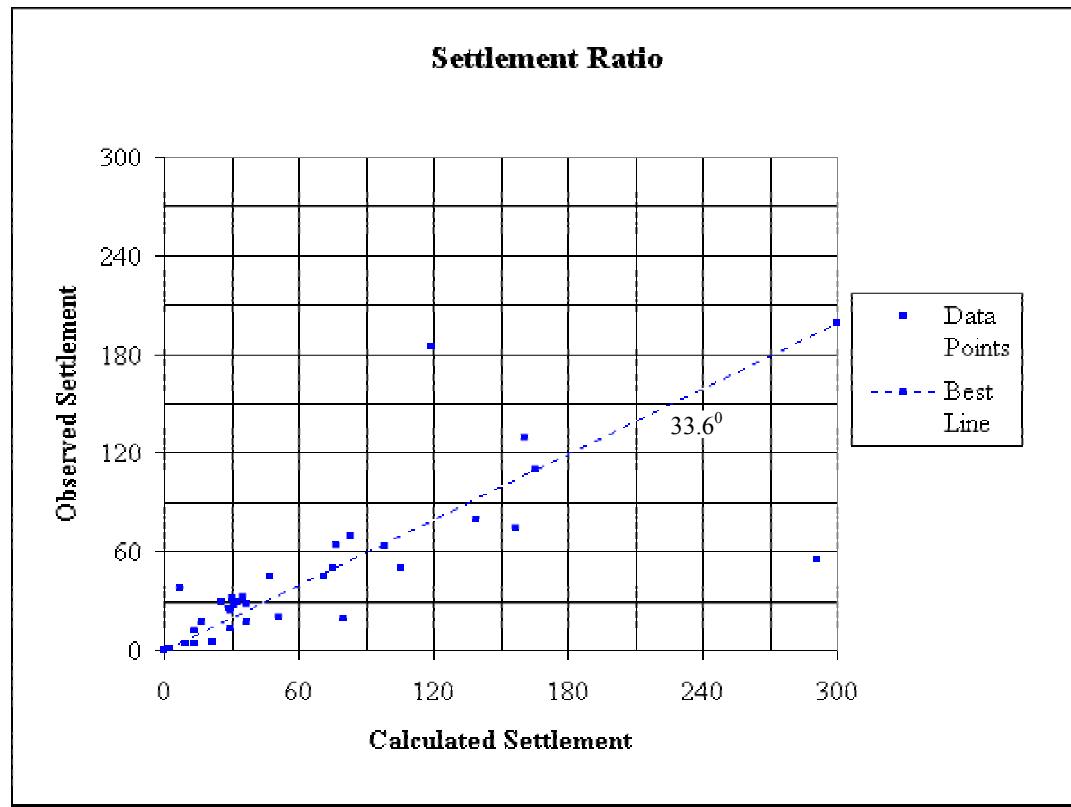
Results obtained from all the methods are presented together as best lines for friction and end-bearing piles in Figs. 4.19 and 4.20 respectively.



**Figure 4.2:** Selection of the proper method presented by a flow chart

**Table 4.1:** Calculated and observed settlement values for settlement ratio method (mm)

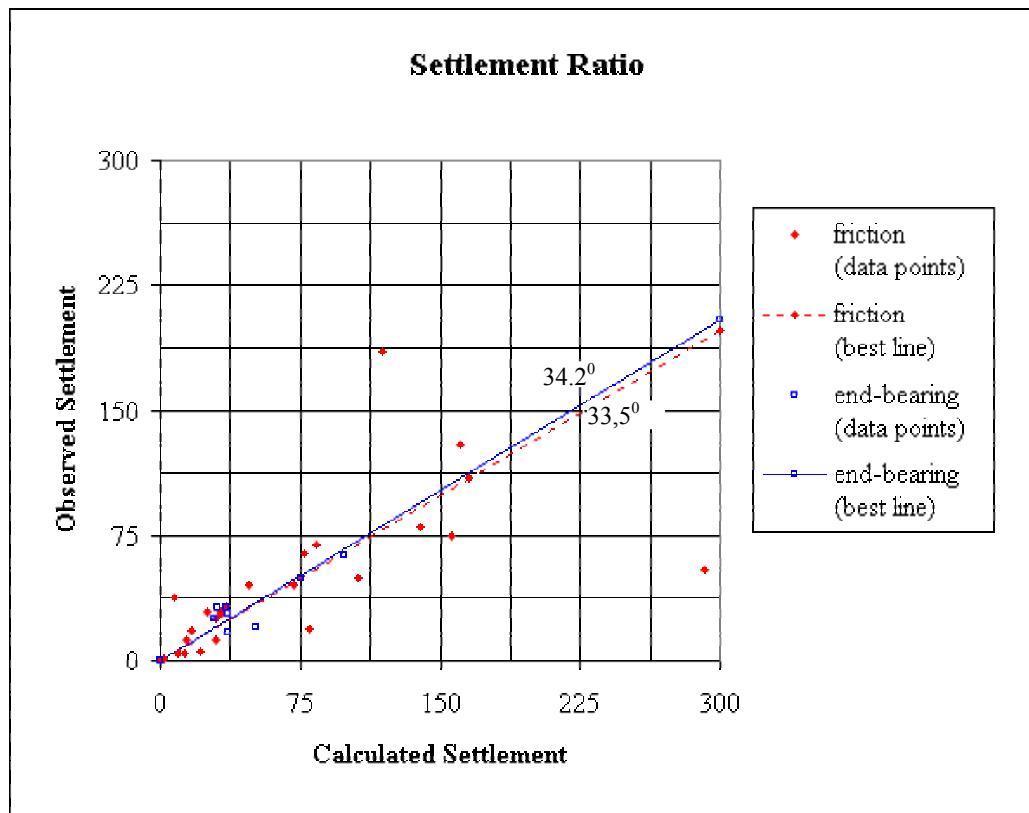
Settlement Ratio	Cal.	Mea.	(Cal.-Mea.) / Mea.*100		Cal.	Mea.	(Cal.-Mea.) / Mea.*100
1 Field Test	7,59	38,1	80,08	17 Molasses Tank	25,34	29,5	14,10
2 Test of Kaino	9,48	3,8	149,47	18 Messeeturm	161,11	130	23,93
3 Frame-type 2	29,61	13	127,77	19 New Court II	30,56	31,5	2,98
4 Frame-type 3	21,58	5	331,60	20 New Court I	36,67	28,1	30,50
5 9-Pile group	2,3	0,9	155,56	21 New Court III	29,09	25,1	15,90
6 Frame-type 7	13,26	4	231,50	22 Congress Office	71,46	45	58,80
7 Five-storey	13,7	12,65	8,30	23 Congress Hotel	105,45	50	110,90
8 Eurotheum	35,05	32	9,53	24 Commerz Bank	36,41	17	114,18
9 Japan Centre	74,89	50	49,78	25 Main Tower	51,1	20	155,50
10 Forum Kastor	156,40	75	108,53	26 Cambridge Road	31,42	27,5	14,25
11 Forum Pollux	139,59	80	74,49	27 19-Storey	77,12	64	20,50
12 American Express	291,4	55	429,87	28 Hotel Japan	17,14	17,5	2,06
13 Westend I Tower	165,7	110	50,66	29 İzmir Hilton	83,3	69,6	19,68
14 Messe-Torhaus	47,48	45	5,51	30 Frame-type 6	79,69	19	319,42
15 Gratham Road	32,84	30	9,47	31 Stonebridge	29,34	25	17,36
16 Treptowers	98,4	63	56,19	32 Dashwood	35,29	33	6,94
				33 Ghent Grain	119,14	185	35,60



**Figure 4.3:** Calculated and observed settlement values for all cases (mm)

**Table 4.2:** Calculated and observed settlement values for friction and end-bearing piles  
settlement ratio method (mm)

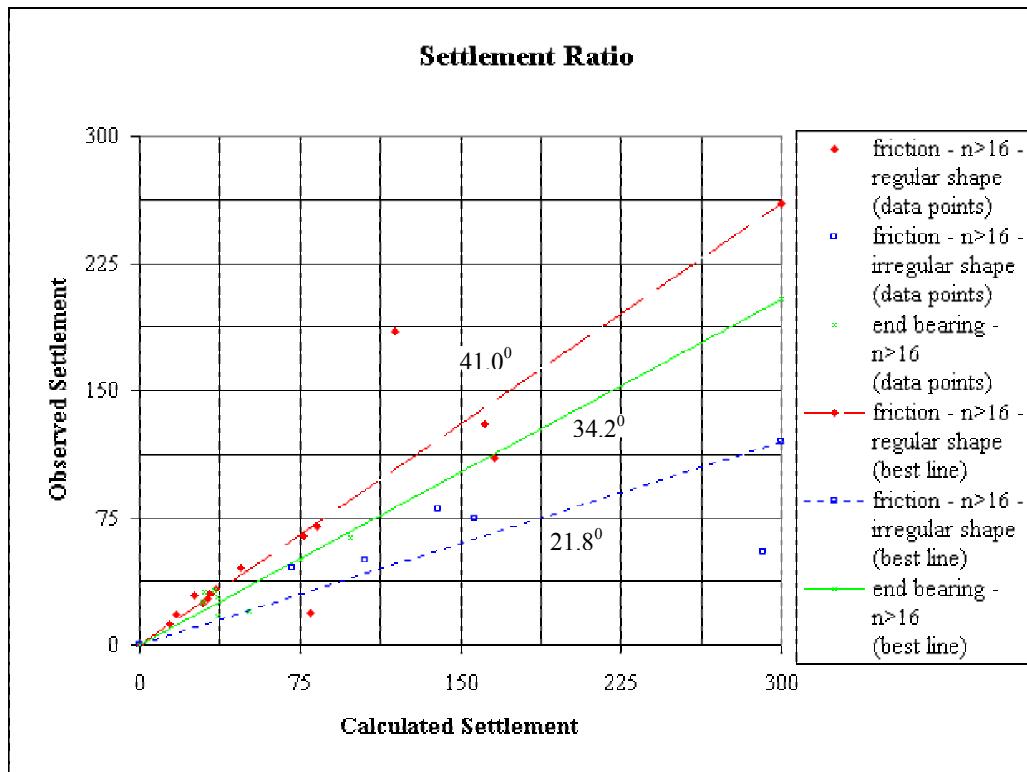
	<b>Friction Piles</b>	<b>Cal.</b>	<b>Mea.</b>		<b>Cal.</b>	<b>Mea.</b>
1	Field Test	7,59	38,1	14	Molasses Tank	25,34
2	Test of Kaino	9,48	3,8	15	Messteturm	161,11
3	Frame-type 2	29,61	13	16	Congress Office	71,46
4	Frame-type 3	21,58	5	17	Congress Hotel	105,45
5	9-Pile group	2,3	0,9	18	Cambridge Road	31,42
6	Frame-type 7	13,26	4	19	19-Storey	77,12
7	Five-storey	13,7	12,65	20	Hotel Japan	17,14
8	Forum Kastor	156,40	75	21	İzmir Hilton	83,3
9	Forum Pollux	139,59	80	22	Frame-type 6	79,69
10	American Express	291,43	55	23	Stonebridge	29,34
11	Westend I Tower	165,73	110	24	Dashwood	35,29
12	Messe-Torhaus	47,48	45	25	Ghent Grain	119,14
13	Gratham Road	32,84	30			185
	<b>End-Bearing Piles</b>					
1	Eurotheum	35,05	32	5	New Court I	36,67
2	Japan Centre	74,89	50	6	New Court III	29,09
3	Treptowers	98,4	63	7	Commerz Bank	36,41
4	New Court II	30,56	31,5	8	Main Tower	51,1



**Figure 4.4:** Calculated and observed settlement values for friction and end-bearing piles (mm)

**Table 4.3:** Calculated and observed settlement values for friction piles (n>16, n<16, regular, irregular shapes), end-bearing piles (n>16) -settlement ratio method (mm)  
 (A,C:regular shapes; B:irregular shapes)

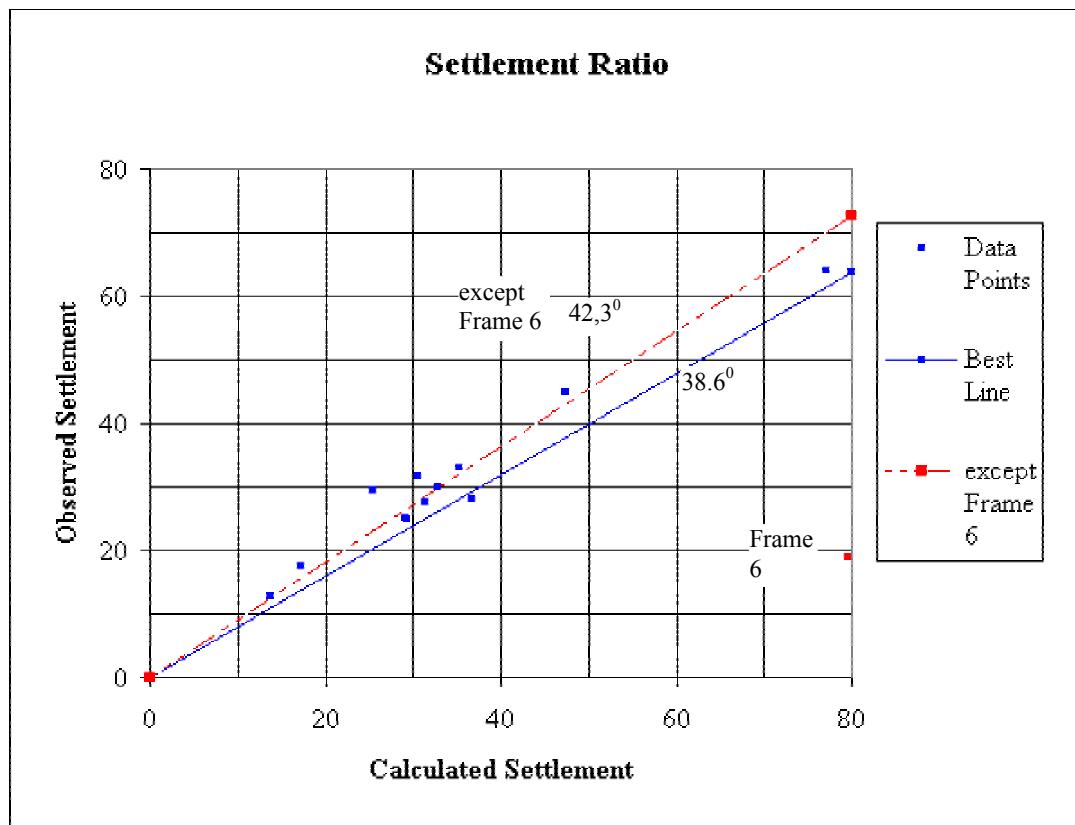
<b>A Friction piles</b>		<b>Cal.</b>	<b>Mea.</b>	(n>16)	<b>B Friction piles</b>		<b>Cal.</b>	<b>Mea.</b>	(n>16)
1	Five-storey B.	13,7	12,65	20	1	Forum Kastor	156,40	75	22
2	Westend I Tower	165,73	110	40	2	Forum Pollux	139,59	80	26
3	Messe-Torhaus	47,48	45	42	3	American Exp.	291,43	55	35
4	Gratham Road	32,84	30	48	4	Congress Office	71,46	45	43
5	Molasses Tank	25,34	29,5	55	5	Congress Hotel	105,45	50	98
<b>End-bearing</b>									
6	Meseturm Tower	161,11	130	64	<b>D piles</b>		(n>16)		n
7	Cambridge Road	31,42	27,5	116	1	Eurotheum	35,05	32	25
8	19-Storey B.	77,12	64	132	2	Treptowers	98,4	63	54
9	Hotel Japan	17,14	17,5	157	3	New Court II	30,56	31,5	77
10	İzmir Hilton	83,3	69,6	189	4	New Court I	36,67	28,1	82
11	Frame-type 6	79,69	19	192	5	New Court III	29,09	25,1	82
12	Stonebridge Park	29,34	25	351	6	Japan Centre	<b>74,89</b>	<b>50</b>	25
13	Dashwood House	35,29	33	462	7	Commerz Bank	<b>36,41</b>	<b>17</b>	111
14	Ghent Grain	119,14	185	697	8	Main Tower	<b>51,1</b>	<b>20</b>	112
<b>C Friction piles</b>				(n<16)					
1	Field Test	7,59	38,1	5	4	Frame-type 3	21,58	5	9
2	Test of Kaino	9,48	3,8	5	5	9-Pile group	2,3	0,9	9
3	Frame-type 2	29,61	13	6	6	Frame-type 7	13,26	4	16



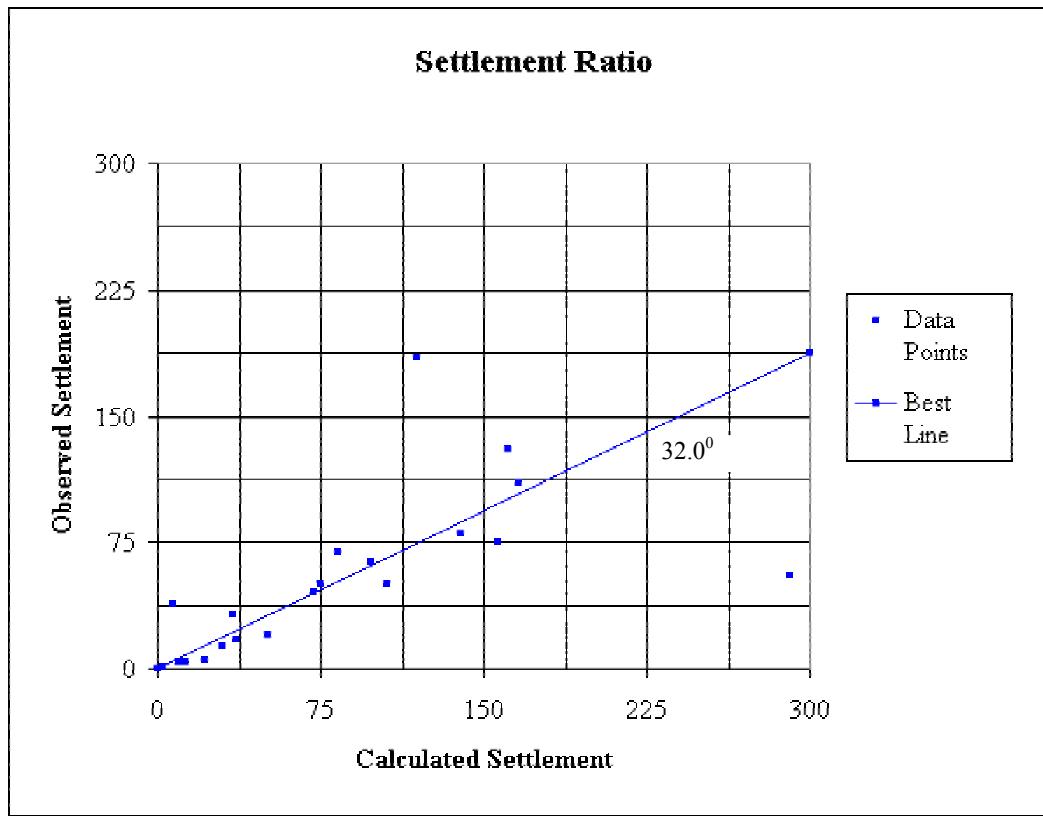
**Figure 4.5:** Calculated and observed settlement values for friction piles ( $n > 16$ , regular, irregular shapes), end-bearing piles ( $n > 16$ ) (mm)

**Table 4.4:** Calculated and observed settlement values ( $50 < p < 1000$ ,  $p < 50$   $p > 1000$ )-settlement ratio met. (mm)

	<b>Cal.</b>	<b>Mea.</b>	<b>50&lt; p &lt; 1000</b>		<b>Cal.</b>	<b>Mea.</b>	<b>p &lt; 50 p &gt; 1000</b>
1 Five-storey B.	13,7	12,65	53,23	1 Field Test	7,59	38,1	5,04
2 Messe-Torhaus	47,48	45	336,9	2 Test of Kaino	9,48	3,8	12,31
3 Gratham Road	32,84	30	185,8	3 Frame-type 2	29,61	13	22,43
4 Molasses Tank	25,34	29,5	59,6	4 Frame-type 3	21,58	5	12,74
5 New Law II	30,56	31,5	769,8	5 9-Pile group	2,3	0,9	4
6 New Law I	36,67	28,1	951,2	6 Frame-type 7	13,26	4	28,58
7 New Law III	29,09	25,1	702,1	7 Eurotheum	35,05	32	1141
8 Cambridge	31,42	27,5	239,3	8 Japan Centre	74,89	50	2215
9 19-Storey B.	77,12	64	392,6	9 Forum Kastor	156,40	75	1991
10 Hotel Japan	17,14	17,5	371,2	10 Forum Pollux	139,59	80	2167
11 Frame-type 6	79,69	19	491,7	11 American Express	291,43	55	2141
12 Stonebridge	29,34	25	297	12 Westend I Tower	165,73	110	3107
13 Dashwood	35,29	33	516,4	13 Treptowers	98,4	63	1474
				14 Messeturm Tower	161,11	4092	130
				15 Congress Office	71,46	1162	45
				16 Congress Hotel	105,45	2648	50
				17 Commerz Bank	36,41	2645	17
				18 Main Tower	51,1	4201	20
				19 Izmir Hilton	83,3	1549	69,6
				20 Ghent Grain	119,14	1868	185



**Figure 4.6:** Calculated and observed settlement values ( $50 \leq p \leq 1000$ ) (mm)



**Figure 4.7:** Calculated and observed settlement values ( $p>1000$  or  $p<50$ ) (mm)

**Table 4.5:** Calculated and observed settlement values for equivalent pier method (friction piles L/re<1) (mm)

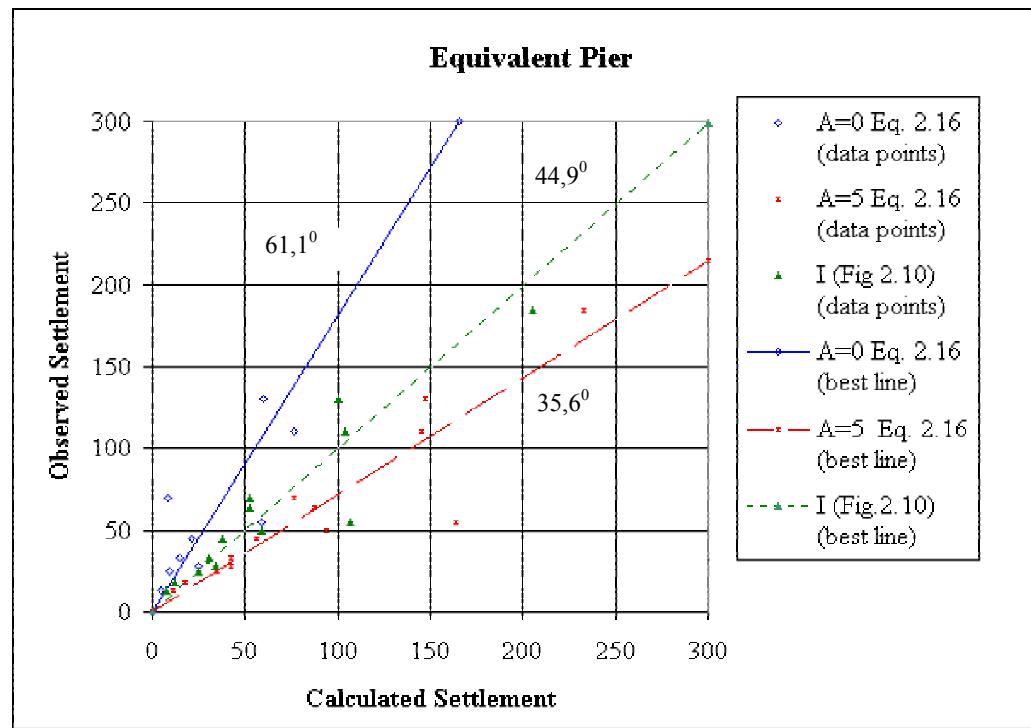
	Friction Piles (L/r <sub>e</sub> <1)			Equivalent Pier			Mea.			(Cal-Mea.)/Mea*100				
	d <sub>e1</sub> (Equation 2.13-14)			d <sub>e2</sub> (Figure 2.9)			d <sub>e1</sub>			d <sub>e2</sub>				
	A=0	A=5	I (Fig. 2.10)	A=0	A=5	I (Fig. 2.10)	A=0	A=5	I (Fig. 2.10)	A=0	A=5	I (Fig. 2.10)		
1 Five-storey B.	4,94	10,84	7,78	10,55	15,89	11,4	12,65	60,9	14,3	38,5	16,6	25,6	9,9	
2 American Exp.	59,2	163,7	107,1	148,1	240,2	169,95	55	7,6	197,7	94,6	169,3	336,7	209,0	
3 Westend I T.	76,21	145,4	103,6	149	213,1	148,42	110	30,7	32,1	5,8	35,4	93,7	34,9	
4 Messeturm T.	60,08	147,4	100,6	141,7	219,2	155,9	130	53,8	13,4	22,7	9,0	68,6	19,9	
5 Congress O.	21,60	56,58	38,13	55,65	86,22	61,98	45	52,0	25,7	15,3	23,7	91,6	37,7	
6 Congress H.		93,46	58,89	68,42	143,59	99,72	50		86,9	17,8	36,8	187,2	99,4	
7 Cambridge R.	24,89	42,42	34,24	42,7	58,88	47,95	27,5	9,5	54,3	24,5	55,3	114,1	74,4	
8 19-Storey B.		87,69	52,03		134	82,59	64		37,0	18,7		109,3	29,0	
9 Hotel Japan			17,05	11,51		23,08	16,61	17,5		2,6	34,2		31,9	5,1
10 İzmir Hilton	8,71	76,29	52,39	57,31	109,1	78,19	69,6	87,5	9,6	24,7	17,7	56,8	12,3	
11 Stonebridge P.	9,47	35,18	24,44	28,21	49,52	38,8	25	62,1	40,7	2,2	12,8	98,1	55,2	
12 Dashwood H.	14,79	42,47	30,6	35,59	59,39	48,58	33	55,2	28,7	7,3	7,8	80,0	47,2	
13 Ghent Grain		232,6	205,2	176,5	271	235,37	185		25,7	10,9	4,6	46,5	27,2	

**Table 4.6:** Calculated and observed settlement values for friction piles ( $L/re > 1$ ) - equivalent pier method (mm)

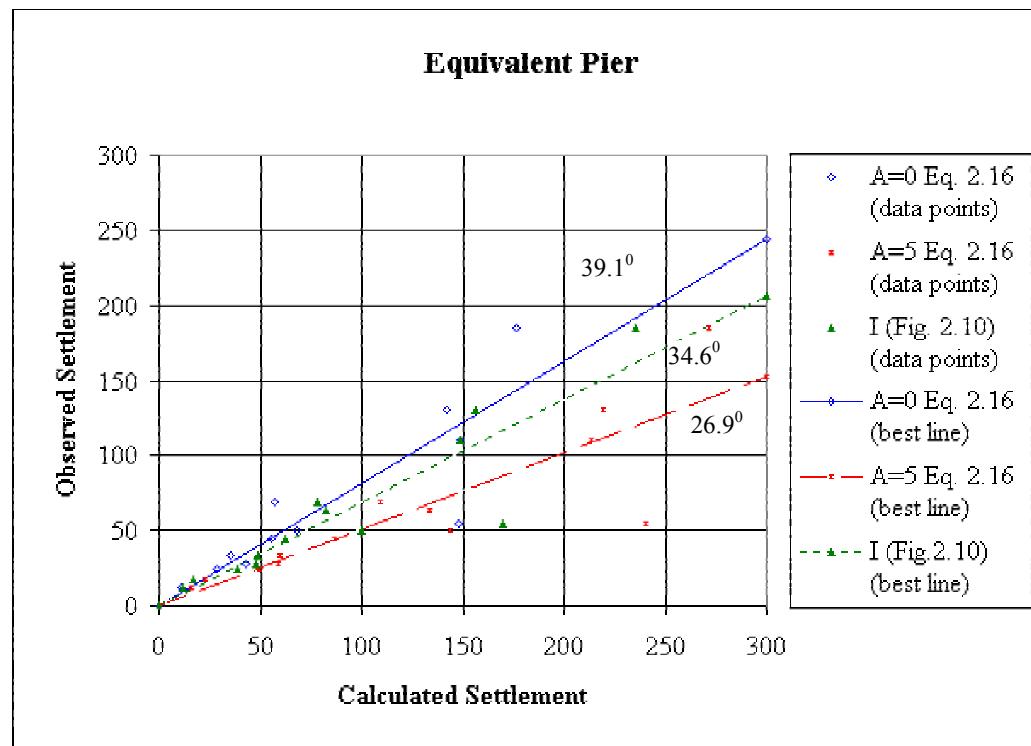
	Friction Piles	Equivalent Pier						Mea.			(Cal-Mea.)/Mea*100					
		d <sub>e1</sub> (Equation 2.13-2.14)			d <sub>e2</sub> (Fig. 2.9)			d <sub>e1</sub>			d <sub>e2</sub>					
		A=0	A=5	I (Fig. 2.10)	A=0	A=5	I (Fig. 2.10)	A=0	A=5	I (Fig. 2.10)	A=0	A=5	I (Fig. 2.10)			
1	Field Test	6,01	6,53	4,28	8,94	9,36	6,71	38,1	84,2	82,9	88,8	76,5	75,4	82,4		
2	Test of Kaino	8,01	9,01	6,83	9,71	10,59	8,26	3,8	110,8	137,1	79,7	155,5	178,7	117,4		
3	Frame-type 2	27,02	29,38	28,99	31,91	33,9	34,05	13	107,8	126,0	123,0	145,5	160,8	161,9		
4	Frame-type 3	17,56	18,71	17,58	22,4	23,3	24,86	5	251,2	274,2	251,6	348,0	366,0	397,2		
5	9-Pile group	1,44	1,55	0,68	2,58	2,71	1,04	0,9	60,0	72,2	24,4	186,7	201,1	15,6		
6	Frame-type 7	11,01	11,98	9,53	15,33	16,13	13,11	4	175,3	199,5	138,3	283,3	303,3	227,8		
7	Forum Kastor	64,64	121,15	84,17	126,00	176,22	124,95	75	13,8	61,5	12,2	68,0	135,0	66,6		
8	Forum Pollux	77,67	123,17	88,09	141,03	180,96	125,88	80	2,9	54,0	10,1	76,3	126,2	57,4		
9	Messe-Torhaus	30,7	45,61	36,71	47,68	61,61	45,91	45	31,8	1,4	18,4	6,0	36,9	2,0		
10	Gratham Road	22,5	36,99	30,5	35,19	48,74	42,42	30	25,0	23,3	1,7	17,3	62,5	41,4		
11	Molasses Tank	19,27	24,24	14,91	57,82	61,68	27,39	29,5	34,7	17,8	49,5	96,0	109,1	7,2		
12	Frame-type 6	63,31	86,17	76,17	97,59	118,45	97,77	19	233,2	353,5	300,9	413,6	523,4	414,6		

**Table 4.7:** Calculated and observed settlement values for end-bearing piles - equivalent pier method (mm)

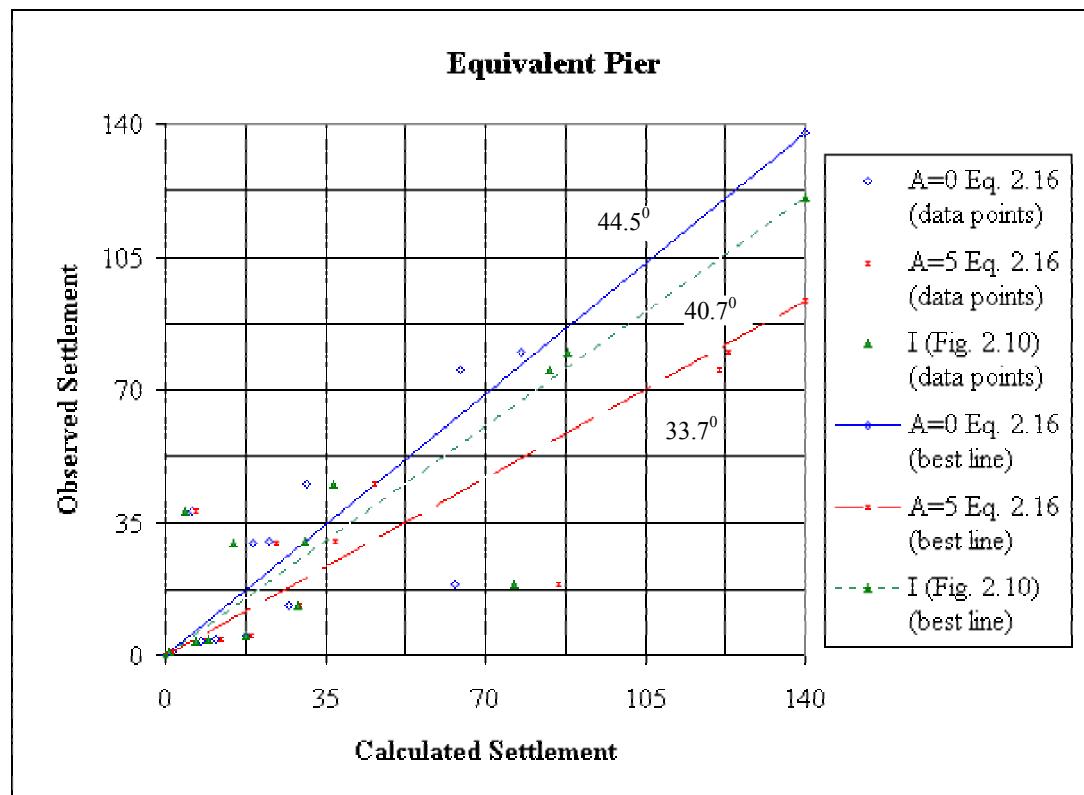
	End-Bearing Piles			Equivalent Pier			Mea.			(Cal-Mea.)/Mea*100		
	d <sub>e1</sub> (Equation 2.13-2.14)			d <sub>e2</sub> (Fig. 2.9)			Mea.			d <sub>e1</sub>		
	A=0	A=5	I (Fig. 2.10)	A=0	A=5	I (Fig. 2.10)	A=0	A=5	I (Fig. 2.10)	A=0	A=5	I (Fig. 2.10)
1 Eurotheum B.	10,42	3,88		20,46	6,75	32	67,4	87,9		36,1	78,9	
2 Japan Centre	22,24	5,52		47,51	10,39	50	55,5	89,0		5,0	79,2	
3 Treptowers B.	57,27	49,22		80,95	66,02	63	9,1	21,9		28,5	4,8	
4 New Court I	7,91	21,29	20,55	16,17	27,91	26,43	31,5	74,9	32,4	34,8	48,7	11,4
5 New Court II	8,99	26,02	25,39	19,24	33,95	32,66	28,1	68,0	7,4	9,6	31,5	20,8
6 New Court III	2,84	19,61	18,3	12,76	25,87	24,1	25,1	88,7	21,9	27,1	49,2	3,1
7 Commerz Bank		7,49	5,29		14,44	9,33	17		55,9	68,9		15,1
8 Main Tower		10,37	4,53		20,08	7,3	20		48,2	77,4		0,4
												63,5



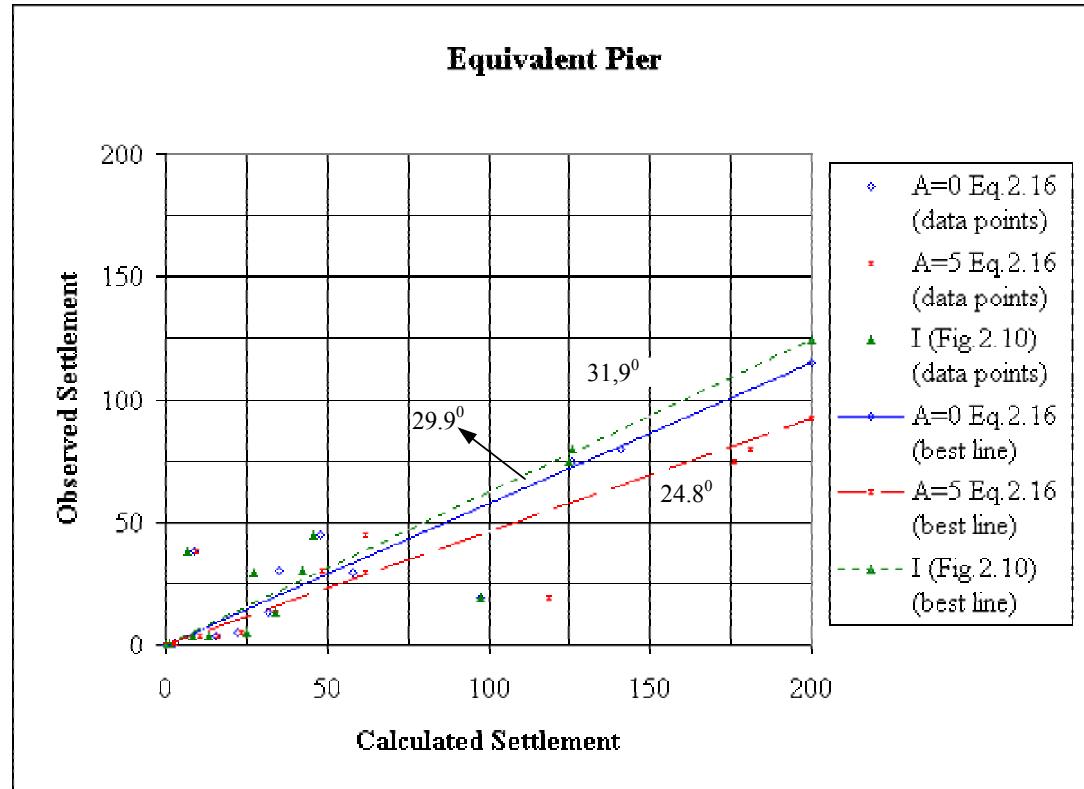
**Figure 4.8:** Calculated and observed values for friction piles ( $L/re < 1$  and  $de < 1$ ) (mm)



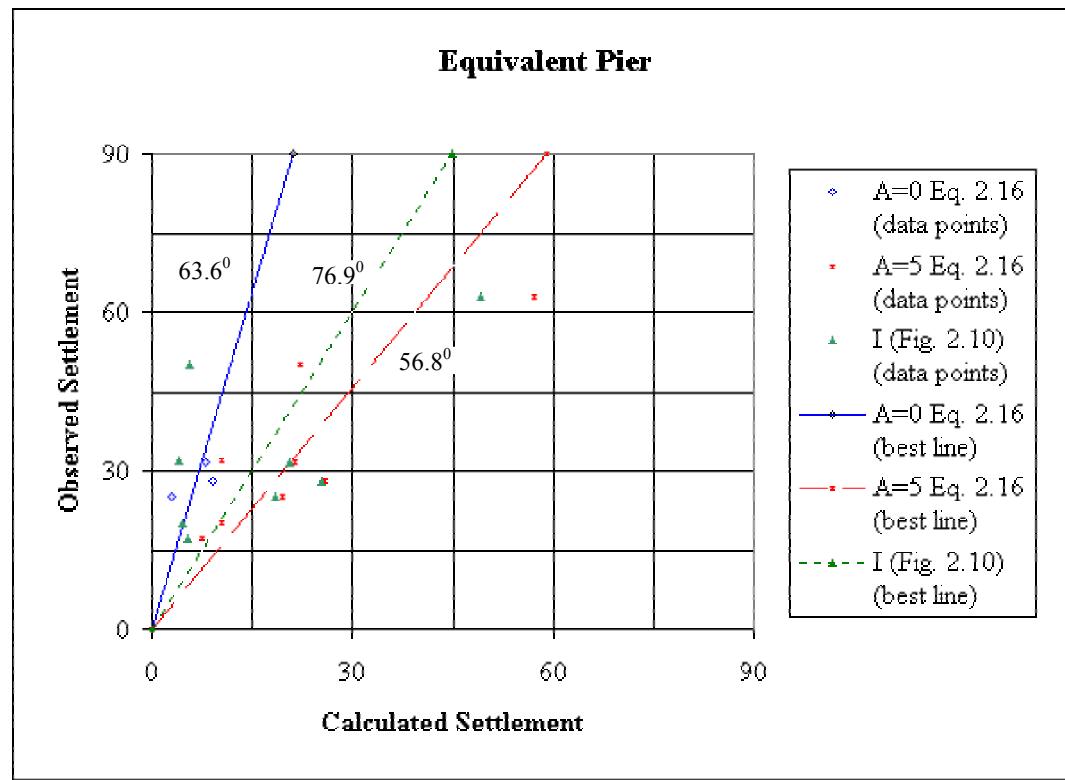
**Figure 4.9:** Calculated and observed values for friction piles ( $L/re < 1$  and  $de2$ ) (mm)



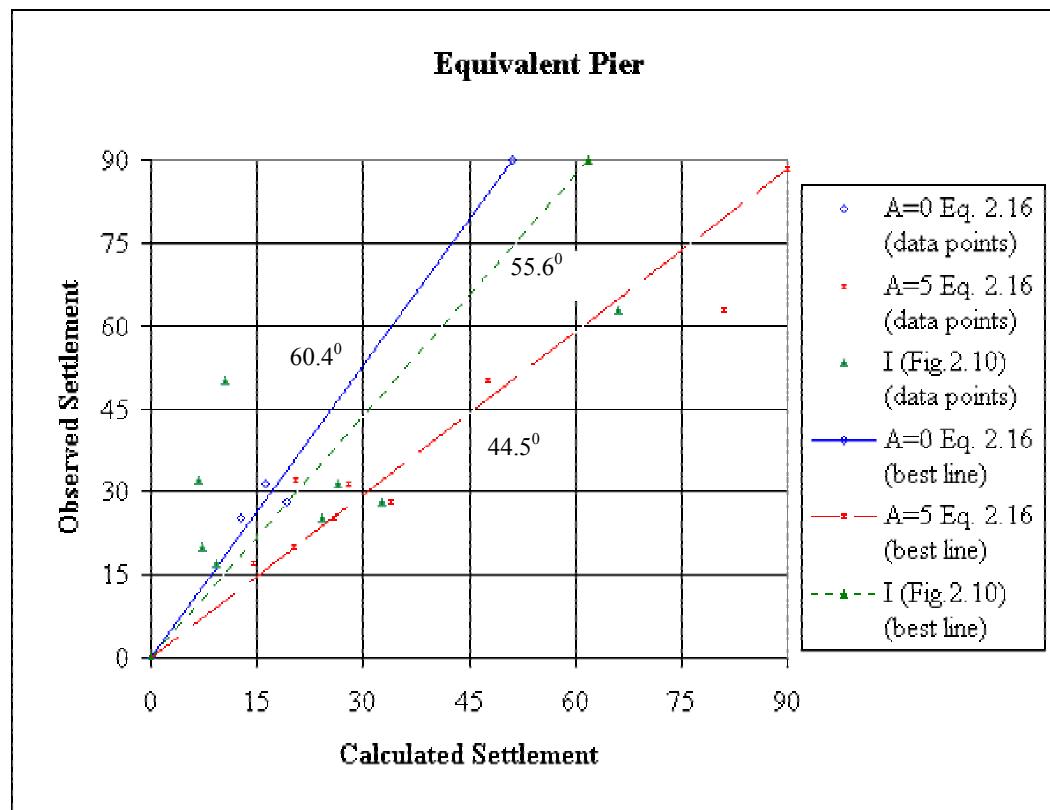
**Figure 4.10:** Calculated and observed values for friction piles ( $L/re>1$  and  $de1$ ) (mm)



**Figure 4.11:** Calculated and observed values for friction piles ( $L/re>1$  and  $de2$ ) (mm)



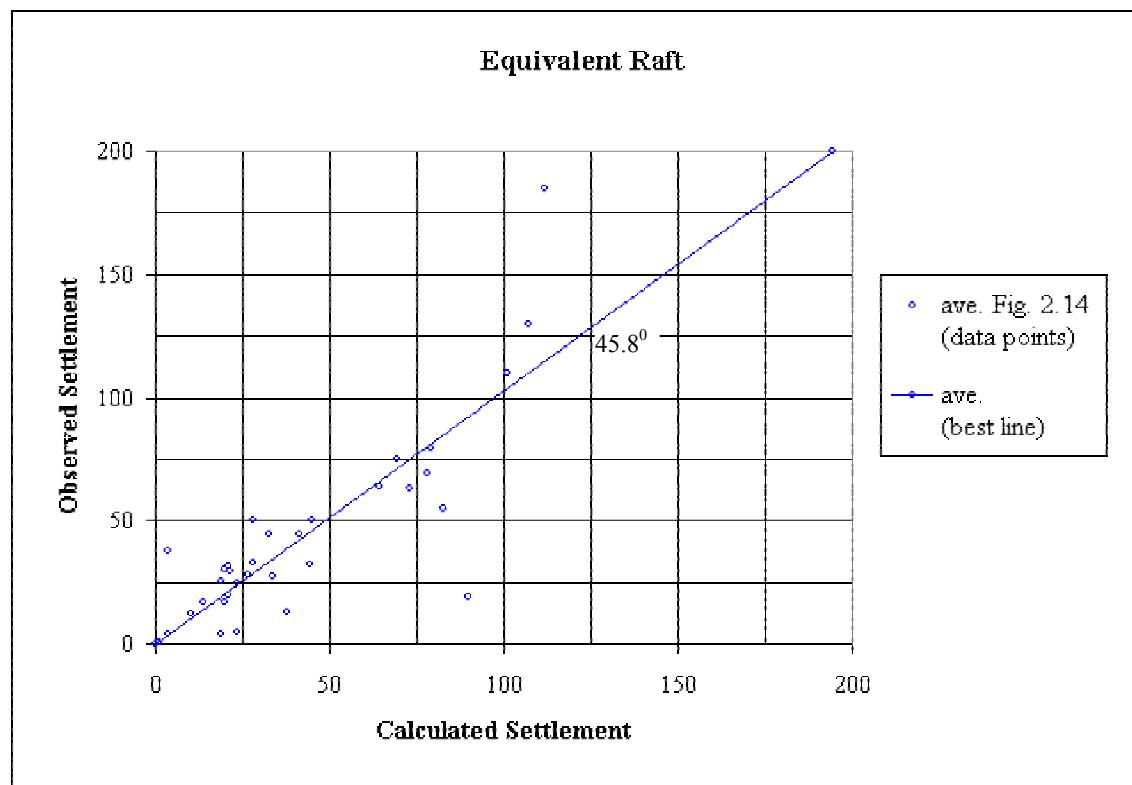
**Figure 4. 12:** Calculated and observed values for end-bearing piles (de1) (mm)



**Figure 4.13:** Calculated and observed values for end-bearing piles (de2) (mm)

**Table 4.8:** Calculated and observed settlement values for equivalent raft method (mm)

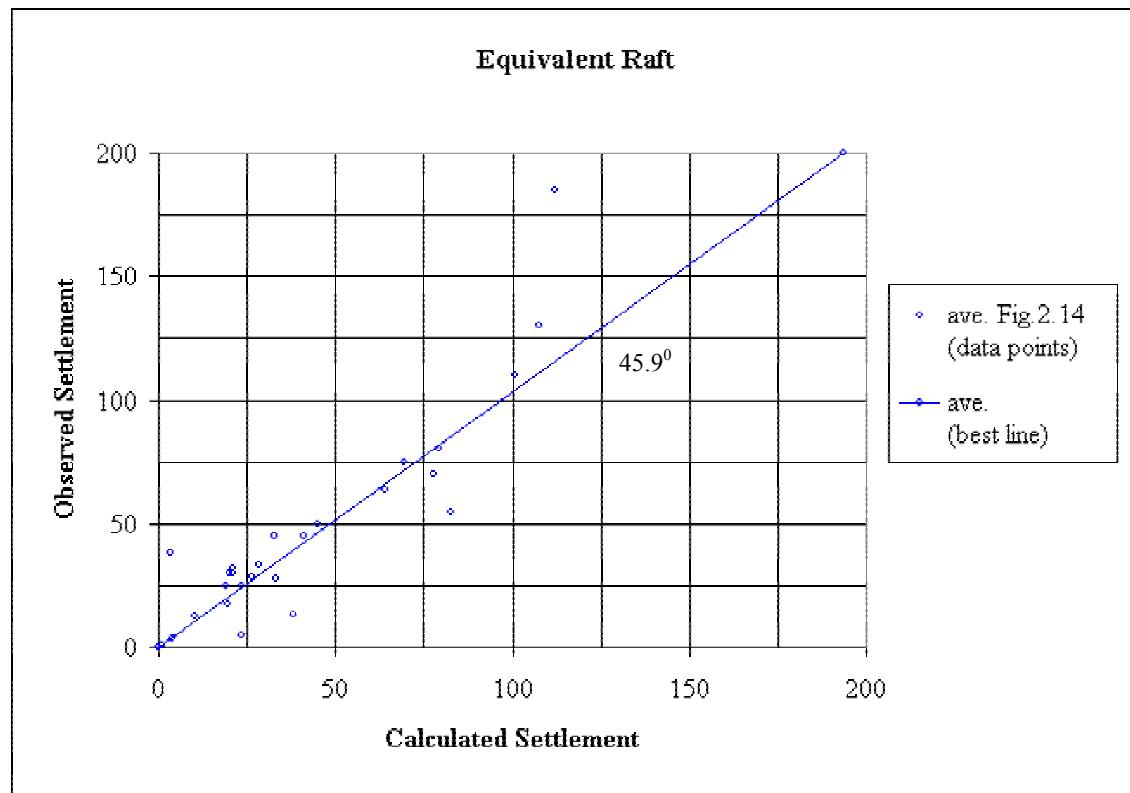
	Equivalent Raft	Ave.	Mea.	(Cal.-Mea.)/ Mea.*100		Ave.	Mea.	(Cal.-Mea.)/ Mea.*100	
1	Field Test	3,56	38,1	90,66	17	Molasses Tank	21,2	29,5	28,14
2	Test of Kaino	3,82	3,8	0,53	18	Messeturm Tower	107,4	130	17,40
3	Frame-type 2	37,92	13	191,69	19	New Law Court II	20,96	31,5	33,46
4	Frame-type 3	23,39	5	367,80	20	New Law Court I	26,5	28,1	5,69
5	9-Pile group	1	0,9	11,11	21	New Law Court III	19,1	25,1	23,90
6	Frame-type 7	18,65	4	366,25	22	Congress C. Office	32,63	45	27,49
7	Five-storey	10,42	12,65	17,63	23	Congress C. Hotel	44,80	50	10,40
8	Eurotheum	44,44	32	38,88	24	Commerz Bank	13,91	17	18,18
9	Japan Centre	28,08	50	43,84	25	Main Tower	20,98	20	4,90
10	Forum Kastor	69,26	75	7,65	26	Cambridge Road	33,45	27,5	21,64
11	Forum Pollux	78,99	80	1,26	27	19-Storey Building	64,24	64	0,37
12	American Express	82,74	55	50,44	28	Hotel Japan	19,69	17,5	12,51
13	Westend I Tower	100,9	110	8,32	29	İzmir Hilton Complex	77,91	69,6	11,94
14	Messe-Torhaus	41,16	45	8,53	30	Frame-type 6	90,03	19	373,84
15	Gratham Road	20,09	30	33,03	31	Stonebridge Park Flats	23,71	25	5,16
16	Treptowers	72,98	63	15,84	32	Dashwood House	28,23	33	14,45
					33	Ghent Grain Terminal	111,8	185	39,55



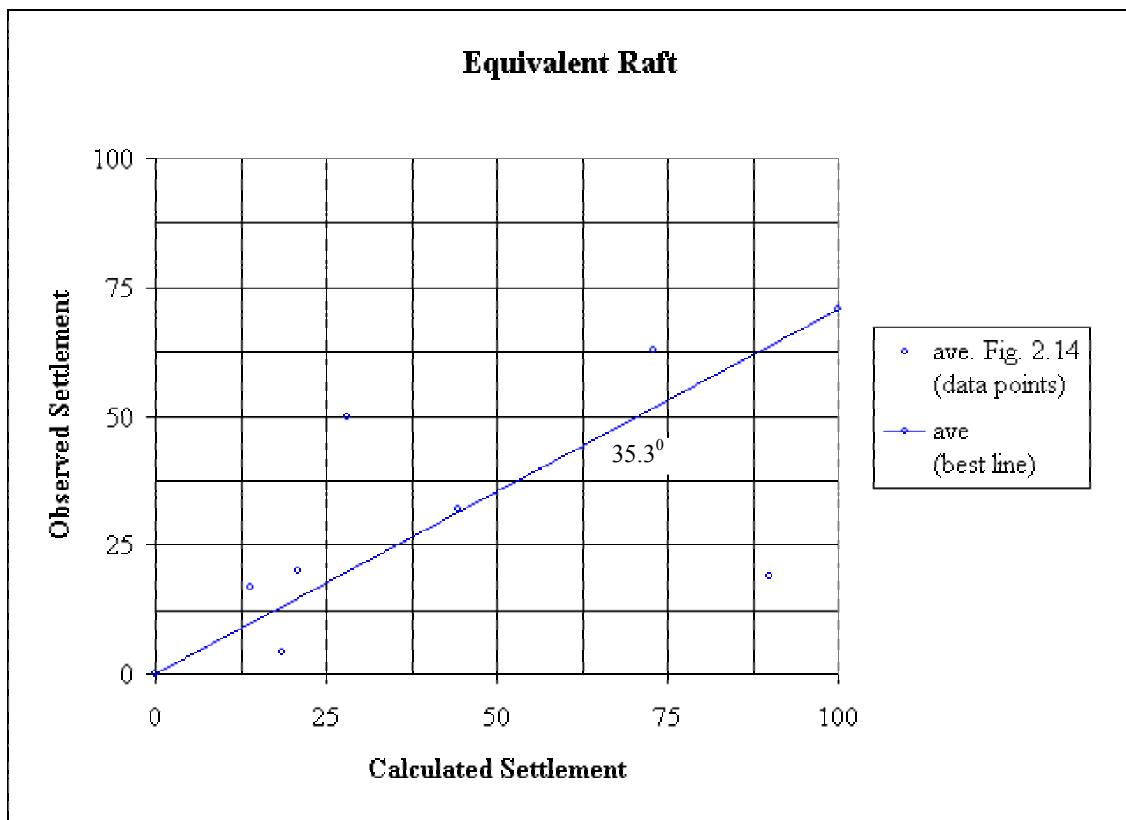
**Figure 4.14:** Calculated and observed values for equivalent raft method (mm)

**Table 4.9:** Calculated and observed settlement values for friction and end-bearing piles - equivalent raft method (mm)

	<b>Friction piles</b>	<b>Ave.</b>	<b>Mea.</b>		<b>Ave.</b>	<b>Mea.</b>
1	Field Test on five-Pile	3,56	38,1	14	Meseturm Tower	107,38
2	Test of Kaino	3,82	3,8	15	New Law Court II	20,96
3	Frame-type 2	37,92	13	16	New Law Court I	26,5
4	Frame-type 3	23,39	5	17	New Law Court III	19,1
5	9-Pile group	1	0,9	18	Congress C. Office	32,63
6	Five-storey Building	10,42	12,65	19	Congress C. Hotel	44,80
7	Forum Kastor	69,26	75	20	Cambridge Road	33,45
8	Forum Pollux	78,99	80	21	19-Storey Building	64,24
9	American Express	82,74	55	22	Hotel Japan	19,69
10	Westend I Tower	100,85	110	23	İzmir Hilton	77,91
11	Messe-Torhaus	41,16	45	24	Stonebridge Park	23,71
12	Gratham Road	20,09	30	25	Dashwood House	28,23
13	Molasses Tank	21,2	29,5	26	Ghent Grain	111,83
	<b>End-bearing piles</b>					
1	Commerz Bank	<b>13,91</b>	17	5	Eurotheum	44,44
2	Japan Centre	<b>28,08</b>	50	6	Treptowers	72,98
3	Main Tower	<b>20,98</b>	20	7	Frame-type 6	90,03
4	Frame-type 7	18,65	4			



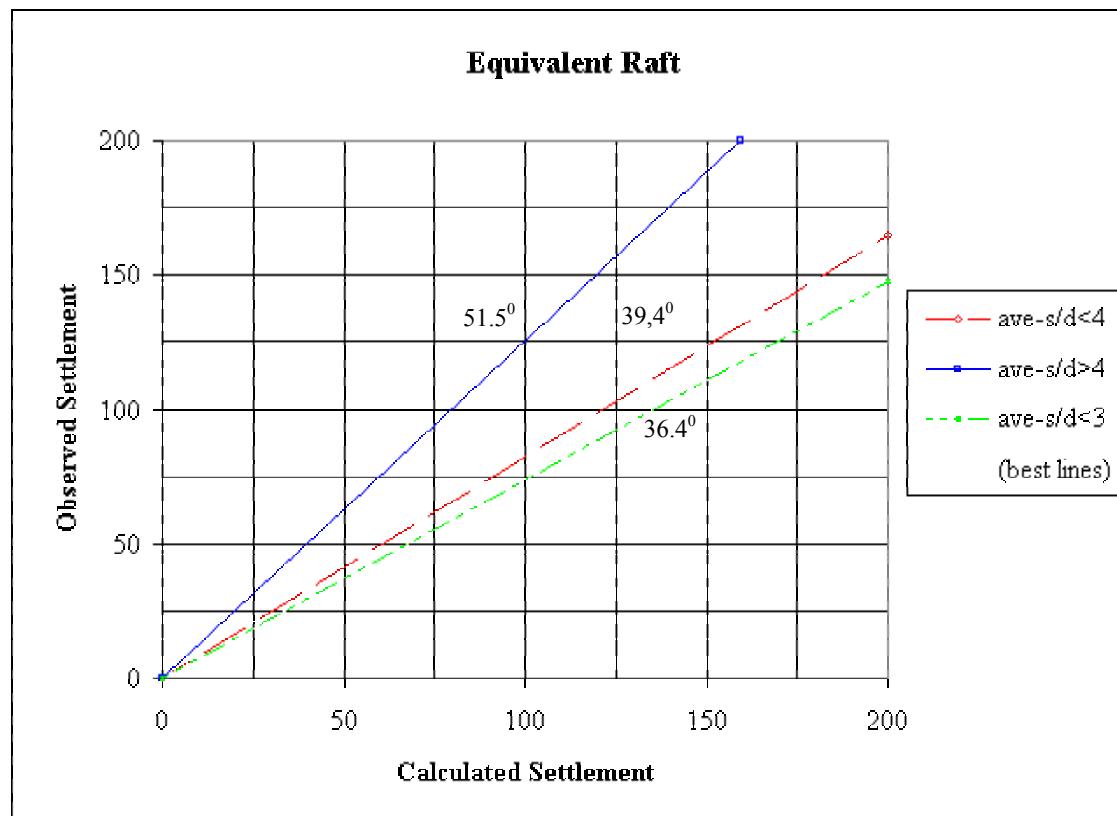
**Figure 4.15:** Calculated and observed values for friction piles (mm)



**Figure 4. 16:** Calculated and observed values for end-bearing piles (mm)

**Table 4.10:** Calculated and observed settlement values for s/d>4, s/d<4 and s/d<3 - equivalent raft method (for friction piles) (mm)

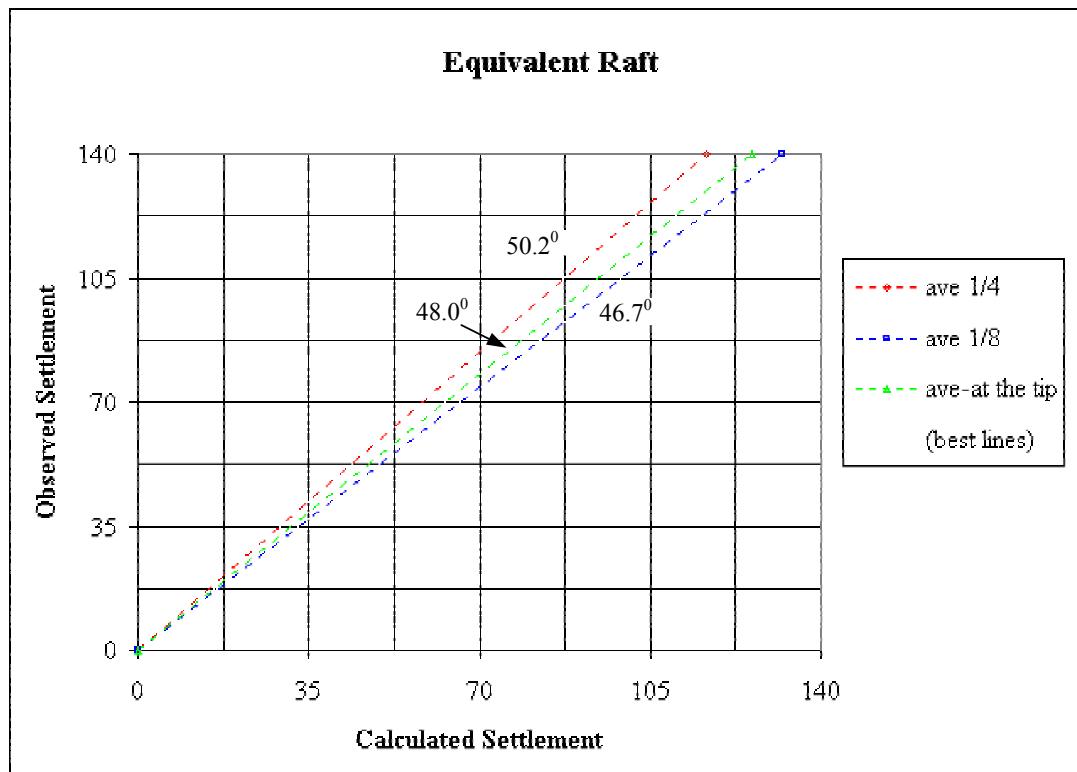
	<b>Equivalent Raft</b>	<b>Ave.</b>	<b>Mea.</b>	<b>s/d</b>		<b>Ave.</b>	<b>Mea.</b>	<b>s/d</b>
1	Test of Kaino	3,82	3,8	3,5	<b>1</b> Field Test	3,56	38,1	4,05
2	Frame-type 3	23,39	5	3	<b>2</b> Five-storey	10,42	12,65	7
3	9-Pile group	1	0,9	3	<b>3</b> Forum Kastor	69,26	75	5
4	American Express	82,74	55	3,15	<b>4</b> Forum Pollux	78,99	80	5
5	Messe-Torhaus	41,16	45	3,25	<b>5</b> Westend I Tower	100,85	110	5
6	Stonebridge	23,71	25	3,58	<b>6</b> Gratham Road	20,09	30	4
7	Dashwood House	28,23	33	3,093	<b>7</b> Molasses Tank	21,2	29,5	7
					<b>8</b> Mессeturm Tower	107,38	130	4,75
					<b>9</b> Congress Office	32,63	45	4,5
					<b>10</b> Congress Hotel	44,80	50	4,5
1	Frame-type 2	37,92	13	1,8	<b>11</b> Cambridge Road	33,45	27,5	4,5
2	Hotel Japan	19,69	17,5	2	<b>12</b> 19-Storey	64,24	64	6
3	İzmir Hilton	77,91	69,6	2,6	<b>13</b> Ghent Grain	111,83	185	4



**Figure 4.17:** Calculated and observed values for friction piles for different s/d (mm)

**Table 4.11:** Calculated and observed settlement values for different pressure distribution and different raft location - equivalent raft method (for friction piles) (mm)

		Pressure is distributed 4V:1H	Pressure is distributed 8V:1H	If pile raft is located at the tip of the piles	Ave.	Ave.	Ave.	Mea.	s/d	Lpile	Braft/Lpile
1	Field Test	3,56	8,47	17,69	38,1	4,05	9,15	0,11			
2	Forum Kastor	69,26	75,51	71,74	75	5	25	0,8			
3	Forum Pollux	78,99	89,77	84,18	80	5	30	0,66			
4	Westend I Tower	100,85	112,58	106,51	110	5	30	1,07			
5	Gratham Road	20,09	22,82	23,55	30	4	17,45	1,1			
6	Molasses Tank	21,2	27,89	27,71	29,5	7	27	0,3			
7	Messeleturm Tower	107,38	120,88	113,75	130	4,75	30,9	1,68			
8	Congress Office	32,63	35,38	33,52	45	4,5	28	1,26			
9	Congress Hotel	44,80	48,85	43,93	50	4,5	28	2			
10	Cambridge Road	33,45	37,3	30,43	27,5	4,5	15,3	1,04			
	Angle	50,21°	46,71°	48,03°							



**Figure 4.18:** Calculated and observed values for friction piles for different pressure distribution and different raft location (mm)

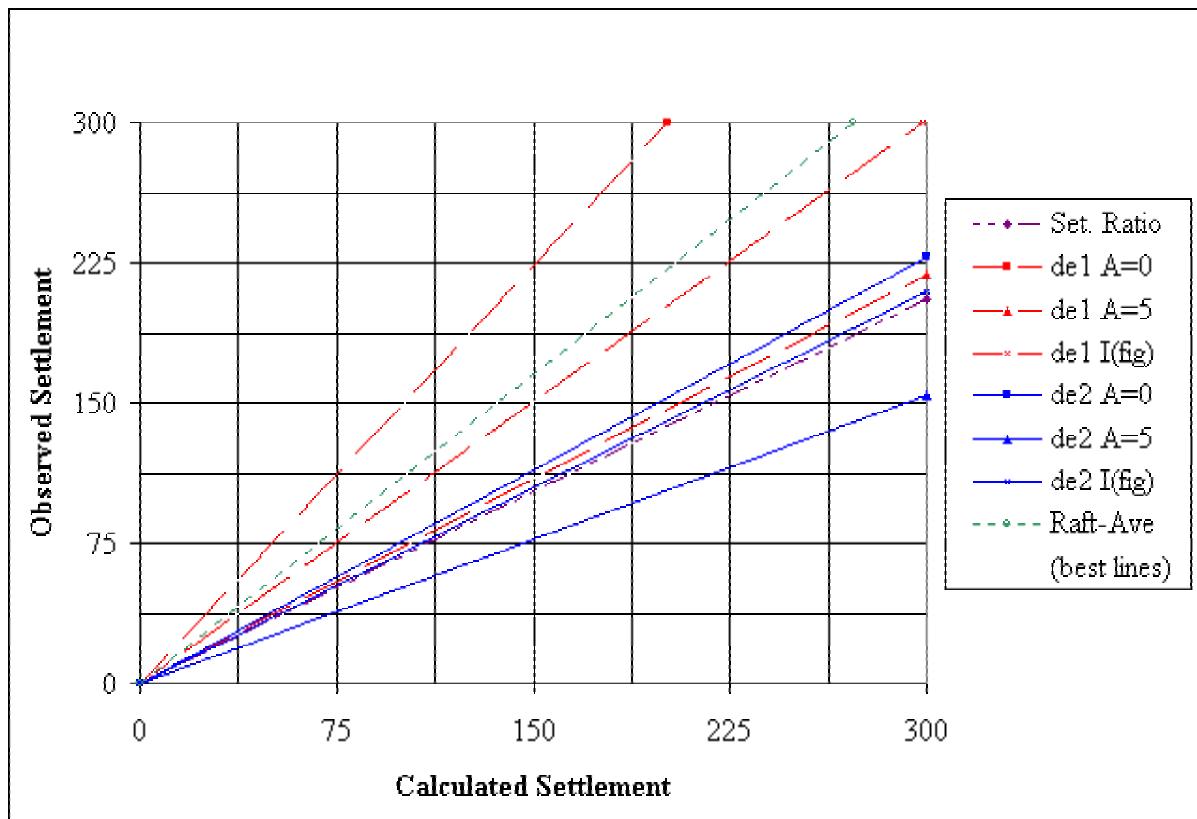
**Table 4.12:** Calculated and observed settlement values for all methods (mm)

	<b>Friction Piles</b>	<b>Settlement Ratio</b>	<b>Equivalent Pier</b>						<b>Equivalent Raft</b>	<b>Mea.</b>		
			d <sub>e1</sub> (Equation 2.13-2.14)			d <sub>e2</sub> (Fig. 2.9)						
			A=0	A=5	I (fig 2.10)	A=0	A=5	I (fig 2.10)				
1	Field Test	7,59	6,01	6,53	4,28	8,94	9,36	6,71	3,56	38,1		
2	Test of Kaino	9,48	8,01	9,01	6,83	9,71	10,59	8,26	3,82	3,8		
3	Frame-type 2	29,61	27,02	29,38	28,99	31,91	33,9	34,05	37,92	13		
4	Frame-type 3	21,58	17,56	18,71	17,58	22,4	23,3	24,86	23,39	5		
5	9-Pile group	2,3	1,44	1,55	0,68	2,58	2,71	1,04	1	0,9		
6	Five-storey	13,7	4,94	10,84	7,78	10,55	15,89	11,4	10,42	12,7		
7	Forum Kastor	156,40	64,64	121,15	84,17	126,00	176,22	124,95	69,26	75		
8	Forum Pollux	139,59	77,67	123,17	88,09	141,03	180,96	125,88	78,99	80		
9	American	291,43	59,2	163,72	107,05	148,1	240,16	169,95	82,74	55		
10	Westend	165,73	76,21	145,36	103,58	148,95	213,09	148,42	100,85	110		
11	Messe-Torhaus	47,48	30,7	45,61	36,71	47,68	61,61	45,91	41,16	45		
12	Gratham Road	32,84	22,5	36,99	30,5	35,19	48,74	42,42	20,09	30		
13	Molasses Tank	25,34	19,27	24,24	14,91	57,82	61,68	27,39	21,2	29,5		
14	Messeturm	161,11	60,08	147,43	100,55	141,7	219,2	155,9	107,38	130		
15	Congress Office	71,46	21,60	56,58	38,13	55,65	86,22	61,98	32,63	45		

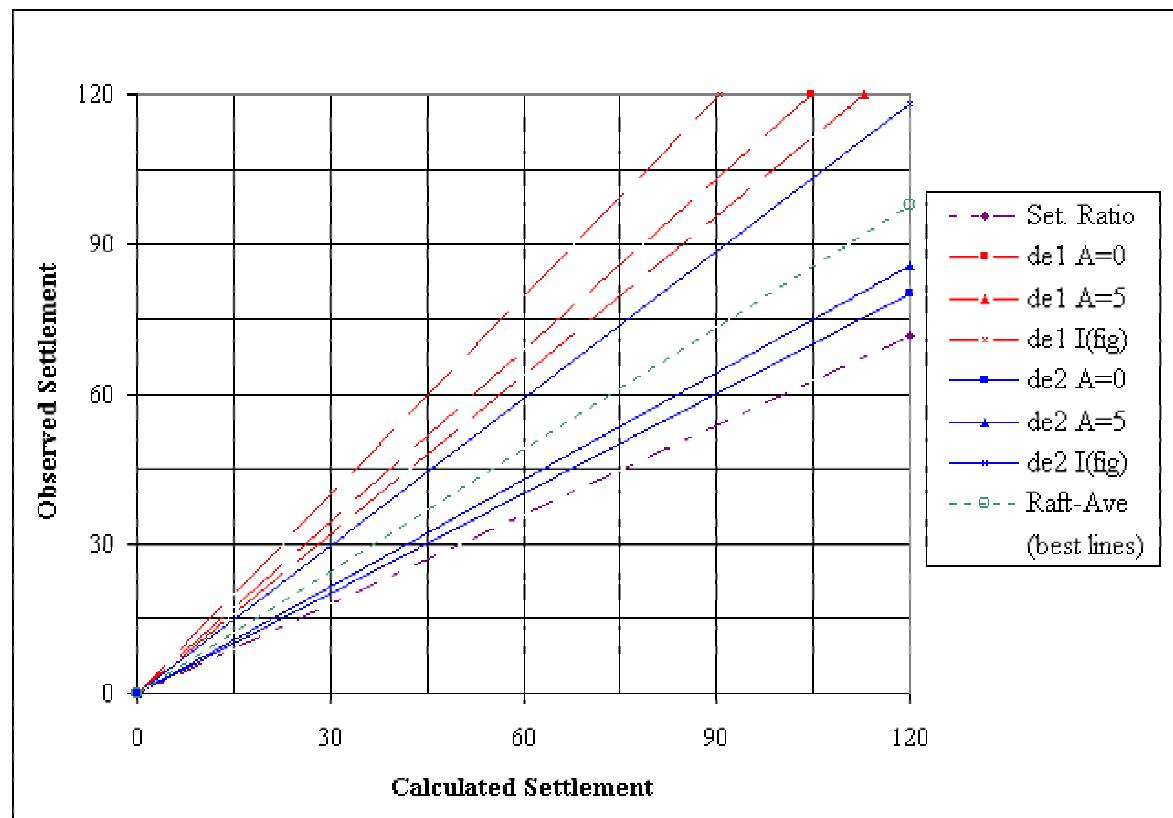
16	Congress Hotel	105,45		93,46	58,89	68,42	143,59	99,72	44,80	50
17	Cambridge	31,42	24,89	42,42	34,24	42,7	58,88	47,95	33,45	27,5
18	19-Storey	77,12		87,69	52,03		133,98	82,59	64,24	64
19	Hotel Japan	17,14		17,05	11,51		23,08	16,61	19,69	17,5
20	İzmir Hilton	83,3	8,71	76,29	52,39	57,31	109,1	78,19	77,91	69,6
21	Stonebridge	29,34	9,47	35,18	24,44	28,21	49,52	38,8	23,71	25
22	Dashwood	35,29	14,79	42,47	30,6	35,59	59,39	48,58	28,23	33
23	Ghent Grain	119,14		232,57	205,22	176,49	271,02	235,37	111,83	185

#### **End-Bearing Piles**

1	Frame-type 7	13,26	11,01	11,98	9,53	15,33	16,13	13,11	18,65	4
2	Eurotheum	35,05		10,42	3,88		20,46	6,75	44,44	32
3	Japan Centre	74,89		22,24	5,52		47,51	10,39	28,08	50
4	Treptowers	98,4		57,27	49,22		80,95	66,02	72,98	63
5	New Court II	30,56	7,91	21,29	20,55	16,17	27,91	26,43	20,96	31,5
6	New Court I	36,67	8,99	26,02	25,39	19,24	33,95	32,66	26,5	28,1
7	New Court III	29,09	2,84	19,61	18,3	12,76	25,87	24,1	19,1	25,1
8	Commerz Bank	36,41		7,49	5,29		14,44	9,33	13,91	17
9	Main Tower	51,1		10,37	4,53		20,08	7,3	20,98	20
10	Frame-type 6	79,69	63,31	86,17	76,17	97,59	118,45	97,77	90,03	19



**Figure 4.19:** Calculated and observed values for friction piles - All methods (mm)



**Figure 4.20:** Calculated and observed values for end-bearing piles - All methods (mm)

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## APPENDIX

### CASE HISTORIES

#### **1. Field Test on Five-Pile Group, San Francisco (n=5)**

In the framework of an investigation on the behaviour of piles in sand, load tests to failure were performed on a single pile and on a five-pile group. The piles were closed-end steel pipes, 273 mm in diameter, driven to a depth of 9.15 m below ground surface through a 300 mm diameter predrilled to a depth of 1.37 m. The piles of the group were connected by a rigid reinforced concrete cap, clear of the ground.

At the test site, the subsoil consists of a hydraulic fill made of clean sand, about 11 m thick, overlain by 1.4 m of sandy gravel and underlain by sand with interbedded layers of stiff clay down to the bedrock found at a depth of around 14.3 m below ground surface. The average settlement is calculated as 36,8 mm by using non-linear analysis by the program GRUPPALO. Using linear elastic analysis average settlement is estimated as 2,6 mm (Randolph (1994)).  
(Mandolini, A., and Viggiani, C., 1997)

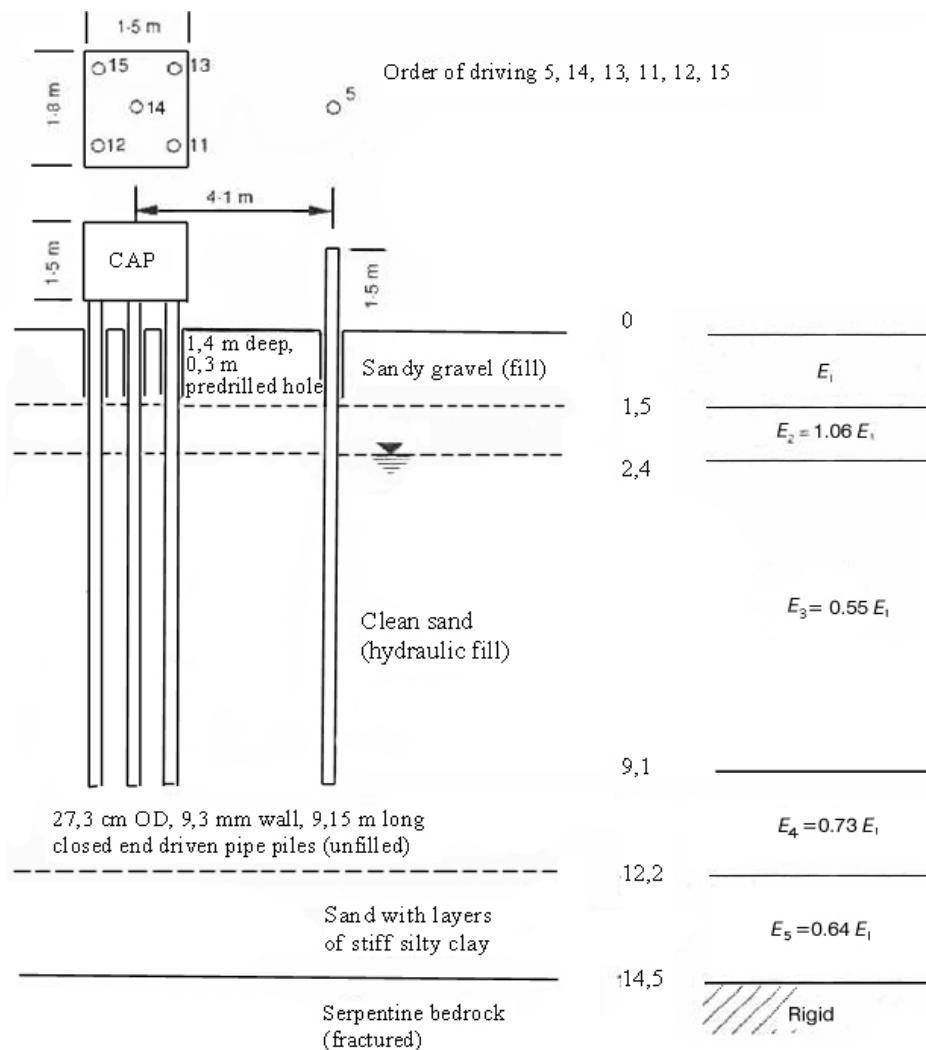
### a) Settlement Ratio Method

$$n=5 \quad d=0,273 \text{ m} \quad r_0=0,1365 \text{ m}$$

$$L=9,15 \quad s/d_{ave}=4,05 \text{ m}$$

$$E_l=92,2 \text{ MN/m}^2 \quad E_p=20000 \text{ MN/m}^2$$

$v_s=0,3$      $v_s=0,4$     Clean Sand



**Figure A.1:** Layout of the test and subsoil profile (Mandolini and Viggiani, 1997)

$$P=2450 \text{ KN}$$

$$\lambda=E_p/G_l=20000/22,13 \approx 903,75$$

$$\rho=G_{l/2}/G_l=0,763\rightarrow 1$$

$$\log \lambda = 2,956 \rightarrow 0,98$$

$$s/d=4,05 \rightarrow 0,93$$

$$L/d=33,52 \rightarrow 0,55$$

$$v_s=0,3 \rightarrow 1$$

$$v_s=0,4 \rightarrow 0,97$$

$$\eta_w=n^{-e} \quad R_s=n^e$$

$$\zeta=\ln\{[0,25+(2,5 \rho (1-v)-0,25)\xi] L/r_0\}$$

$$\eta=r_b/r_0=1 \quad \xi=G_b/G_b=1$$

$$\mu L=(2/(\lambda\zeta))^{0,5}L/r_0$$

$$P_{\text{single}}=2450/5=490 \text{ KN}$$

	e	$\eta_w$	R_s	$\zeta$	$\mu L$	$\tanh \mu L \frac{L}{(\mu L r_0)}$	$P_t/(w_t G_l r_0)$
$v_s=0,3$	0,501	0,446	2,240	4,495	1,487	40,690	45,427
$v_s=0,4$	0,486	0,457	2,187	4,341	1,513	40,195	46,689

	$P_t/w_t$	K=n $\eta_w k$	$\delta=P/K(\text{mm})$	$P_{\text{single}}/k$	$\delta=\delta_s R_s$
$v_s=0,3$	137,225	306,219	8,00	3,57	8,00
$v_s=0,4$	141,037	322,435	7,59	3,47	7,59

$$\delta_{\text{measured}}=38,1 \text{ mm}$$

### b) Equivalent Pier Method

$$B = A_G^{0.5} = 1,643$$

$$A_p = \pi d^2 n / 4 = 0,2926 \text{ m}^2$$

$$E_p = 20000 \text{ MPa}$$

$$E_s' = 57,55 \text{ MPa} \quad E_u = 66,41 \text{ MPa}$$

$$d_e = 1,27 A_G^{0.5} = 2,087 \text{ m (for friction piles)}$$

$$\rho = 0,763 \quad L = 9,15 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

### Method 1

	$E_e$	$\lambda$	$\zeta$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s = 0,3$	2219,277	100,253	2,460	0,789	3,654	0,295	6,02
			2,816	0,738	3,730	0,320	6,53
$v_s = 0,4$	2223,225	100,431	2,306	0,814	3,617	0,297	5,63
			2,710	0,751	3,710	0,327	6,19

### Method 2

$$L/d_e = 9,15 / 2,086 = 4,38 \rightarrow I_\delta = 0,21 \quad (\text{Fig. 2.10})$$

	$v_s = 0,3$	$v_s = 0,4$
$\delta \text{ (mm)}$	4,28	3,97

$$K \approx 300 \text{ (pile stiffness factor)} \quad s/d \approx 4,05 \quad L/d \approx 33,51 \quad B = 1,643 \text{ m}$$

$$d_e/B \approx 0,81 \text{ assumed, then } d_e \approx 1,33 \text{ m (Fig. 2.9)}$$

## Method 1

	$E_e$	$\lambda$	$\zeta$	$\mu L$	$\tanh \mu L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,3$	2219,27	100,25	2,910	1,138	4,915	0,279	8,94
			3,151	1,094	5,016	0,292	9,36
$v_s=0,4$	2223,225	100,431	2,756	1,168	4,846	0,286	8,514
			3,032	1,114	4,970	0,302	8,987

## Method 2

$$L/d_e = 9,15 / 1,33 = 6,87 \rightarrow I_\delta = 0,21 \text{ (Fig. 2.10)}$$

$\delta$ (mm)	$v_s=0,3$	$v_s=0,4$
	6,71	6,23

$$\delta_{\text{measured}} = 38,1 \text{ mm}$$

## c) Equivalent Raft Method

$$\delta_i \text{ ave} = \mu_1 \mu_0 q_n B / E$$

B	L	$q_n$	L/B	H	D/B	H/B	$\mu_0$	$\mu_1$	$\delta_i$
4,07	4,277	140,745	1,05	3	1,49	0,73	0,905	0,26	2,65
7,534	7,691	42,282	1,02	3,1	1,20	0,41	0,91	0,14	0,56
11,11	11,27	19,567	1,01	2,3	1,09	0,20	0,91	0,05	0,16
									3,22 mm

$$\delta_c = m_v \sigma_z H \mu_d \mu_g$$

$$D/(LB)^{0.5} = 1,46 \rightarrow \mu_d = 0,665$$

For sand with layers of stiff silty clay

$z/B$	$\sigma_z/q$	$\sigma_z$	H	$m_b$	$\mu_g$	$\mu_d$	$\delta_c$ (mm)
1,781	0,11	15,48	2,3	0,0145	1	0,665	0,344

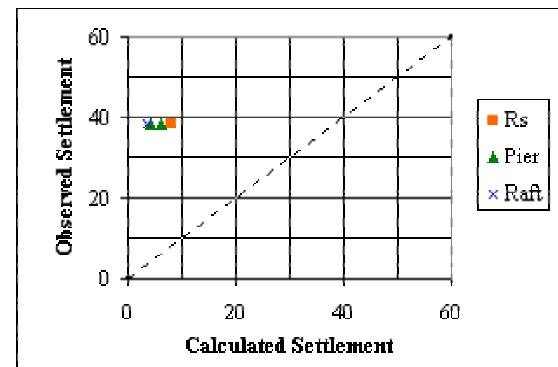
$$\delta_T = \delta_i + \delta_c = 3,22 + 0,344 = \boxed{3,56 \text{ mm}}$$

$\delta_{\text{measured}} = 38,1 \text{ mm}$

**Table A.1:** Measured and computed settlements for Field Test on Five Pile Group (mm)

Settlement (mm)									
Set. Ratio		Equivalent Pier			Equivalent Raft			Mea.	
		d <sub>e1</sub>		d <sub>e2</sub>		H=8,4 m	H=5,3 m (at the pile tip)		
		Met1	Met2	Met1	Met2	Ave.	Ave.		
vs=0,3	8,00	6,02	4,28	8,94	6,71	3,56	17,69	5,92	8,47
		6,53		9,36					
vs=0,4	7,59	5,63	3,97	8,51	6,23	3,42	17,13	5,77	8,27
		6,19		8,98					

Field Test on Five Pile Group			
Rs	8	Mea.	38,1
Pier	6,02 4,28		
Raft	3,56		



**Figure A.2:** Measured and computed settlements for Field Test on Five Pile Group (mm)

## **2. Test of Kaino and Aoki (n=5)**

The soil profile consisted of layers of alluvial clay underlain by interbedded sand and clay layers. The modulus values varied from about 12 MPa near the surface to about 74 MPa along the lower parts of the pile, while the value at the pile tip was taken as 38 MPa. The piles were 24 m long and 1 m diameter and were constructed using the reverse circulation method. The interaction factor method was used to analyse the settlement using the program DEFPIG (non-linear), and the group settlement under a load of 6.66 MN was computed to be 3.9 mm. (H.G. Poulos, 1993)

### **a) Settlement Ratio Method**

$$n = 5 \quad d = 1 \text{ m} \quad r_0 = 0.5 \text{ m}$$

$$L = 24 \text{ m} \quad s/d_{ave} = 3.5 \quad s = 3.5 \text{ m}$$

$$E_p = 30000 \text{ MN/m}^2$$

$$P = 6.66 \text{ MN} \quad v_s = 0.3 \quad v_s = 0.4$$

$$\lambda = E_p/G_l = 30000/14.6 \approx 2054.79$$

$$\rho = G_{l/2}/G_l = 0.657 \rightarrow 0.975$$

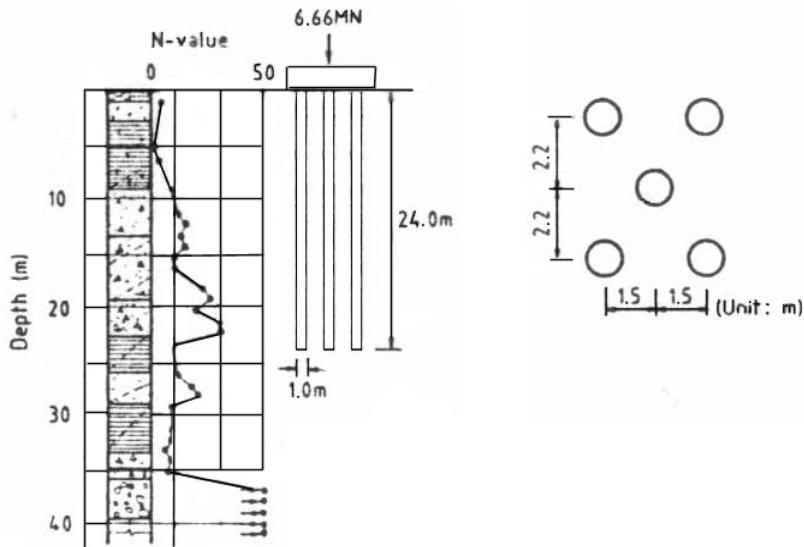
$$\log \lambda = 3.31 \rightarrow 1.05$$

$$s/d = 3.5 \rightarrow 0.975$$

$$L/d = 24 \rightarrow 0.542$$

$$v_s = 0.3 \rightarrow 1$$

$$v_s = 0.4 \rightarrow 0.97$$



**Figure A.3:** The soil profile and the pile group configuration (Poulos, 1993)

$$\eta_w = n^e \quad R_s = n^e \quad \eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 1$$

$$\zeta = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et.al, 1992})$$

$$\mu L = (2/(\lambda \zeta))^{0.5} L/r_0$$

$$P_{\text{single}} = 6660/5 = 1332 \text{ KN}$$

	e	$\eta_w$	$R_s$	$\zeta$	$\mu L$	$\tanh \mu L L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s=0,3$	0,541	0,418	2,388	4,012	0,747	40,68	45,96
$v_s=0,4$	0,524	0,429	2,327	3,857	0,762	40,449	47,984

	$P_t / w_t$	$K = n \eta_w k$	$\delta = P / K (\text{mm})$	$P_{\text{single}} / k$	$\delta = \delta_s R_s$
$v_s=0,3$	335,51	702,32	9,48	3,97	9,48
$v_s=0,4$	350,28	752,65	8,84	3,80	8,84

$\delta_{\text{measured}} = 3,8 \text{ mm}$

### b) Equivalent Pier Method

$$B = A_G^{0.5} = 4,647 \text{ m} \quad A_p = \pi d^2 n / 4 = 3,926 \text{ m}^2$$

$$E_p = 30000 \text{ MPa} \quad E_s' = 37,96 \text{ MPa} \quad E_u = 43,8 \text{ MPa}$$

$$d_e = 1,27 A_G^{0.5} = 5,902 \text{ m} \text{ (for friction piles)}$$

$$\rho = 0,657 \quad L = 24 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-v) L / r_0) \text{ (W. Fleming, et.al, 1992)}$$

$$\zeta_2 = \ln / \{ 5 + [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L / r_0 \} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s = 0,3$	5485,213	375,699	2,236	0,396	3,865	0,269	8,01
			2,664	0,363	3,896	0,303	9,01
$v_s = 0,4$	5487,602	375,863	2,082	0,411	3,851	0,266	7,34
			2,566	0,370	3,889	0,304	8,40

### Method 2

$$L/d_e = 24/5,9 = 4,066 \rightarrow I_\delta = 0,23 \text{ (Fig. 2.10)}$$

	$v_s = 0,3$	$v_s = 0,4$
$\delta \text{ (mm)}$	6,83	6,34

$K \approx 700$  (pile stiffness factor)     $s/d \approx 3,5$      $L/d \approx 24$      $B=4,647$  m

$d_e/B \approx 0,96$  assumed, then  $d_e \approx 4,46$  m

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,3$	5485,213	375,699	2,516	0,495	4,980	0,246	9,71
			2,855	0,464	5,024	0,269	10,59
$v_s=0,4$	5487,602	375,863	2,362	0,510	4,957	0,246	8,99
			2,748	0,473	5,011	0,272	9,94

### Method 2

$L/d_e = 24/4,46 = 5,38 \rightarrow I_\delta = 0,21$  (Fig. 2.10)

	$v_s=0,3$	$v_s=0,4$
$\delta$ (mm)	8,26	7,67

$\delta_{\text{measured}} = 3,8$  mm

### c) Equivalent Raft Method

$P = 6660$  KN

$q_n = P/(BL)$

$\delta_i = \mu_1 \mu_0 q_n B / E_u$

B	L	H	H/B	L/B	D/B	E <sub>u</sub>	q <sub>n</sub>	μ <sub>0</sub>	μ <sub>1</sub>	δ <sub>i</sub> (mm)
12	13,4	7	0,58	1,11	1,33	38,60	41,41	0,91	0,21	2,461
20	21,4	3	0,15	1,07	1,15	45,55	15,56	0,91	0,04	0,249
23,4	24,8	3	0,12	1,06	1,11	48,45	11,47	0,92	0,03	0,153
26,8	28,2	5	0,18	1,05	1,08	67,50	8,81	0,92	0,05	0,161
										3,023

$$(LB)^{0,5} / D = 0,79 \rightarrow m_d = 68$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)]$$

$$\text{for sand } q_c/N=5 \quad M_0=2q_c+20$$

$$\delta_c = m_v \sigma_z H m_d m_g$$

z/B	σ <sub>z</sub> /q	σ <sub>z</sub>	m <sub>v</sub>	m <sub>g</sub>	m <sub>d</sub>	δ <sub>c</sub>
0,29	0,68	28,16	0,02	1	0,68	2,68 (sand)
0,70	0,39	16,15	0,019	0,85	0,68	0,52 (clay)
0,95	0,28	11,59	0,033	1	0,68	0,78 (sand)
1,29	0,18	7,45	0,013	0,85	0,68	0,27 (clay)
						Σδ <sub>c</sub> = 4,26
						Σδ <sub>c</sub> = 0,798

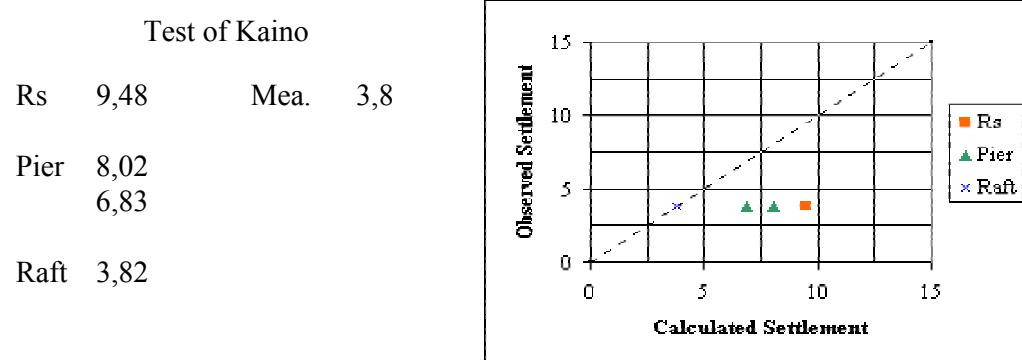
$$\delta_T = \delta_i + \delta_c$$

$$\delta_T = 0,798 + 3,051 = \boxed{3,82 \text{ mm}}$$

$$\delta_{\text{measured}} = 3,8 \text{ mm}$$

**Table A.2:** Measured and computed settlements for Test of Kaino (mm)

Set. Ratio		Settlement (mm)						Mea.	
		Equivalent Pier				Eq. Raft			
		d <sub>e1</sub>		d <sub>e2</sub>					
		Met1	Met2	Met1	Met2	Ave.			
vs=0,3	9,48	8,02	6,83	9,71	8,26	3,82	3,80		
		9,01		10,59					
vs=0,4	8,84	7,34	6,34	8,99	7,67	3,82	3,80		
		8,40		9,94					



**Figure A.4:** Measured and computed settlements for Test of Kaino (mm)

### **3. Frame-Type Building 2 (n=6)**

The total structural load of 15 MN is supported on a piled foundation which has 6 filling piles with a diameter of 1000 mm and length of 15,5 m. The distance between piles is 1,8 m. The size of groups in plane is 4,8\*3 m. At the site of the building tough plastic clay,  $E_u=35$  Mpa, is located. Different formulations are used to obtain settlement value. Settlement predictions and methods are given below:

USSR standarts    Poulos    Vesic    Skempton    Bartolomey:

48 mm        38 mm        5 mm        14 mm        11 mm

(Bartolomey, A.A., Yushkov, B.S., Leshin, G.M., Khanin, R.E., Kolesnik, G.S., Mulyukov, E.I., Doroshkevitch, N.M., 1981)

#### **a) Settlement Ratio Method**

$$n=6 \quad d=1 \text{ m} \quad r_0=0,5 \text{ m}$$

$$L=15,5 \text{ m} \quad s=1,8 \text{ m}$$

$$G=11,7 \text{ (MN/m}^2\text{)} \quad E_p=30000 \text{ MN/m}^2$$

$$v_s=0,15 \quad v_s=0,3 \quad \text{Tough Plastic Clays}$$

$$P=15 \text{ MN}$$

$$\lambda=E_p/G_l=30000/11,7 \approx 2564,103$$

$$\rho=G_{l/2}/G_l=1 \rightarrow 1,06$$

$$\log \lambda = 3,408 \rightarrow 1,065$$

$$s/d=1,8 \rightarrow 1,09$$

$$L/d=15,5 \rightarrow 0,525$$

$$v_s=0,15 \rightarrow 1,035$$

$$v_s = 0,3 \rightarrow 1$$

$$\eta_w = n^{-e} \quad R_s = n^e$$

$$\zeta = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et al., 1992})$$

$$\eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 1$$

$$\mu L = (2/(\lambda\zeta))^{0.5} L/r_0$$

$$P_{\text{single}} = 15000/6 = 2500 \text{ KN}$$

	e	$\eta_w$	R_s	$\zeta$	$\mu L$	$\tan \mu L L / (\mu L r_0)$	$P_t / (w_t G r_0)$
$v_s = 0,15$	0,668	0,301	3,313	4,188	0,423	29,273	47,809
$v_s = 0,3$	0,646	0,314	3,181	3,994	0,433	29,195	50,600

	$P_t/w_t$	K = n $\eta_w k$	$\delta = P/K(\text{mm})$	$P_{\text{single}}/k$	$\delta = \delta_s R_s$
$v_s = 0,15$	279,687	506,447	29,61	8,938	29,61
$v_s = 0,3$	296,012	558,168	26,87	8,445	26,87

$$\delta_{\text{measured}} = 13 \text{ mm}$$

### b) Equivalent Pier Method

$$B = A_G^{0.5} = 3,794$$

$$A_p = \pi d^2 n / 4 = 4,712 \text{ m}^2$$

$$E_p = 30000 \text{ MPa}$$

$$E_s' = 26,833 \text{ MPa} \quad E_u = 35 \text{ MPa}$$

$$d_e = 1,27 A_G^{0,5} = 4,819 \text{ (for friction piles)}$$

$$\rho = 1 \quad L = 15,5 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-v) L / r_0) \text{ (W. Fleming, et al., 1992)}$$

$$\zeta_2 = \ln / \{ 5 + [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L / r_0 \} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s = 0,15$	9835,530	843,045	2,615	0,193	3,176	0,232	27,02
			2,926	0,183	3,180	0,253	29,38
$v_s = 0,3$	9837,88	843,247	2,421	0,201	3,173	0,237	24,37
			2,788	0,187	3,179	0,263	26,98

### Method 2

$$L/d_e = 15,5 / 4,819 = 3,216 \rightarrow I_\delta = 0,25 \text{ (Fig. 2.10)}$$

	$v_s = 0,15$	$v_s = 0,3$
$\delta \text{ (mm)}$	28,99	25,65

$$K \approx 850 \text{ (pile stiffness factor)} \quad s/d \approx 1,8 \quad L/d \approx 15,5 \quad B = 3,794 \text{ m}$$

$$d_e/B \approx 0,93 \text{ assumed, then } d_e \approx 3,529 \text{ m (Fig. 2.9)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s = 0,15$	9835,530	843,045	2,926	0,250	4,302	0,201	31,91
			3,164	0,240	4,309	0,214	33,90
$v_s = 0,3$	9837,88	843,247	2,732	0,258	4,296	0,208	29,13
			3,014	0,246	4,305	0,223	31,36

### Method 2

$$L/d_e = 15,5 / 3,529 = 4,392 \rightarrow I_\delta = 0,215 \text{ (Fig. 2.10)}$$

$\delta$ (mm)	$v_s = 0,15$	$v_s = 0,3$
	34,05	30,12

$$\delta_{\text{measured}} = 13 \text{ mm}$$

### c) Equivalent Raft Method

$$L = 9,76 \quad B = 7,96 \quad L/B = 1,22$$

$$H = 15,92 \quad D = 10,3 \quad D/B = 1,293 \quad H/B = 2$$

$$\mu_0 = 0,91 \quad \mu_1 = 0,55$$

$$q_n = 15000 / (BL) = 193,076 \text{ KPa}$$

$$\delta_{\text{ave}} = q_n \mu_0 \mu_1 B / E_u = 193,076 \cdot 0,91 \cdot 0,55 \cdot 7,96 / 35 = 21,97 \text{ mm}$$

$$D/(LB)^{0,5} = 1,16 \rightarrow \mu_d = 0,7$$

Tough Clay  $\rightarrow \mu_g = 0,7$

$$z/B=1 \quad \sigma_z/q=0,3 \quad \sigma_z=57,92 \text{ KPa}$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)] \approx 0,0352$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g$$

$$= 0,0352 \cdot 57,92 \cdot 15,92 \cdot 0,7 \cdot 0,7 \approx 15,94 \text{ mm}$$

$$\delta_{T \text{ ave}} = \delta_i + \delta_c = \boxed{37,92 \text{ mm}}$$

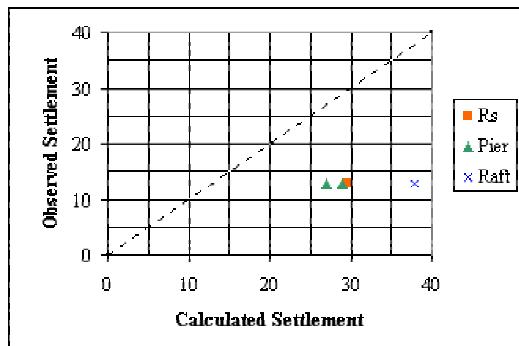
$$\delta_{\text{measured}} = 13 \text{ mm}$$

**Table A.3:** Measured and computed settlements for Frame Type Building 2 (mm)

Set. Ratio		Settlement (mm)						Mea.	
		Equivalent Pier				Equi. Raft			
		d <sub>e1</sub>		d <sub>e2</sub>		H=5,6 m	H=15,92 m		
		Met1	Met2	Met1	Met2	Ave.	Ave.	13,00	
vs=0,15		29,61	27,02	28,99	31,91	34,05	22,28	37,92	
			29,38		33,90				
vs=0,3		26,87	24,37	25,65	29,13	30,12	18,64	33,04	
			26,99		31,36				

Frame 2 (Though Clay)

Rs	29,61	Mea.	13
Pier	27,02		
	28,99		
Raft	37,92		



**Figure A.5:** Measured and computed settlements for Frame Type Building 2 (mm)

#### **4. Frame-Type Building 3 (n=9)**

The total structural load of 8,1 MN is supported on a group of 9 driven piles 35\*35 cm in section. Penetration depth is 15,5 m. The group has a plan area of 3\*3 m. At the site of the building tough plastic clay,  $E_u=35$  Mpa, is located. Different formulations are used to obtain settlement value. Settlement predictions and methods are given below:

USSR standarts    Poulos    Vesic    Skempton    Bartolomey:

40 mm    32 mm    9 mm    14 mm    6 mm

(Bartolomey, A.A., et al., 1981)

##### **a) Settlement Ratio Method**

$$n=9 \quad d=0,394 \text{ m} \quad r_0=0,197 \text{ m}$$

$$L=15,5 \text{ m} \quad s=1,182 \text{ m}$$

$$E_u=35 \text{ (MN/m}^2\text{)} \quad \text{Tough Plastic Clays} \quad E_p=25000 \text{ MN/m}^2$$

$$P=8,1 \text{ MN} \quad v_s=0,15 \quad v_s=0,3$$

$$\lambda=E_p/G_l=25000/11,7 \approx 2136,752$$

$$\rho=G_{l/2}/G_l=1 \rightarrow 1,06$$

$$\log \lambda = 3,329 \rightarrow 1,05$$

$$s/d=3 \rightarrow 1$$

$$L/d=39,34 \rightarrow 0,552$$

$$v_s=0,15 \rightarrow 1,035$$

$$v_s=0,3 \rightarrow 1$$

$$\eta_w = n^{-e} \quad R_s = n^e \quad \eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 1$$

$$\zeta = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et al., 1992})$$

$$\mu L = (2/(\lambda \zeta))^{0.5} L/r_0$$

$$P_{\text{single}} = 8100/9 = 900 \text{ KN}$$

	e	$\eta_w$	R <sub>s</sub>	$\zeta$	$\mu L$	$\tan \mu L L / (\mu L r_0)$	P <sub>t</sub> /(w <sub>t</sub> G <sub>b</sub> r <sub>0</sub> )
v <sub>s</sub> =0,15	0,635	0,247	4,043	5,119	1,064	58,213	73,169
v <sub>s</sub> =0,3	0,614	0,259	3,857	4,925	1,084	57,662	75,569

	P <sub>t</sub> /w <sub>t</sub>	K=n $\eta_w$ k	$\delta=P/K(\text{mm})$	P <sub>single</sub> /k	$\delta=\delta_s R_s$
v <sub>s</sub> =0,15	168,649	375,356	21,58	5,33	21,57
v <sub>s</sub> =0,3	174,17	406,419	19,93	5,16	19,93

$$\delta_{\text{measured}} = 5 \text{ mm}$$

### b) Equivalent Pier Method

$$B = A_G^{0.5} = 3$$

$$A_p = \pi d^2 n / 4 = 1,0973 \text{ m}^2$$

$$E_p = 25000 \text{ MPa} \quad E_s' = 26,833 \text{ MPa} \quad E_u = 35 \text{ MPa}$$

$$d_e = 1,27 A_G^{0.5} = 3,81 \text{ (for friction piles)}$$

$$\rho = 1 \quad L = 15,5 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et al., 1992})$$

$$\zeta_2 = \ln / \{ 5 + [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L/r_0 \} \quad (\text{K. Horikoshi, M. Randolph, 1999})$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,15$	3071,61	262,531	2,850	0,420	3,844	0,221	17,56
			3,104	0,403	3,861	0,236	18,71
$v_s=0,3$	3074,69	262,793	2,655	0,435	3,829	0,229	16,10
			2,957	0,412	3,852	0,248	17,38

### Method 2

$$L/d_e = 15,5 / 3,81 = 4,068 \rightarrow I_\delta = 0,222 \quad (\text{Fig. 2.10})$$

	$v_s=0,15$	$v_s=0,3$
$\delta \text{ (mm)}$	17,58	15,56

$$K \approx 700 \text{ (pile stiffness factor)} \quad s/d \approx 3 \quad L/d \approx 39,34 \quad B=3 \text{ m}$$

$$d_e/B \approx 0,85 \text{ assumed, then } d_e \approx 2,55 \text{ m} \quad (\text{Fig. 2.9})$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,15$	3071,61	262,531	3,251	0,588	5,462	0,189	22,41
			3,428	0,573	5,490	0,196	23,30
$v_s=0,3$	3074,69	262,793	3,057	0,606	5,428	0,199	20,89
			3,268	0,586	5,465	0,209	21,91

## Method 2

$$L/d_e = 15,5 / 2,55 = 6,078 \rightarrow I_\delta = 0,21 \quad (\text{Fig. 2.10})$$

$\delta$ (mm)	$v_s = 0,15$	$v_s = 0,3$
	24,86	21,99

$$\delta_{\text{measured}} = 5 \text{ mm}$$

### c) Equivalent Raft Method

$$L=7,96 \quad B=7,96 \quad L/B=1$$

$$H=15,92 \quad D=10,3 \quad D/B=1,29 \quad H/B=2$$

$$\mu_0=0,91 \quad \mu_1=0,53$$

$$q_n = 8100/(BL) = 127,83 \text{ KPa}$$

$$\delta_{i \text{ ave}} = q_n \mu_0 \mu_1 B / E_u = 127,83 \cdot 0,91 \cdot 0,53 \cdot 7,96 / 35 = 14,02 \text{ mm}$$

$$D/(LB)^{0,5} = 1,293 \rightarrow \mu_d = 0,685$$

$$\text{Tough Clay} \rightarrow \mu_g = 0,7$$

$$z/B=1 \quad \sigma_z/q = 0,272 \quad \sigma_z = 34,771 \text{ KPa}$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)] \approx 0,0353$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g$$

$$= 0,0353 \cdot 34,771 \cdot 15,92 \cdot 0,685 \cdot 0,7 \approx 9,37 \text{ mm}$$

$$\delta_{T \text{ ave}} = \delta_i + \delta_c = \boxed{23,39 \text{ mm}}$$

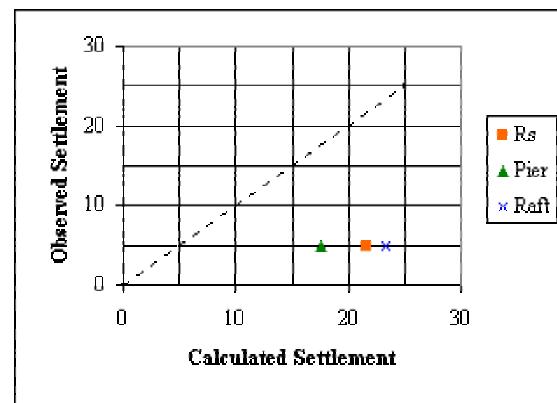
$$\delta_{\text{measured}} = 5 \text{ mm}$$

**Table A.4:** Measured and computed settlements for Frame Type Building 3 (mm)

		Settlement (mm)						Mea.	
Set. Ratio	vs=0,15	Equivalent Pier				Equi. Raft			
		d <sub>e1</sub>		d <sub>e2</sub>		H=5,588 m	H=7,96 m		
		Met1	Met2	Met1	Met2	Ave.	Ave.		
21,58	21,58	17,56		22,40		14,41	23,39	5,00	
		18,71	17,58	23,30					
19,93	vs=0,3	16,10		20,89		21,99	12,11	20,52	
		17,38	15,56	21,91					

Frame 3 (Though Clay)

Rs	21,58	Mea.	5
Pier	17,56		
	17,58		
Raft	23,39		



**Figure A.6:** Measured and computed settlements for Frame Type Building 3 (mm)

## **5. 9-Pile Group (n=9)**

The site consists of various layers of stiff to very stiff clay, and geotechnical data is available from standard penetration tests, cone penetration tests, pressuremeter tests, unconsolidated undrained triaxial tests, laboratory consolidation tests, and seismic cross-hole tests. The piles were about 13 m long, 0.273 m diameter steel tubes with a 9.3 mm wall thickness. The pile spacing in the group was three times the pile diameters, or 0.819 m. The programs DEFPIG (non-linear), PIGLET (simplified continuum analysis) and GAPFIX (non-linear) were employed and approximately 1.43, 1.43, 1.21 mm settlement predictions were obtained relatively. (H.G. Poulos ,(1989), M.Polo and M. Clemente, (1998))

### **a) Settlement Ratio Method**

$$n = 9 \text{ piles} \quad d = 0.273 \text{ m} \quad r_0 = 0.1365 \text{ m}$$

$$L = 13 \text{ m} \quad s/d = 3$$

$$P = 1.8 \text{ MN}$$

$$v_s = 0.15 \quad v_s = 0.33$$

$$1. E = 40 + 5.38z \quad E_u = 110 \text{ MPa} \quad G_l = 36.67 \text{ MPa}$$

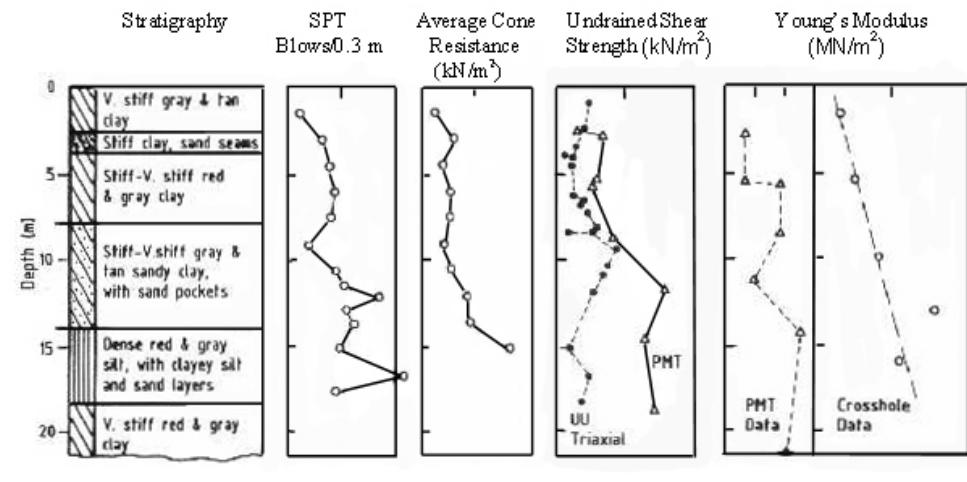
$$2. \text{ From Pressuremeter test} \quad E_u = 147 \text{ MPa} \quad G_l = 49 \text{ MPa}$$

$$3. E_u = 190 \text{ MPa} \quad G_l = 63.3 \text{ MPa}$$

$$E_p = 21000, 25000 \text{ MN/m}^2$$

$$\lambda = E_p/G_l$$

$$\rho = G_{l/2}/G_l$$



**Figure A.7:** Summary of geotechnical data at test site(Poulos, 1989, .Polo and Clemente, 1998)

$$s/d = 3 \rightarrow 1$$

$$L/d = 13/0,273 = 47,62 \rightarrow 0,549$$

$$v_s = 0,15 \rightarrow 1,04$$

$$v_s = 0,33 \rightarrow 1$$

$$\eta_w = n^{-e} \quad R_s = n^e$$

$$\zeta = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et al.1992})$$

$$\eta = r_b/r_0 = 1 \quad \xi = G_b/G_b = 1$$

$$\mu L = (2/(\lambda\zeta))^{0,5} L/r_0$$

$$P_{\text{single}} = 1800/9 = 200 \text{ KN}$$

	E' = 145,6	E_u = 168,4	E' = 112,7	E_u = 130,3	E' = 84,3	E_u = 97,5
e	0,467	0,449	0,515	0,495	0,520	0,500
$\eta_w$	0,358	0,372	0,322	0,336	0,318	0,332
R_s	2,791	2,683	3,100	2,968	3,139	3,004

$\zeta$	4,923	4,685	4,974	4,736	4,926	4,688
$\mu L$	3,333	3,417	2,673	2,740	2,325	2,383
$\tanh \mu L$	28,497	27,810	35,282	34,469	40,186	39,286
$L/(\mu L r_0)$						
$P_t/(w_t G_l r_0)$	26,047	26,992	33,113	34,240	36,404	37,703
$P_t/w_t$	225,17	233,33	221,47	229,01	182,36	188,87
$K=n\eta_w k$	725,87	782,49	642,79	694,24	522,74	565,76
$\delta=P/K(mm)$	2,48	2,30	2,80	2,59	3,44	3,18
$P_{single}/k$	0,88	0,85	0,90	0,87	1,09	1,05
$\delta=\delta_s R_s$	2,48	2,30	2,80	2,59	3,44	3,18

$$\delta_{measured}=0,9 \text{ mm}$$

### b) Equivalent Pier Method

$$B=A_G^{0.5}=2,73 \text{ m}$$

$$A_p=\Pi d^2 n/4=0,5268 \text{ m}^2$$

$$E_p=25000 \text{ MPa}$$

$$E=40+5,38z \quad E_s'=84,33 \text{ MPa} \quad E_u=110 \text{ MPa}$$

$$\text{From Pressuremeter test} \quad E_s'=112,7 \text{ MPa} \quad E_u=147 \text{ MPa}$$

$$E_u=190 \text{ MPa}$$

$$d_e=1,27 A_G^{0,5}=3,46 \text{ m (for friction piles)}$$

$$\rho=0,71-0,68-0,67 \quad L=13 \text{ m}$$

$$E_e=E_p A_p/A_G + E_s(1-A_p/A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-\nu) L/r_0) \text{ (W. Fleming, et.al 1992)}$$

$$\zeta_2 = \ln/\{5+[0,25+(2,5 \rho (1-\nu)-0,25)\xi] L/r_0\} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

	E'=145,6	E_u=168,4	E'=112,7	E_u=130,3	E'=84,3	E_u=97,5
E_e	1652,71	1673,86	1911,19	1927,55	1884,87	1897,12
$\lambda$	26,09	26,43	39,00	39,33	51,40	51,79
$\zeta_{(1-2)}$	2,39	2,15	2,44	2,11	2,39	2,06
	2,65	2,48	2,69	2,45	2,66	2,42
$\mu L$	1,35	1,42	1,09	1,17	0,96	1,03
	1,28	1,32	1,04	1,09	0,91	0,95
tanh $\mu L$	2,44	2,37	2,76	2,66	2,93	2,84
L/( $\mu L d_e$ )	2,52	2,48	2,82	2,77	2,99	2,94
$I_\delta$	0,43	0,46	0,37	0,38	0,35	0,35
	0,46	0,49	0,39	0,41	0,37	0,38
$\delta$	1,58	1,44	1,74	1,53	2,20	1,91
	1,66	1,55	1,84	1,65	2,34	2,07

## Method 2

$$L/d_e = 13/3,46 = 3,74 \rightarrow I_\delta = 0,22 \text{ (Fig. 2.10)}$$

	E'=145,6	E_u=168,4	E'=112,7	E_u=130,3	E'=84,3	E_u=97,5
$\delta$	0,79	0,68	1,02	0,88	1,37	1,18

$$K \approx 200 \text{ (pile stiffness factor)} \quad s/d \approx 3 \quad L/d \approx 47,6 \quad B=2,73 \text{ m}$$

$d_e/B \approx 0,75$  assumed, then  $d_e \approx 2,05$  m (Fig. 2.9)

	$E' = 145,6$	$E_u = 168,4$	$E' = 112,7$	$E_u = 130,3$	$E' = 84,3$	$E_u = 97,5$
$E_e$	1652,71	1673,86	1911,19	1927,55	1884,87	1897,12
$\lambda$	26,09	26,43	39,00	39,33	51,40	51,79
$\zeta_{(1-2)}$	2,90	2,66	2,95	2,62	2,91	2,58
	3,14	2,96	3,18	2,93	3,15	2,90
$\mu L$	2,05	2,13	1,67	1,76	1,47	1,55
	1,97	2,02	1,60	1,67	1,41	1,46
$\tanh \mu L$	2,98	2,88	3,53	3,38	3,88	3,73
$L/(\mu L d_e)$	3,08	3,02	3,63	3,53	3,99	3,89
$I_\delta$	0,45	0,49	0,37	0,39	0,35	0,36
	0,47	0,52	0,39	0,42	0,36	0,38
$\delta$	2,76	2,58	2,95	2,68	3,63	3,27
	2,87	2,71	3,06	2,82	3,79	3,47

## Method 2

$L/d_e = 13/2,05 = 6,34 \rightarrow I_\delta = 0,2$  (Fig. 2.10)

	$E' = 145,6$	$E_u = 168,4$	$E' = 112,7$	$E_u = 130,3$	$E' = 84,3$	$E_u = 97,5$
$\delta$	1,20	1,04	1,55	1,34	2,08	1,80

$\delta_{\text{measured}} = 0,9$  mm

### c) Equivalent Raft Method

$$L=7,07 \text{ m} \quad B=7,07 \text{ m} \quad H=14,06 \text{ m}$$

$$L/B=1 \quad D/B=1,23 \quad H/B=2$$

$$P=1800 \text{ kN} \quad q_n=1800/(BL)=36,01 \text{ KPa} \quad v_s=0,15$$

$$E=40+5,38z \quad E_s'_{\text{mid}}=77,56 \text{ MPa} \quad E_u_{\text{mid}}=101,17 \text{ MPa}$$

$$\text{From Pressuremeter test} \quad E_s'_{\text{mid}}=104 \text{ MPa} \quad E_u_{\text{mid}}=136 \text{ MPa}$$

$$E_s'_{\text{mid}}=133,64 \text{ MPa} \quad E_u_{\text{mid}}=174,32 \text{ MPa}$$

$$\mu_l=0,536 \quad \mu_0=0,91$$

$$\delta_{i \text{ ave}}=\mu_l \mu_0 q_n B / E_u = 0,91 \cdot 0,536 \cdot 36,42 \cdot 7,03 / 101,17 = 1,23 \text{ mm}$$

$$= 0,91 \cdot 0,536 \cdot 36,42 \cdot 7,03 / 136 = 0,91 \text{ mm}$$

$$= 0,91 \cdot 0,536 \cdot 36,42 \cdot 7,03 / 147,32 = 0,71 \text{ mm}$$

$$D/(LB)^{0,5}=1,23 \rightarrow \mu_d=0,68$$

$$\text{stiff clay} \rightarrow \mu_g=0,7$$

$$z/B=1 \quad \sigma_z/q=0,27 \quad \sigma_z=9,83 \text{ KPa}$$

$$m_v=[(1+v)(1-2v)]/[E'(1-v)] \approx 0,0122 - 0,0091 - 0,0070$$

$$\delta_c=m_v \sigma_z H \mu_d \mu_g$$

$$= 0,0122 \cdot 9,83 \cdot 14,6 \cdot 0,68 \cdot 0,7 \approx 0,803 \text{ mm}$$

$$= 0,0091 \cdot 9,83 \cdot 14,6 \cdot 0,68 \cdot 0,7 \approx 0,599 \text{ mm}$$

$$= 0,0070 \cdot 9,83 \cdot 14,6 \cdot 0,68 \cdot 0,7 \approx 0,466 \text{ mm}$$

$$\delta_T=\delta_{i \text{ ave}}+\delta_c = 2,03 - 1,51 - 1,18 \text{ mm}$$

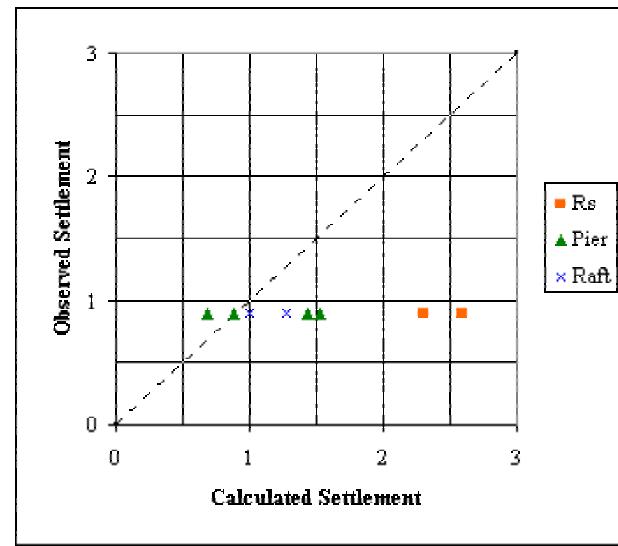
$$\delta_{\text{measured}}=0,9 \text{ mm}$$

**Table A.5:** Measured and computed settlements for 9-Pile Group (mm)

Settlement (mm)																
Settlement Ratio				Equivalent Pier												
				de1				de2								
				Met1				Met2				Met1				
E <sub>s</sub> =	E <sub>p</sub> =25000	E <sub>p</sub> =21000	E <sub>p</sub> =25000	E <sub>p</sub> =21000	147	110	190	147	110	190	147	E <sub>p</sub> =25000	E <sub>p</sub> =21000	Met2		
vs=0,15	2,80	3,44	2,48	1,74	2,20	1,58		1,02	1,37	0,79	2,95	3,63	2,76	1,55	2,08	1,20
				1,84	2,34	1,66					3,06	3,79	2,87			
vs=0,33	2,59	3,18	2,30	1,53	1,91	1,44		0,88	1,18	0,68	2,68	3,27	2,58	1,34	1,80	1,04
				1,65	2,07	1,55					2,82	3,47	2,71			

Equivalent Raft							Mea.	
Eu=110		Eu=147		Eu=190				
H (m)	Ave.	Ave.	Ave.	Ave.	Ave.	Ave.		
vs=0,15	1,28	2,03	0,95	1,51	0,74	1,09		
vs=0,33	1,02	1,72	0,76	1,28	0,59	1,00	0,90	

9-Pile Group		
Rs	2,59	Mea. 0,9
	2,30	
Pier	1,53	
	0,88	
	1,44	
	0,68	
Raft	1,00	
	1,28	



**Figure A.8:** Measured and computed settlements for 9-Pile Group (mm)

## **6. Frame-Type Building 7 (n=16)**

The total structural load of 16 MN is supported on a group of 16 piles 40\*40 cm in section. Distance between piles varies from 1,2 to 1,6 and penetration depth is 20 m. The group has a plan area of 4,5\*5 m. At the site of the building shingle,  $E_u=80$  MPa is located. Different formulations are used to obtain settlement value. Settlement predictions and methods are given below:

USSR standards    Poulos    Vesic    Skempton    Bartolomey:

40 mm    32 mm    9 mm    14 mm    6 mm

(Bartolomey, A.A., et al., 1981)

### **a) Settlement Ratio Method**

$$n = 16 \quad d = 0,4512 \text{ m} \quad r_0 = 0,2256 \text{ m}$$

$$L = 20 \text{ m} \quad s = 1,4 \text{ m}$$

$$E_u = 80 \text{ MN/m}^2 \quad \text{Shingle} \quad E_p = 25000 \text{ MN/m}^2$$

$$P = 16 \text{ MN} \quad v_s = 0,35 \quad v_s = 0,4$$

$$\lambda = E_p/G_l = 25000/26,7 \approx 936,329$$

$$\rho = G_{l/2}/G_l = 1 \rightarrow 1,06$$

$$\log \lambda = 2,971 \rightarrow 0,99$$

$$s/d = 3,1 \rightarrow 1$$

$$L/d = 44,326 \rightarrow 0,55$$

$$v_s = 0,35 \rightarrow 0,98$$

$$v_s = 0,4 \rightarrow 0,97$$

$$\eta_w = n^{-e} \quad R_s = n^e \quad \eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 1$$

$$\zeta = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et al., 1992})$$

$$\mu L = (2/(\lambda\zeta))^{0.5} L/r_0$$

$$P_{\text{single}} = 16000/16 = 1000 \text{ KN}$$

	e	$\eta_w$	R_s	$\zeta$	$\mu L$	$\tan \mu L \cdot L / (\mu L \cdot r_0)$	$P_t / (w_t G_l r_0)$
$v_s = 0,35$	0,565	0,208	4,798	4,970	1,837	45,854	58,508
$v_s = 0,4$	0,559	0,211	4,722	4,890	1,852	45,551	59,093

	$P_t/w_t$	K = n $\eta_w k$	$\delta = P/K(\text{mm})$	$P_{\text{single}}/k$	$\delta = \delta_s R_s$
$v_s = 0,35$	352,426	1175,185	13,61	2,83	13,61
$v_s = 0,4$	355,949	1206,079	13,26	2,81	13,26

$$\delta_{\text{measured}} = 4 \text{ mm}$$

### b) Equivalent Pier Method

$$B = A_G^{0.5} = 4,763$$

$$A_p = \pi d^2 n / 4 = 2,558 \text{ m}^2$$

$$E_p = 25000 \text{ MPa}$$

$$E_s' = 72 \text{ MPa} \quad E_u = 80 \text{ MPa}$$

$$d_e = 1,13 \quad A_G^{0.5} = 5,36 \quad (\text{for end-bearing piles})$$

$$\rho = 1 \quad L = 20 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et al, 1992})$$

$$\zeta_2 = \ln/\{5+[0,25+(2,5 \rho (1-v)-0,25)\xi] L/r_0\} \quad (\text{K. Horikoshi, M. Randolph, 1999})$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,35$	2906,347	108,852	2,495	0,640	3,293	0,265	11,01
			2,840	0,600	3,339	0,289	11,98
$v_s=0,4$	2908,71	108,94	2,415	0,650	3,281	0,266	10,63
			2,784	0,605	3,333	0,291	11,65

### Method 2

$$L/d_e = 20/5,36 = 3,731 \rightarrow I_\delta = 0,23 \quad (\text{Fig. 2.10})$$

$\delta$ (mm)	$v_s=0,35$	$v_s=0,4$
	9,53	9,198

$$K \approx 300 \text{ (pile stiffness factor)} \quad s/d \approx 3,1 \quad L/d \approx 44,32 \quad B=4,74 \text{ m}$$

$$d_e/B \approx 0,75 \text{ assumed, then } d_e \approx 3,55 \text{ m} \quad (\text{Fig. 2.9})$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,35$	2906,347	108,852	2,905	0,894	4,485	0,245	15,33
			3,147	0,859	4,553	0,258	16,13
$v_s=0,4$	2908,71	108,94	2,825	0,906	4,462	0,247	14,93
			3,084	0,867	4,537	0,262	15,78

## **Method 2**

$$L/d_e = 20/3,557 = 5,621 \rightarrow I_\delta = 0,21 \quad (\text{Fig. 2.10})$$

$\delta$ (mm)	$v_s = 0,35$	$v_s = 0,4$
	13,11	12,65

$$\delta_{\text{measured}} = 4 \text{ mm}$$

### **c) Equivalent Raft Method**

$$L=5 \quad B=4,5 \quad L/B=1,11$$

$$H=9 \quad D=20 \quad D/B=4,444 \quad H/B=2$$

$$\mu_0=0,88 \quad \mu_1=0,53$$

$$q_n = 16000/(BL) = 711,11 \text{ KPa}$$

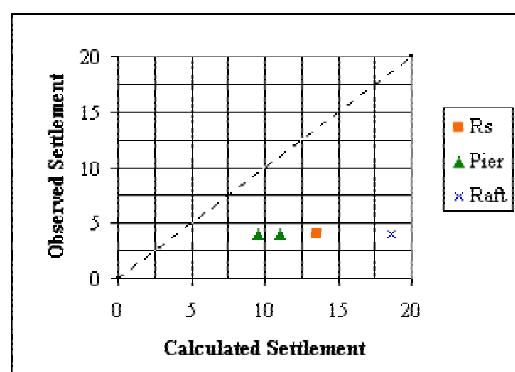
$$\delta_{\text{ave}} = q_n \mu_0 \mu_1 B / E_u = 71,11 \cdot 0,88 \cdot 0,53 \cdot 4,5 / 80 = 18,656$$

$$\delta_{\text{measured}} = 4 \text{ mm}$$

**Table A.6:** Measured and computed settlements for Frame Type Building 7 (mm)

Set. Ratio		Settlement (mm)				Mea.	
		Equivalent Pier		Eq. Raft			
		$d_{e1}$		$d_{e2}$			
		Met1	Met2	Met1	Met2		
$v_s=0,35$	13,61	11,01	9,53	15,33	13,11	4,00	
		11,98		16,13			
$v_s=0,4$	13,26	10,63	9,19	14,93	12,65	18,65	
		11,65		15,78			

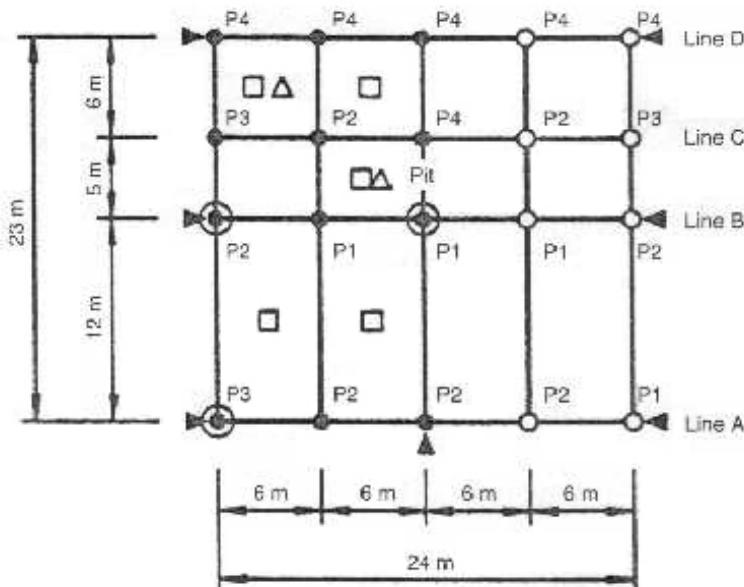
Frame 7 (Shingle)  
 Rs 13,61      Mea. 4  
 Pier 11,01  
     9,53  
 Raft 18,65



**Figure A.9:** Measured and computed settlements for Frame Type Building 7 (mm)

## 7. Five-storey Building in Urawa-Japan (n=20)

A piled raft foundation has been adopted in Japan for a five-storey building with plan area measuring 24 m by 23 m. The foundation consisted of a raft (0.3 m thick) with 20 piles, one under each column. The piles were bored concrete piles, either 0.8 or 0.7 m in diameter, with a central steel H-pile inserted. The pile diameter and steel pile size depended on the column load, which ranged between 1.02 MN and 3.95 MN. The GASGROUP (using superposition principle, with interaction factors) analysis yielded a settlement ratio,  $R_s$ , of 2,516, and predicted settlement of the pile group is calculated as 12,6 mm. The average settlement computed by program GARP (plate on springs approach) is 13,5 mm. (Poulos, H.G., 2001, Yamashita, K. et al, 1993, Randolph, M. and Guo, W., 1999)



**Figure A.10:** Five-storey building in Japan, foundation plan (Yamashita et al, 1993)

### a) Settlement Ratio Method

$$n = 20 \text{ piles} \quad d = 0,75 \text{ m} \quad r_0 = 0,375 \text{ m}$$

$$L = 15,8 \text{ m} \quad s \approx 5,25 \text{ m} \quad E_p = 25000 \text{ MN/m}^2$$

$$E_{u(\text{ave})} = 42,5 \text{ MPa} \text{ (loose to medium sand)}$$

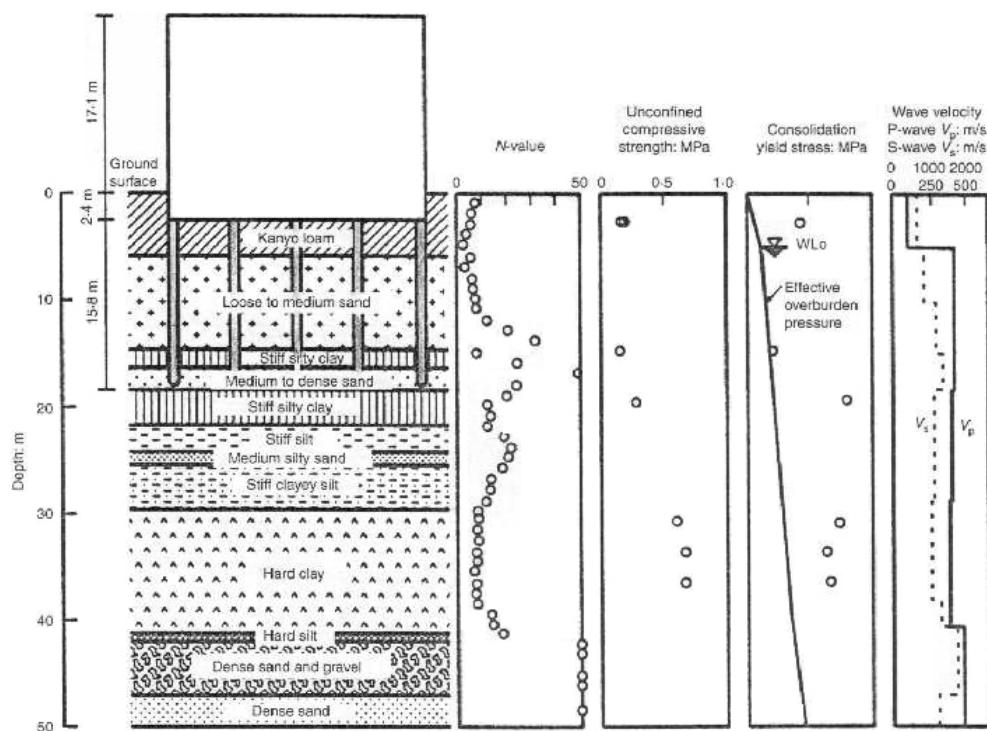
$$E_{u(\text{ave})} = 60 \text{ MPa} \text{ (stiff cohesive soil)}$$

$$P = 23 \text{ MN}$$

$$v_s = 0,2 \quad v_s = 0,3$$

$$\lambda = E_p/G_l = 25000/20 \approx 1250$$

$$\rho = G_{l/2}/G_l = 0,71 \rightarrow 0,98$$



**Figure A.11:** Elevation of building and summary of soil investigation (Yamashita et al, 1993)

$$\log \lambda = 3,09 \rightarrow 1,02$$

$$s/d = 7 \rightarrow 0,78$$

$$L/d = 21,06 \rightarrow 0,538$$

$$v_s = 0,2 \rightarrow 1,03$$

$$v_s = 0,3 \rightarrow 1$$

$$\eta_w = n^{-e} \quad R_s = n^e$$

$$\zeta = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et al., 1992})$$

$$\eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 1 \quad \mu L = (2/(\lambda \zeta))^{0,5} L/r_0$$

$$P_{\text{single}} = 23000/20 = 1150 \text{ KN}$$

	$e$	$\eta_w$	$R_s$	$\zeta$	$\mu L$	$\tanh \mu L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s = 0,2$	0,432	0,274	3,648	4,091	0,833	34,497	40,820
$v_s = 0,3$	0,538	0,284	3,513	3,958	0,847	34,296	42,261

	$P_t/w_t$	$K = n \eta_w k$	$\delta = P/K(\text{mm})$	$P_{\text{single}}/k$	$\delta = \delta_s R_s$
$v_s = 0,2$	306,15	1678,21	13,70	3,75	13,70
$v_s = 0,3$	316,96	1804,21	12,74	3,62	12,74

$$\delta_{\text{measured}} = 12,65 \text{ mm}$$

### Equivalent Pier Method

$$B = A_G^{0.5} = 24,24 \text{ m}$$

$$A_p = \Pi d^2 n / 4 = 8,836 \text{ m}^2$$

$E_p=25000 \text{ MPa}$

$E_s'=48 \text{ MPa} \quad E_u=60 \text{ MPa}$

$d_e=1,27 A_G^{0,5}=30,79 \text{ m}$  (for friction piles)

$\rho=0,71 \quad L=15,8 \text{ m}$

$E_e=E_p A_p / A_G + E_s (1 - A_p / A_G)$

$\zeta_1=\ln(2,5 \rho (1-\nu) L/r_0)$  (W. Fleming, et al., 1992)

$\zeta_2=\ln/\{5+[0,25+(2,5 \rho (1-\nu)-0,25)\xi] L/r_0\}$  (K. Horikoshi, M. Randolph, 1999)

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,2$	423,067	21,153	0,376	0,514	0,472	0,317	4,94
			1,864	0,231	0,504	0,696	10,84
$v_s=0,3$	427,007	21,350	0,243	0,637	0,453	0,250	3,59
			1,836	0,231	0,504	0,691	9,93

### Method 2

$L/d_e=15,8/30,79=0,513 \rightarrow I_\delta=0,5$  (Fig. 2.10)

	$v_s=0,2$	$v_s=0,3$
$\delta \text{ (mm)}$	7,78	7,18

$K \approx 420$  (pile stiffness factor)     $s/d \approx 7$      $L/d \approx 21,06$      $B=24,24$

$d_e/B \approx 0,78$  assumed, then  $d_e \approx 18,91 \text{ m}$  (Fig. 2.9)

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,2$	423,067	21,153	0,864	0,552	0,759	0,416	10,55
			1,997	0,363	0,800	0,627	15,89
$v_s=0,3$	427,007	21,350	0,730	0,598	0,748	0,394	9,232
			1,956	0,365	0,800	0,631	14,76

### Method 2

$$L/d_e = 15,8/18,91 = 0,835 \rightarrow I_\delta = 0,45 \text{ (Fig.2.10)}$$

	$v_s=0,2$	$v_s=0,3$
$\delta \text{ (mm)}$	11,40	10,52

$$\delta_{\text{measured}} = 12,65 \text{ mm}$$

### Equivalent Raft Method

$$P = 23000 \text{ KN}$$

$$q_n = P / (BL)$$

$$\delta_{\text{ave}} = \mu_1 \mu_0 q_n B / E$$

$q_n$	L	B	L/B	D	H	D/B	H/B	$\mu_0$	$\mu_1$	$E_u$	$\delta_i$
30,45	30	29	1,034	12,93	5,3	0,445	0,182	0,93	0,045	42,5	0,869
21,03	36	35	1,028	18,2	11,8	0,52	0,337	0,93	0,1	60	1,141
											$\Sigma 2,01$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)]$$

for sand  $q_c/N=5$   $q_c \approx 5 \text{ MPa}$   $M_0=4q_c$

$$\delta_c = m_v \sigma_z H m_d m_g$$

$$D/(LB)^{0.5} = 0,438 \rightarrow \mu_d = 0,87$$

Silt and sand  $\rightarrow \mu_g = 1$

$z/B$	$\sigma_z/q$	$\sigma_z$	$E_{\text{mid-dr}}$	$v$	$H$	$m_v$	$\mu_g$	$\mu_d$	$\delta_c$
0,091	0,88	23,26	36,8	0,3	5,3	0,05	1	0,87	5,36
0,386	0,6	15,86	48	0,2	11,8	0,0187	1	0,87	3,05
									$\Sigma 8,41$

$$\delta_T = \delta_i + \delta_c = 2,01 + 8,41 = \boxed{10,42 \text{ mm}}$$

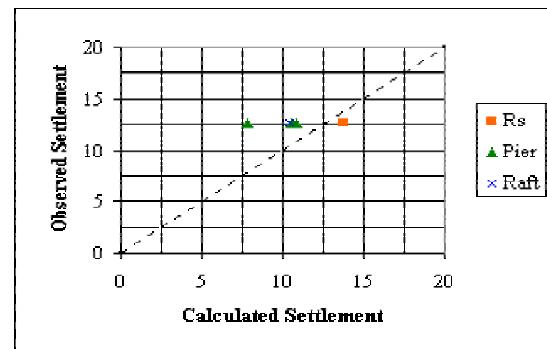
$\delta_{\text{measured}} = 12,5 \text{ mm}$

**Table A.7:** Measured and computed settlements for Five-Storey Building in Urawa Japan (mm)

Set. Ratio		Settlement (mm)					Mea.	
		Equivalent Pier				Eq. Raft		
		d <sub>e1</sub>		d <sub>e2</sub>				
Met1	Met2	Met1	Met2	Ave.				
vs=0,2	13,70	4,94	7,78	10,55	11,40	10,43	12,65	
		10,84		15,89				
vs=0,3	12,74	3,60	7,18	9,23	10,52			
		9,93		14,76				

Urawa - Japan

Rs	13,7	Mea.	12,65
Pier	10,84		
	7,78		
	10,55		
Raft	10,43		



**Figure A.12:** Measured and computed settlements for Five-Storey Building in Urawa Japan (mm)

## **8. Eurotheum Building (n=25)**

The basement and raft of the new high-rise Eurotheum building are loaded eccentrically by a 110 m high office tower, 28.1 m square in plan, which is surrounded by a six-storey apartment building. The foundation level is 11,5-13 m below street level and 6 m below the groundwater level. Frankfurt limestone exists 55 m below the ground surface. The building is founded on a piled raft with a thickness of 1.0-2.5 m and a plan area of 2000 m<sup>2</sup>, together with 25 bored piles which are concentrated beneath the eccentrically placed core of the skyscraper. The length of the 1.5 m diameter bored piles depends on their location, varying from 25 m for the corner piles, to 27.5 m for the edge piles and 30 m for the inner piles. (Katzenbach, R., Arslan,U., and Moormann, C., 2000)

### **a) Settlement Ratio Method**

$$n = 25 \quad d = 1,5 \text{ m} \quad r_0 = 0,75 \text{ m}$$

$$L = 27,5 \text{ m} \quad s = 4 \text{ m}$$

$$G = 20 + 1,0z \text{ MN/m}^2 \quad \text{Frankfurt clay} \quad E_p = 35000 \text{ MN/m}^2$$

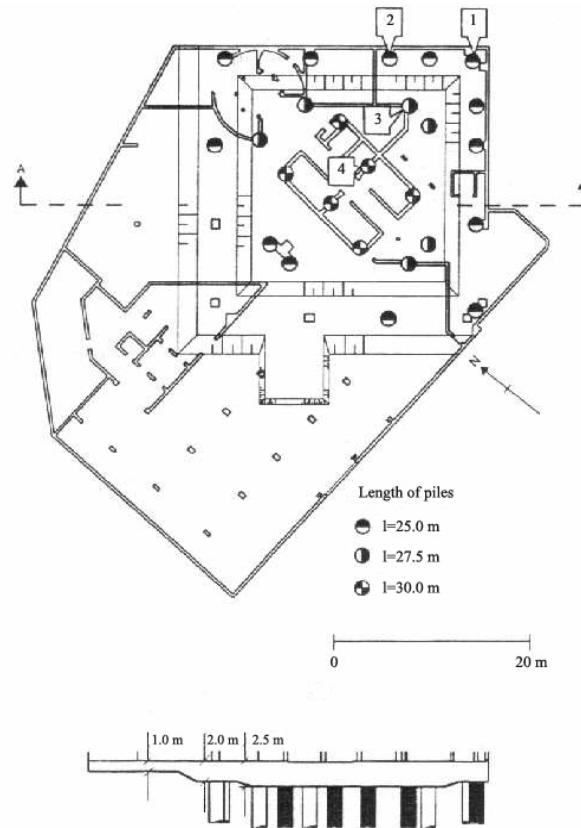
$$E_u = 20000 \text{ MN/m}^2 \quad \text{Frankfurt Limestone}$$

$$v_s = 0,1 \quad v_s = 0,3$$

$$P = 570 \text{ MN}$$

$$\lambda = E_p / G_l = 35000 / 52,5 \approx 666,667$$

$$\rho = G_{l/2} / G_l = 0,742 \rightarrow 1$$



**Figure A.13:** Piled raft foundation for Eurotheum building, plan and section A-A  
 (Katzenbach et al, 2000)

$$\log \lambda = 2,823 \rightarrow 0,96$$

$$s/d = 4 \rightarrow 0,93$$

$$L/d = 18,33 \rightarrow 0,533$$

$$v_s = 0,1 \rightarrow 1,05$$

$$v_s = 0,3 \rightarrow 1$$

$$\eta_w = n^{-e} \quad R_s = n^e$$

$$\zeta = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et al., 1992})$$

$$\eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 0,0078$$

$$\mu L = (2/(\lambda\zeta))^{0.5} L/r_0$$

$$P_{\text{single}} = 570000/25 = 22800 \text{ KN}$$

	e	$\eta_w$	R_s	$\zeta$	$\mu L$	$\tanh \mu L L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s=0,1$	0,499	0,200	4,994	2,259	1,336	23,895	82,501
$v_s=0,3$	0,475	0,216	4,626	2,248	1,339	23,858	83,657

	$P_t/w_t$	$K=n\eta_w k$	$\delta=P/K(mm)$	$P_{\text{single}}/k$	$\delta=\delta_s R_s$
$v_s=0,1$	3248,507	16260,56	35,05	7,018	35,05
$v_s=0,3$	3294,021	17800,79	32,02	6,921	32,02

$$\delta_{\text{measured}} = 32 \text{ mm}$$

### b) Equivalent Pier Method

$$B = A_G^{0.5} = 28,1 \text{ m}$$

$$A_p = \pi d^2 n / 4 = 44,178 \text{ m}^2$$

$$E_p = 35000 \text{ MPa} \quad E_s' = 1155 \text{ MPa} \quad E_u = 157,5 \text{ MPa}$$

$$d_e = 1,13 A_G^{0.5} = 31,753 \text{ m} \text{ (for end-bearing piles)}$$

$$\rho = 0,742 \quad L = 27,5 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-v) L / r_0) \text{ (W. Fleming, et al., 1992)}$$

$$\zeta_2 = \ln / \{ 5 + [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L / r_0 \} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,1$	2067,29	39,376	-0,793				
			1,696	0,299	0,841	0,067	10,42
$v_s=0,3$	2087,11	39,754	-0,804				
			1,695	0,298	0,841	0,076	10,09

### Method 2

$$L/d_e = 27,5/31,753 = 0,866 \rightarrow I_\delta = 0,025 \text{ (Fig. 2.10)}$$

$\delta$ (mm)	$v_s=0,1$	$v_s=0,3$
	3,88	3,28

$$K \approx 200 \text{ (pile stiffness factor)} \quad s/d \approx 4 \quad L/d \approx 18,33 \quad B=28,1 \text{ m}$$

$$d_e/B \approx 0,78 \text{ assumed, then } d_e \approx 21,918 \text{ m (Fig. 2.9)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,1$	2067,29	39,376	-0,422				
			1,732	0,429	1,182	0,090	20,46
$v_s=0,3$	2087,11	39,754	-0,433				
			1,731	0,427	1,183	0,104	19,96

$$\delta_{\text{measured}} = 32 \text{ mm}$$

## Method 2

$$L/d_e = 27,5/21,918 = 1,25 \rightarrow I_\delta = 0,03 \text{ (Fig. 2.10)}$$

	$v_s = 0,1$	$v_s = 0,3$
$\delta \text{ (mm)}$	6,75	5,71

$$\delta_{\text{measured}} = 32 \text{ mm}$$

### c) Equivalent Raft Method

$$L=28,1 \quad B=28,1 \quad L/B=1$$

$$H=14,5 \quad D=40,5 \quad H/B=0,516 \quad D/B=1,441$$

$$E_{\text{uave}}=176,25 \quad E_s' = 131,45$$

$$\mu_0 \rightarrow 0,905 \quad \mu_1 \rightarrow 0,168$$

$$\delta_{\text{iave}} = q_n B \mu_0 \mu_1 / E_u = 17,20 \text{ mm}$$

$$D/(LB)^{0,5} = 1,441 \rightarrow \mu_d = 0,68$$

$$\text{Frankfurt clay} \rightarrow \mu_g = 0,7$$

$$z/B=0,258 \quad \sigma_z/q=0,727 \quad \sigma_z=524,803 \text{ Kpa}$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)] \approx 0,00743$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g$$

$$= 0,00743 \cdot 524,803 \cdot 14,5 \cdot 0,68 \cdot 0,7 \approx 26,94 \text{ mm}$$

$$\delta_{\text{Taverage}} = 17,20 + 26,94 = 44,15 \text{ mm}$$

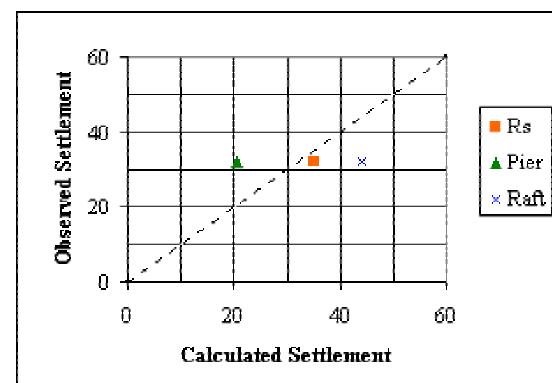
$$\delta_{\text{measured}} = 32 \text{ mm}$$

**Table A.8:** Measured and computed settlements for Eurotheum Building (mm)

Set. Ratio		Settlement (mm)						Mea.	
		Equivalent Pier				Equivalent Raft			
		d <sub>e1</sub>		d <sub>e2</sub>		H=23,66 m (end-bearing piles)	H=14,5 m (friction piles)		
Met1	Met2	Met1	Met2	Ave.	Ave.				
vs=0,1	35,05		3,88		6,75	46,71	44,15	32,00	
		10,42		20,47					
vs=0,3	32,02		3,28		5,71	36,71	34,52		
		10,09		19,96					

Eurotheum

Rs	35,05	Mea.	32
Pier	20,47		
Raft	44,15		



**Figure A.14:** Measured and computed settlements for Eurotheum Building (mm)

## **9. Japan Centre (n=25)**

The 115.3 m high Taunustor-Japan-Centre office tower is located in the centre of the financial district of Frankfurt am Main. The building comprises four basement floors and eccentrically placed tower with 29 floors above grade having dimensions of 36,6\*36,6 m in plan. The total structural load of 1050 MN is supported on a piled raft 15,8 m below the ground surface, which is about 9,5 m below the groundwater table. The raft has a thickness of 3,0 m at the centre, reducing 1,0 m at the edges. The raft is loaded with a remarkable eccentricity in the building load of 7.5. Therefore the positions of the 25 bored piles (diameter 1.3 m, length 22 m) under the raft were optimised during the design to guarantee fairly constant settlements over the entire foundation. At the site of the Japan-Centre building, the boundary between the Frankfurt Clay and the rocky Frankfurt Limestone is located approximately 43 m below the ground surface, which is only about 5 m below the base level of the piles. (Katzenbach, R., Arslan,U., and Moormann, C., 2000)

### **a) Settlement Ratio Method**

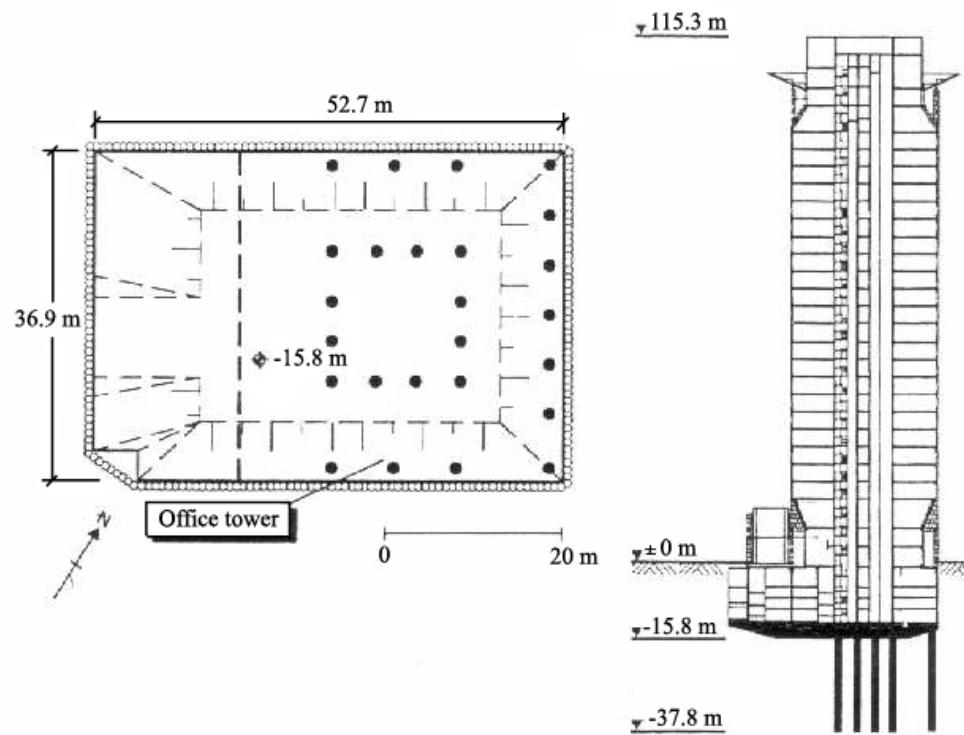
$$n = 25 \quad d = 1,3 \text{ m} \quad r_0 = 0,65 \text{ m}$$

$$L = 22 \text{ m} \quad s = 4,5 \text{ m}$$

$$G = 20 + 1,0z \text{ (MN/m}^2\text{)} \quad \text{Frankfurt Clay} \quad E_p = 30000 \text{ MN/m}^2$$

$$E_u = 20000 \text{ MN/m}^2 \quad \text{Frankfurt Limestone}$$

$$P = 1050 \text{ MN} \quad v_s = 0,1 \quad v_s = 0,3$$



**Figure A.15:** Japan Centre building, ground plan and sectional elevation  
(Katzenbach et al, 2000)

$$\lambda = E_p / G_l = 30000 / 47,8 \approx 627,615$$

$$\rho = G_{l/2} / G_l = 0,769 \rightarrow 1$$

$$\log \lambda = 2,797 \rightarrow 0,95$$

$$s/d = 4,5 \rightarrow 0,9$$

$$L/d = 16,92 \rightarrow 0,528$$

$$v_s = 0,1 \rightarrow 1,05$$

$$v_s = 0,3 \rightarrow 1$$

$$\eta_w = n^e \quad R_s = n^e \quad \eta = r_b / r_0 = 1 \quad \xi = G_l / G_b = 0,00717$$

$$\zeta = \ln(2,5 \rho (1-v) L / r_0) \quad (\text{W. Fleming, et al., 1992})$$

$$\mu L = (2/(\lambda\zeta))^{0.5} L/r_0$$

$$P_{\text{single}} = 1050000/25 = 42000 \text{ KN}$$

	e	$\eta_w$	R_s	$\zeta$	$\mu L$	$\tan \mu L L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s=0,1$	0,474	0,217	4,598	2,177	1,294	22,489	83,000
$v_s=0,3$	0,451	0,233	4,276	2,167	1,298	22,455	84,066

	$P_t/w_t$	$K=n\eta_w k$	$\delta=P/K(\text{mm})$	$P_{\text{single}}/k$	$\delta=\delta_s R_s$
$v_s=0,1$	2578,838	14019,22	74,89	16,28	74,89
$v_s=0,3$	2611,93	15269,22	68,76	16,08	68,76

$$\delta_{\text{measured}} = 50 \text{ mm}$$

### b) Equivalent Pier Method

$$B = A_G^{0.5} = 32,012 \text{ m}$$

$$A_p = \pi d^2 n / 4 = 33,183 \text{ m}^2$$

$$E_p = 30000 \text{ MPa}$$

$$E_s' = 105,16 \text{ MPa} \quad E_u = 143,4 \text{ MPa}$$

$$d_e = 1,13 A_G^{0.5} = 36,174 \text{ (for end-bearing piles)}$$

$$\rho = 0,769 \quad L = 22 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-v) L / r_0) \text{ (W. Fleming, et al., 1992)}$$

$$\zeta_2 = \ln / \{ 5 + [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L / r_0 \} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,1$	1073,16	22,450	-1,148				
$v_s=0,3$	1091,66	22,838	1,670	0,280	0,592	0,080	22,24
			-1,27				
			1,670	0,278	0,593	0,092	21,50

### Method 2

$$L/d_e = 22/36,174 = 0,541 \rightarrow I_\delta = 0,02 \quad (\text{Fig. 2.10})$$

$\delta$ (mm)	$v_s=0,1$	$v_s=0,3$
	5,52	4,67

$$K \approx 210 \text{ (pile stiffness factor)} \quad s/d \approx 4,5 \quad L/d \approx 16,9 \quad B=32,012 \text{ m}$$

$$d_e/B \approx 0,75 \text{ assumed, then } d_e \approx 24,009 \text{ m} \quad (\text{Fig. 2.9})$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,1$	1073,160	22,450	-0,738				
$v_s=0,3$	1091,66	22,838	1,700	0,419	0,866	0,114	47,51
			-0,749				
			1,699	0,415	0,866	0,131	46,22

## Method 2

$$L/d_e = 22/24,001 = 0,916 \rightarrow I_\delta = 0,025 \text{ (Fig. 2.10)}$$

$\delta$ (mm)	$v_s = 0,1$	$v_s = 0,3$
	10,39	8,79

$$\delta_{\text{measured}} = 50 \text{ mm}$$

### c) Equivalent Raft Method

$$L=36,6 \quad B=27 \quad L/B=1,355$$

$$H=5 \quad D=37,8 \quad D/B=1,4 \quad H/B=0,185$$

$$E_{\text{uave}}=156,9 \quad E_s' = 115,06$$

$$\mu_0 \rightarrow 0,92 \quad \mu_1 \rightarrow 0,04$$

$$q_n = 1050000/(BL) = 1062,53 \text{ KPa}$$

$$\delta_{\text{iave}} = q_n B \mu_0 \mu_1 / E_u = 8,31 \text{ mm}$$

$$D/(LB)^{0,5} = 1,202 \rightarrow \mu_d = 0,695$$

$$\text{Frankfurt Clay} \rightarrow \mu_g = 0,7$$

$$z/B = 2,5/27 = 0,092 \quad \sigma_z/q = 0,9 \quad \sigma_z = 956,28 \text{ KPa}$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)] \approx 0,00849$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g = 0,00849 \cdot 956,28 \cdot 5 \cdot 0,695 \cdot 0,7 \approx 19,76 \text{ mm}$$

$$\delta_{\text{Taverage}} = 28,08 \text{ mm}$$

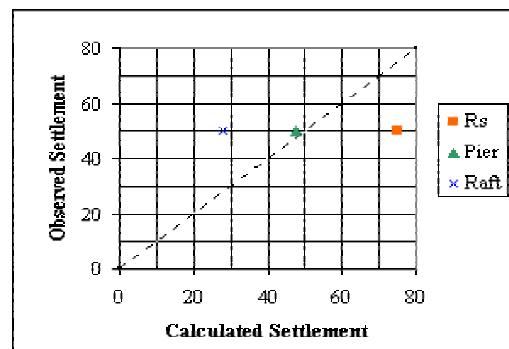
$$\delta_{\text{measured}} = 50 \text{ mm}$$

**Table A.9:** Measured and computed settlements for Japan-Centre Building (mm)

		Settlement (mm)								Mea.	
Set. Ratio	B*L(36,6*36,6)	Equivalent Pier						B*L (28*36,6)			
		d <sub>e1</sub>		d <sub>e2</sub>		d <sub>e1</sub>					
		Met1	Met2	Met1	Met2	Met1	Met2	Ave.			
vs=0,1	74,89		4,82		9,09		5,52	47,51	10,39	28,08	50
		21,43		45,94		22,24					
vs=0,3	68,76		4,08		7,69		4,67		8,79	21,02	(40 - 60)
		20,66		44,55		21,50		46,22			

Japan Centre

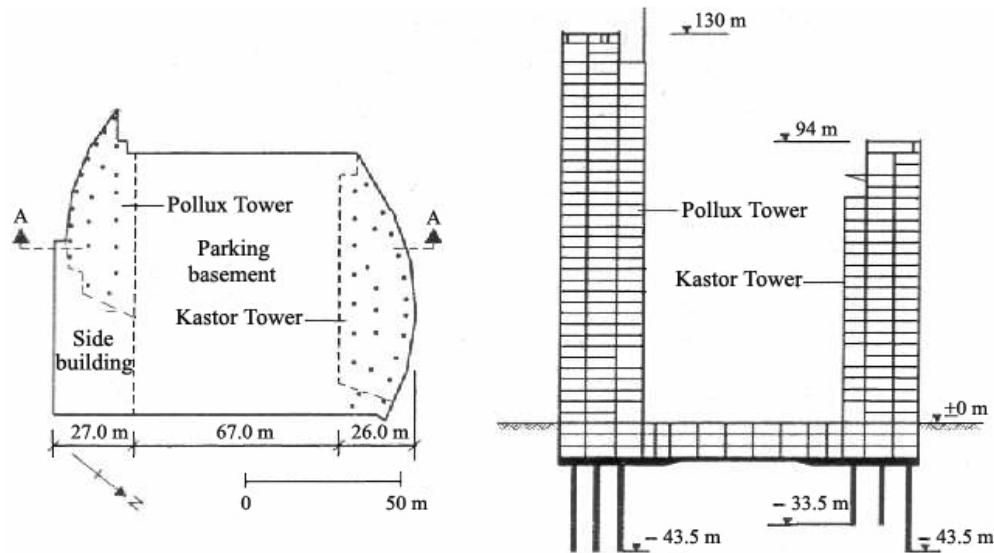
Rs	74,89	Mea.	50
Pier	47,51		
Raft	28,08		



**Figure A.16:** Measured and computed settlements for Japan-Centre Building (mm)

## 10. Forum (Pollux and Kastor) Building Complex (n=26,22)

The Forum building complex is located 150 m south-east of the Messeturm tower. There are two office towers; the so-called Kastor with height of 94 m, and Pollux with height of 130 m. These towers are located at opposite ends of a 120.5 m wide parking basement with three underground floors. Although the raft loading is extremely eccentric, the raft is designed as a single structure (14000 m<sup>2</sup> plan area) with bored piles having a diameter of 1.3 m and lengths of 20 m and 30 m concentrated under the Kastor building (26 piles) and under the Pollux building (22 piles). The thickness of the raft is 3.0 m beneath the towers and 1.0 m in the area of the parking basement. (Katzenbach, R., Arslan, U., and Moormann, C., 2000)



**Figure A.17:** Forum building complex, ground plan and section A-A (Katzenbach et al, 2000)

## Solution for Forum Pollux

### a) Settlement Ratio Method

$$n = 26 \quad d = 1,3 \text{ m} \quad r_0 = 0,65 \text{ m}$$

$$L = 30 \text{ m} \quad s = 5 \text{ m}$$

$$G = 20 + 1,0z \text{ (MN/m}^2\text{)} \quad E_p = 30000 \text{ MN/m}^2$$

$$v_s = 0,1 \quad v_s = 0,3 \quad \text{Frankfurt Clay}$$

$$P = 990 \text{ MN}$$

$$\lambda = E_p/G_l = 30000/55,5 \approx 540,540$$

$$\rho = G_{l/2}/G_l = 0,729 \rightarrow 0,99$$

$$\log \lambda = 2,732 \rightarrow 0,93$$

$$s/d = 5 \rightarrow 0,875$$

$$L/d = 23,077 \rightarrow 0,54$$

$$v_s = 0,1 \rightarrow 1,05$$

$$v_s = 0,3 \rightarrow 1$$

$$\eta_w = n^{-e} \quad R_s = n^e \quad \eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 1$$

$$\zeta = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et al., 1992})$$

$$\mu L = (2/(\lambda \zeta))^{0,5} L/r_0$$

$$P_{\text{single}} = 990000/26 = 38076,923 \text{ KN}$$

	e	$\eta_w$	R <sub>s</sub>	$\zeta$	$\mu L$	$\tanh \mu L L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s = 0,1$	0,456	0,225	4,429	4,328	1,349	29,889	33,490
$v_s = 0,3$	0,435	0,242	4,126	4,077	1,390	29,318	35,215

	P <sub>t</sub> /W <sub>t</sub>	K=nη <sub>w</sub> k	δ=P/K(mm)	P <sub>single</sub> /k	δ=δ <sub>s</sub> R <sub>s</sub>
v <sub>s</sub> =0,1	1208,154	7091,875	139,59	31,51	139,59
v <sub>s</sub> =0,3	1270,405	8004,951	123,67	29,97	123,67

δ<sub>measured</sub>=80 mm

### b) Equivalent Pier Method

$$B=A_G^{0.5}=34,35 \text{ m}$$

$$A_p=\Pi d^2 n/4=34,50 \text{ m}^2$$

$$E_p=30000 \text{ MPa} \quad E_s'=122,1 \text{ MPa} \quad E_u=166,5 \text{ MPa}$$

$$d_e=1,27 A_G^{0.5}=38,81 \text{ (for friction piles)}$$

$$\rho=0,729 \quad L=30 \text{ m}$$

$$E_e=E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1=\ln(2,5 \rho (1-v) L/r_0) \text{ (W. Fleming, et al., 1992)}$$

$$\zeta_2=\ln/\{5+[0,25+(2,5 \rho (1-v)-0,25)\xi] L/r_0\} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

### Method 1

	E <sub>e</sub>	λ	ζ <sub>(1-2)</sub>	μL	tanh μL L/(μL d <sub>e</sub> )	I <sub>δ</sub>	δ
v <sub>s</sub> =0,1	995,912	17,944	0,814	0,508	0,633	0,418	77,67
			2,111	0,316	0,665	0,662	123,17
v <sub>s</sub> =0,3	1017,46	18,332	0,563	0,605	0,614	0,371	58,37
			2,048	0,317	0,665	0,677	106,49

## Method 2

$L/d_e = 30/43,62 = 0,687 \rightarrow I_\delta = 0,474$  (Fig. 2.10)

$\delta$ (mm)	$v_s=0,1$	$v_s=0,3$
	88,09	74,54

$K \approx 200$  (pile stiffness factor)     $s/d \approx 5$      $L/d \approx 23,07$      $B=34,35$  m

$d_e/B \approx 0,75$  assumed, then  $d_e \approx 25,763$  m (Fig. 2.9)

## Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,1$	995,912	17,944	1,341	0,671	0,016	0,448	141,03
			2,177	0,526	1,067	0,575	180,96
$v_s=0,3$	1017,46	18,332	1,089	0,736	0,991	0,442	117,91
			2,076	0,533	1,065	0,604	161,00

## Method 2

$L/d_e = 30/25,76 = 1,164 \rightarrow I_\delta = 0,4$  (Fig. 2.10)

$\delta$ (mm)	$v_s=0,1$	$v_s=0,3$
	125,88	106,51

$\delta_{\text{measured}} = 80$  mm

### c) Equivalent Raft Method

L	B	H	L/B	H/B	D/B
69	30	30	2,3	1	1,11
84	45	30	1,86	0,66	1,41

$$P=990000 \text{ KN} \quad v_s = 0,1$$

$$\delta_{i \text{ ave}} = \mu_1 \mu_0 q_n B / E_u$$

$\mu_0$	$\mu_1$	$E_{uave}$	q	$\delta_i$
0,91	0,36	181,5	478,26	25,89
0,905	0,24	271,5	261,90	9,42

$$\delta_{i \text{ ave}} = 35,31 \text{ mm}$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)]$$

$$D/(LB)^{0,5} = 0,736 \rightarrow \mu_d = 0,786$$

$$\text{Frankfurt Clay} \rightarrow \mu_g = 0,7$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g$$

$E_{\text{mid-dr}}$	$m_v$	$\sigma_z$	$\delta_c$
133,1	0,0073	294,13	35,39
199,1	0,0049	102,82	8,27

$$\delta_c = 43,66 \text{ mm}$$

$$\delta_T = \delta_{i \text{ ave}} + \delta_c = 78,99 \text{ mm}$$

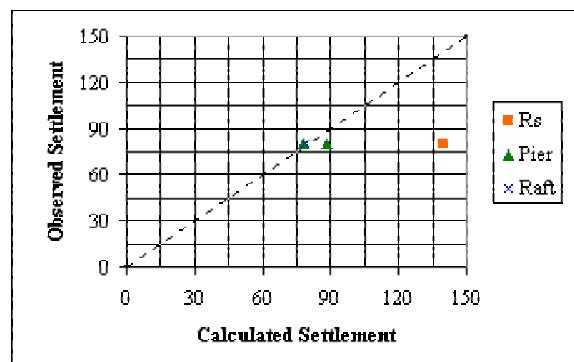
$$\delta_{\text{measured}} = 80 \text{ mm}$$

**Table A.10:** Measured and computed settlements for Forum Pollux (mm)

Set. Ratio		Settlement (mm)									Mea.	
		Equivalent Pier				Equivalent Raft						
		d <sub>e1</sub>		d <sub>e2</sub>		H=40 m	H=60 m	H=40 m (at the pile tip)	H=53,2 m (1/6)	H=50 m (1/8)		
		Met1	Met2	Met1	Met2	Ave.	Ave.	Ave.	Ave.	Ave.		
vs=0,1	139,59	77,67	88,09	141,0	125,9	69,62	78,99	84,01	86,52	89,77	80	
		123,2		181,0								
vs=0,3	123,67	58,37	74,54	117,9	106,5	54,7	63,39	68,2	69,41	72,14		
		106,5		161,0								

Forum Pollux

Rs	139,6	Mea.	80
Pier	77,67		
	88,09		
Raft	78,99		



**Figure A.18:** Measured and computed settlements for Forum Pollux (mm)

## Solution for Forum Kastor

### a) Settlement Ratio Method

$$n = 22 \quad d = 1,3 \text{ m} \quad r_0 = 0,65 \text{ m}$$

$$L = 25 \text{ m} \quad s = 5 \text{ m}$$

$$G = 20 + 1,0z \text{ (MN/m}^2\text{)} \quad E_p = 30000 \text{ MN/m}^2$$

$$v_s = 0,1 \quad v_s = 0,3 \quad \text{Frankfurt Clay}$$

$$P = 920 \text{ MN}$$

$$\lambda = E_p/G_l = 30000/50,5 \approx 594,059$$

$$\rho = G_{l/2}/G_l = 0,752 \rightarrow 1$$

$$\log \lambda = 2,773 \rightarrow 0,94$$

$$s/d = 5 \rightarrow 0,875$$

$$L/d = 19,23 \rightarrow 0,535$$

$$v_s = 0,1 \rightarrow 1,05$$

$$v_s = 0,3 \rightarrow 1$$

$$\eta_w = n^{-e} \quad R_s = n^e \quad \eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 1$$

$$\zeta = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et al.an, 1992})$$

$$\mu L = (2/(\lambda \zeta))^{0,5} L/r_0$$

$$P_{\text{single}} = 920000/22 = 41818,18 \text{ KN}$$

	e	$\eta_w$	R <sub>s</sub>	$\zeta$	$\mu L$	$\tanh \mu L L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s = 0,1$	0,462	0,239	4,171	4,176	1,092	28,092	33,975
$v_s = 0,3$	0,440	0,256	3,896	3,925	1,126	27,649	35,975

	P <sub>t</sub> /w <sub>t</sub>	K=nη <sub>w</sub> k	δ=P/K(mm)	P <sub>single</sub> /k	δ=δ <sub>s</sub> R <sub>s</sub>
v <sub>s</sub> =0,1	1115,234	5882,159	156,40	37,49	156,40
v <sub>s</sub> =0,3	1180,903	6666,851	137,99	35,41	137,99

δ<sub>measured</sub>=75 mm

### b) Equivalent Pier Method

$$B=A_G^{0.5}=38,73 \text{ m}$$

$$A_p=\Pi d^2 n/4=29,201 \text{ m}^2$$

$$E_p=30000 \text{ MPa} \quad E_s'=111,1 \text{ MPa} \quad E_u=151,5 \text{ MPa}$$

$$d_e=1,27 A_G^{0.5}=49,18 \text{ (for friction piles)}$$

$$\rho=0,752 \quad L=25 \text{ m}$$

$$E_e=E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1=\ln(2,5 \rho (1-v) L/r_0) \text{ (W. Fleming, et al., 1992)}$$

$$\zeta_2=\ln/\{5+[0,25+(2,5 \rho (1-v)-0,25)\xi] L/r_0\} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

### Method 1

	E <sub>e</sub>	λ	ζ <sub>(1-2)</sub>	μL	tanh μL L/(μL d <sub>e</sub> )	I <sub>δ</sub>	δ
v <sub>s</sub> =0,1	692,959	13,722	0,543	0,526	0,465	0,384	64,64
			2,044	0,271	0,496	0,719	121,15
v <sub>s</sub> =0,3	712,766	14,114	0,291	0,708	0,437	0,290	41,42
			1,993	0,271	0,496	0,727	103,55

## Method 2

$$L/d_e = 25/49,18 = 0,508 \rightarrow I_\delta = 0,5 \quad (\text{Fig. 2.10})$$

$\delta$ (mm)	$v_s=0,1$	$v_u=0,5$
	84,17	71,22

$$K \approx 200 \text{ (pile stiffness factor)} \quad s/d \approx 5 \quad L/d \approx 19,23 \quad B=41,53 \text{ m}$$

$$d_e/B \approx 0,77 \text{ assumed, then } d_e \approx 31,98 \text{ m} \quad (\text{Fig. 2.9})$$

## Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,1$	692,959	13,722	1,043	0,626	0,743	0,453	126,00
			2,059	0,446	0,786	0,634	176,22
$v_s=0,3$	712,766	14,114	0,792	0,709	0,721	0,430	101,14
			1,975	0,449	0,786	0,659	155,02

## Method 2

$$L/d_e = 25/29,82 = 0,838 \rightarrow I_\delta = 0,45 \quad (\text{Fig. 2.10})$$

$\delta$ (mm)	$v_s=0,1$	$v_s=0,3$
	124,95	105,73

$$\delta_{\text{measured}} = 75 \text{ mm}$$

### c) Equivalent Raft Method

L	B	H	L/B	H/B	D/B
83,33	28,33	28,33	2,94	0,99	1,06
97,49	42,49	28,33	2,29	0,66	1,37

$$P=900000 \text{ KN} \quad v_s = 0,1$$

$$\delta_{i \text{ ave}} = \mu_1 \mu_0 q_n B / E_u$$

$\mu_0$	$\mu_1$	$E_{uave}$	q	$\delta_i$
0,915	0,36	168,97	389,64	21,52
0,905	0,24	253,96	222,03	8,07

$$\delta_{i \text{ ave}} = 29,59 \text{ mm}$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)]$$

$$D/(LB)^{0,5} = 0,620 \rightarrow \mu_d = 0,812$$

$$\text{Frankfurt Clay} \rightarrow \mu_g = 0,7$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g$$

$E_{\text{mid-dr}}$	$m_v$	$\sigma_z$	$\delta_c$
123,91	0,0079	247,42	31,43
186,24	0,0052	97,41	8,23

$$\delta_c = 39,67 \text{ mm}$$

$$\delta_T = \delta_{i \text{ ave}} + \delta_c = 69,26 \text{ mm}$$

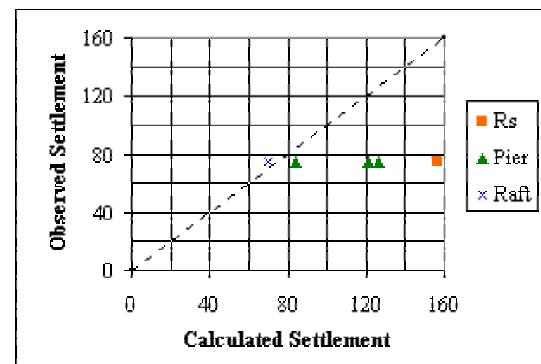
$$\delta_{\text{measured}} = 75 \text{ mm}$$

**Figure A.11:** Measured and computed settlements for Forum Kastor (mm)

Settlement (mm)										
Set. Ratio	Equivalent Pier				Equivalent Raft					Mea.
	d <sub>e1</sub>		d <sub>e2</sub>		H=40 m	H=56,66 m	H=40 m (at the pile tip)	H=51 m (1/6)	H=48,32 m (1/8)	
	Met1	Met2	Met1	Met2	Ave.	Ave.	Ave.	Ave.	Ave.	
vs=0,1	156,4	64,64	84,17	126	125	59,42	70,17	73,98	74,46	76,33
		121,2		176,2						
vs=0,3	138	41,42	71,22	101,1	105,7	45,81	56	60,07	59,56	61,04
		103,6		155						

Forum Kastor

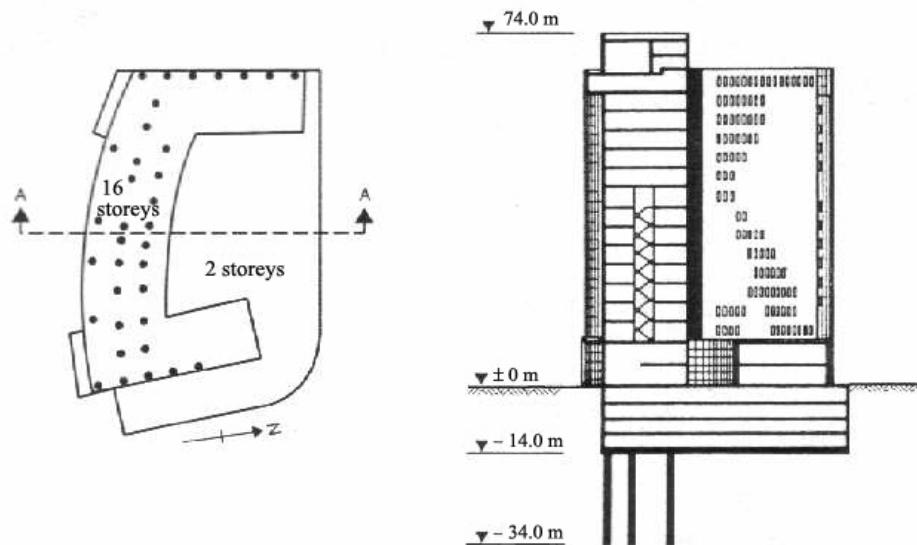
Rs	156,4	Mea.
Pier	121,2	75
	84,17	
	126	
Raft	70,17	



**Figure A.19:** Measured and computed settlements for Forum Kastor (mm)

## 11. American Express (n=35)

The American Express office building constructed in 1991-92 is situated about one km west of Messeturm tower. The raft of the 74 m high American Express building is loaded eccentrically by the 16-storey office tower. To minimise tilting and differential settlement of the raft, 35 bored piles with a diameter of 0.9 m and a length of 20 m were located under the tower. (Katzenbach, R., Arslan, U., and Moormann, C., 2000)



**Figure A.20:** American Express building, ground plan and section A-A  
(Katzenbach et al, 2000)

### a) Settlement Ratio Method

$$n = 35 \quad d = 0,9 \text{ m} \quad r_0 = 0,45 \text{ m}$$

$$L = 20 \text{ m} \quad s = 3,15 \text{ m}$$

$$G = 20 + 1,0z \text{ (MN/m}^2\text{)} \quad E_p = 30000 \text{ MN/m}^2$$

$$v_s = 0,1 \quad v_s = 0,3 \quad \text{Frankfurt Clay}$$

$$P = 1200 \text{ MN}$$

$$\lambda = E_p/G_l = 30000/46 \approx 652,174$$

$$\rho = G_{l/2}/G_l = 0,78 \rightarrow 1,01$$

$$\log \lambda = 2,81 \rightarrow 0,95$$

$$s/d = 3,5 \rightarrow 0,97$$

$$L/d = 22,22 \rightarrow 0,54$$

$$v_s = 0,1 \rightarrow 1,05$$

$$v_s = 0,3 \rightarrow 1$$

$$\eta_w = n^e \quad R_s = n^e$$

$$\zeta = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et al., 1992})$$

$$\eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 1$$

$$\mu L = (2/(\lambda \zeta))^{0,5} L/r_0$$

$$P_{\text{single}} = 1200000/35 = 34285,7 \text{ KN}$$

	$e$	$\eta_w$	$R_s$	$\zeta$	$\mu L$	$\tanh \mu L L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s = 0,1$	0,527	0,153	6,528	4,360	1,178	31,184	37,104
$v_s = 0,3$	0,502	0,167	5,970	4,109	1,214	30,671	39,078

	P <sub>t</sub> /w <sub>t</sub>	K=nη <sub>w</sub> k	δ=P/K(mm)	P <sub>single</sub> /k	δ=δ <sub>s</sub> R <sub>s</sub>
v <sub>s</sub> =0,1	768,064	4117,534	291,43	44,64	291,41
v <sub>s</sub> =0,3	808,925	4741,869	253,06	42,38	253,06

δ<sub>measured</sub>=55 mm

### b) Equivalent Pier Method

$$B=A_G^{0.5}=43,60 \text{ m}$$

$$A_p=\Pi d^2 n/4=22,266 \text{ m}^2$$

$$E_p=30000 \text{ MPa} \quad E_s'=101,2 \text{ MPa} \quad E_u=138 \text{ MPa}$$

$$d_e=1,27 A_G^{0.5}=55,38 \text{ (for friction piles)}$$

$$\rho=0,78 \quad L=20 \text{ m}$$

$$E_e=E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1=\ln(2,5 \rho (1-v) L/r_0) \text{ (W. Fleming, et al., 1992)}$$

$$\zeta_2=\ln/\{5+[0,25+(2,5 \rho (1-v)-0,25)\xi] L/r_0\} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

### Method 1

	E <sub>e</sub>	λ	ζ <sub>(1-2)</sub>	μL	tanh μL L/(μL d <sub>e</sub> )	I <sub>δ</sub>	δ
v <sub>s</sub> =0,1	451,303	9,811	0,240	0,665	0,315	0,276	59,20
			1,836	0,240	0,354	0,764	163,72
v <sub>s</sub> =0,3	469,48	10,206	-0,01				
			1,789	0,238	0,354	0,764	138,49

## Method 2

$$L/d_e = 20/55,38 = 0,361 \rightarrow I_\delta = 0,5 \quad (\text{Fig. 2.10})$$

$\delta$ (mm)	$v_s=0,1$	$v_s=0,3$
	107,05	90,58

$$K \approx 200 \text{ (pile stiffness factor)} \quad s/d \approx 3,5 \quad L/d \approx 22,22 \quad B=43,60 \text{ m}$$

$$d_e/B \approx 0,8 \text{ assumed, then } d_e \approx 34,85 \text{ m} \quad (\text{Fig. 2.9})$$

## Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,1$	451,303	9,811	0,702	0,617	0,510	0,435	148,10
			1,948	0,370	0,548	0,706	240,16
$v_s=0,3$	469,48	10,206	0,451	0,755	0,484	0,374	107,79
			1,882	0,369	0,548	0,724	208,39

## Method 2

$$L/d_e = 20/34,88 = 0,57 \rightarrow I_\delta = 0,5 \quad (\text{Fig. 2.10})$$

$\delta$ (mm)	$v_s=0,1$	$v_s=0,3$
	169,95	143,80

$$\delta_{\text{measured}} = 55 \text{ mm}$$

### c) Equivalent Raft Method

L	B	H	L/B	H/B	D/B
92,16	28,9	28,9	3,18	1	0,94
106,61	43,35	28,9	2,46	0,66	1,29

$$P=1200000 \text{ KN} \quad v_s = 0,1$$

$$\delta_{i \text{ ave}} = \mu_1 \mu_0 q_n B / E_u$$

$\mu_0$	$\mu_1$	$E_{uave}$	q	$\delta_i$
0,92	0,36	161,25	450,54	26,74
0,91	0,24	247,95	259,65	9,91

$$\delta_{i \text{ ave}} = 36,65 \text{ mm}$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)]$$

$$D/(LB)^{0,5} = 0,529 \rightarrow \mu_d = 0,838$$

$$\text{Frankfurt Clay} \rightarrow \mu_g = 0,7$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g$$

$E_{\text{mid-dr}}$	$m_v$	$\sigma_z$	$\delta_c$
118,25	0,00827	286,54	40,16
181,8	0,00537	64,91	5,91

$$\delta_c = 46,07 \text{ mm}$$

$$\delta_T = \delta_{i \text{ ave}} + \delta_c = 82,72 \text{ mm}$$

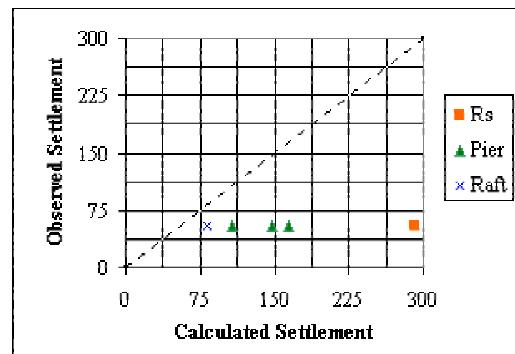
$$\delta_{\text{measured}} = 55 \text{ mm}$$

**Table A.12:** Measured and computed settlements for American Express (mm)

Settlement (mm)											
Set. Ratio	Equivalent Pier								Mea.		
	B'=32,36				B'=43,60						
	d <sub>e1</sub>		d <sub>e2</sub>		d <sub>e1</sub>		d <sub>e2</sub>				
	Met1	Met2	Met1	Met2	Met1	Met2	Met1	Met2	Ave.	Ave.	
v <sub>s</sub> =0,1	291,43	107,70 199,26	144,25 285,02	199,41 210,67	59,20 163,72	148,10 240,16	107,05 240,16	169,95	78,14	82,74	55
v <sub>s</sub> =0,3	253,06	68,00 170,04	122,05 249,24	157,77 178,26	— 138,49	90,58 208,39	107,79 208,39	143,80	62,97	66,28	

American Express

Rs	291,43	Mea.	55
Pier	163,72		
	107,05		
	148,10		
Raft	82,74		



**Figure A.21:** Measured and computed settlements for American Express (mm)

## **12. Westend I Tower, Frankfurt (n=40)**

The Westend 1 Tower is a 51-storey, 208 m high building in Frankfurt, Germany. The foundation for the tower consists of piled raft with 40 bored piles, each about 30 m long and 1.3 m in diameter. The central part of the raft is 4.5 m thick, decreasing to 3 m at the edges. The raft is founded at a depth of 14.5 m below the ground surface and about 9.5 m below groundwater level. The piles concentrated beneath the heavy columns of the superstructure. The 2940 m<sup>2</sup> raft of the skyscraper is separated by a settlement joint from the adjacent raft of the side building, which has a plan area of 3000 m<sup>2</sup>. Hence the office tower is founded on its own centrically loaded piled raft. Using programs GARP (plate on springs approach) and GASP (a piled strip analysis), approximately 106 and 141 mm settlement predictions are obtained relatively. (Poulos, H.G., 2001, Katzenbach, R., Arslan, U., Moormann, C., 2000)

### **a) Settlement Ratio Method**

$$n = 40 \quad d = 1,3 \text{ m} \quad r_0 = 0,65 \text{ m}$$

$$L = 30 \text{ m} \quad s/d = 5$$

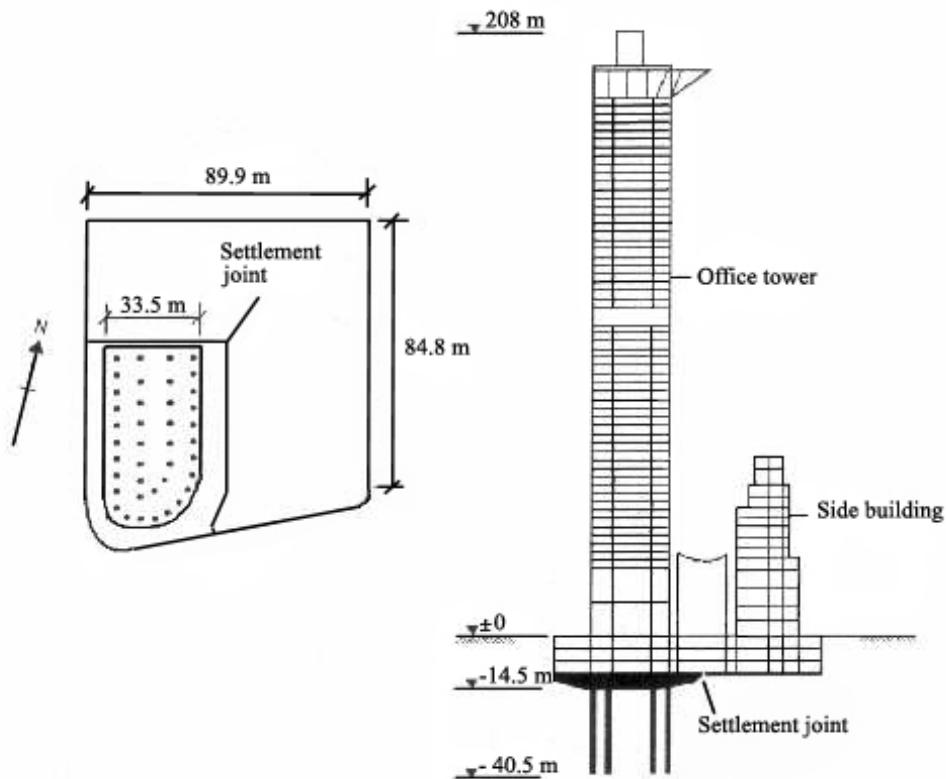
$$G = 20 + 1,0z \text{ (MN/m}^2\text{)} \quad \text{Stiff Frankfurt Clay} \quad E_p = 30000 \text{ MN/m}^2$$

$$P = 1420 \text{ MN} \quad v_s = 0,1 \quad v_s = 0,3$$

$$\lambda = E_p/G_l = 30000/53 \approx 566,03$$

$$\rho = G_{l/2}/G_l = 0,717 \rightarrow 0,98$$

$$\log \lambda = 2,752 \rightarrow 0,94$$



**Figure A.22:** Westend 1 Tower, Frankfurt; foundation plan and cross section  
(Poulos, 2001, Katzenbach et al, 2000)

$$s/d = 5 \rightarrow 0.875$$

$$L/d = 23.07 \rightarrow 0.54$$

$$v_s = 0.1 \rightarrow 1.05$$

$$v_s = 0.3 \rightarrow 1$$

$$\eta_w = n^{-e} \quad R_s = n^e \quad \eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 1$$

$$\zeta = \ln(2.5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, F. Randolph, K. Elson, J. Weltman, 1992})$$

$$\mu L = (2/(\lambda \zeta))^{0.5} L/r_0$$

$$P_{\text{single}} = 1420000/40 = 35500 \text{ KN}$$

	e	$\eta_w$	R_s	$\zeta$	$\mu L$	$\tanh \mu L / (\mu L r_0)$	$P_t / (w_t G r_0)$
$v_s=0,1$	0,457	0,185	5,397	4,310	1,321	30,286	33,558
$v_s=0,3$	0,435	0,200	4,981	4,059	1,361	29,717	35,324

	$P_t / w_t$	$K = n \eta_w k$	$\delta = P / K (\text{mm})$	$P_{\text{single}} / k$	$\delta = \delta_s R_s$
$v_s=0,1$	1156,103	8567,74	165,73	30,70	165,72
$v_s=0,3$	1216,915	9772,29	145,30	29,17	145,30

$$\delta_{\text{measured}} = 110 \text{ mm}$$

### b) Equivalent Pier Method

$$B = A_G^{0.5} = 46,28 \text{ m}$$

$$A_p = \Pi d^2 n / 4 = 53,09 \text{ m}^2$$

$$E_p = 30000 \text{ MPa}$$

$$E_s' = 116,6 \text{ MPa} \quad E_u = 159 \text{ MPa}$$

$$d_e = 1,27 A_G^{0.5} = 58,78 \text{ m} \text{ (for friction piles)}$$

$$\rho = 0,716 \quad L = 30 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-v) L / r_0) \text{ (W. Fleming, F. Randolph, K. Elson, J. Weltman, 1992)}$$

$$\zeta_2 = \ln / \{ 5 + [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L / r_0 \} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,1$	857,195	16,173	0,498	0,508	0,470	0,367	76,21
			1,894	0,260	0,499	0,701	145,36
$v_s=0,3$	877,87	16,563	0,247	0,713	0,438	0,263	46,09
			1,837	0,261	0,499	0,706	123,93

### Method 2

$$L/d_e = 30/58,78 = 0,51 \rightarrow I_\delta = 0,5 \text{ (Fig. 2.10)}$$

$\delta$ (mm)	$v_s=0,1$	$v_s=0,3$
	103,58	87,65

$$K \approx 200 \text{ (pile stiffness factor)} \quad s/d \approx 5 \quad L/d \approx 23,07 \quad B = 46,28 \text{ m}$$

$$d_e/B \approx 0,78 \text{ assumed, then } d_e \approx 36,1 \text{ m} \quad (\text{Fig. 2.9})$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,1$	857,195	16,173	0,986	0,588	0,746	0,441	148,95
			2,038	0,409	0,787	0,631	213,09
$v_s=0,3$	877,87	16,563	0,734	0,673	0,724	0,413	117,86
			1,958	0,412	0,786	0,653	186,47

## Method 2

$$L/d_e = 30/36, l=0,83 \rightarrow I_\delta = 0,44 \text{ (Fig. 2.10)}$$

$\delta$ (mm)	$v_s=0,1$	$v_s=0,3$
	148,42	108,84

$$\delta_{\text{measured}} = 110 \text{ mm}$$

### c) Equivalent Raft Method

L	B	H	L/B	H/B	D/B
69,82	42,2	42,2	1,65	1	0,81
90,92	63,3	42,2	1,43	0,66	1,21

$$P=1420000 \text{ KN} \quad v_s = 0,1$$

$$\delta_{i \text{ ave}} = \mu_1 \mu_0 q_n B / E_u$$

$\mu_0$	$\mu_1$	$E_{uave}$	q	$\delta_i$
0,92	0,36	195,3	481,94	34,49
0,91	0,24	321,9	246,73	10,59

$$\delta_{i \text{ ave}} = 45,08 \text{ mm}$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)]$$

$$D/(LB)^{0,5} = 0,635 \rightarrow \mu_d = 0,81$$

$$\text{Frankfurt Clay} \rightarrow \mu_g = 0,7$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g$$

$E_{\text{mid-dr}}$	$m_v$	$\sigma_z$	$\delta_c$
143,22	0,0068	282,90	46,21
236,06	0,0041	96,38	9,55

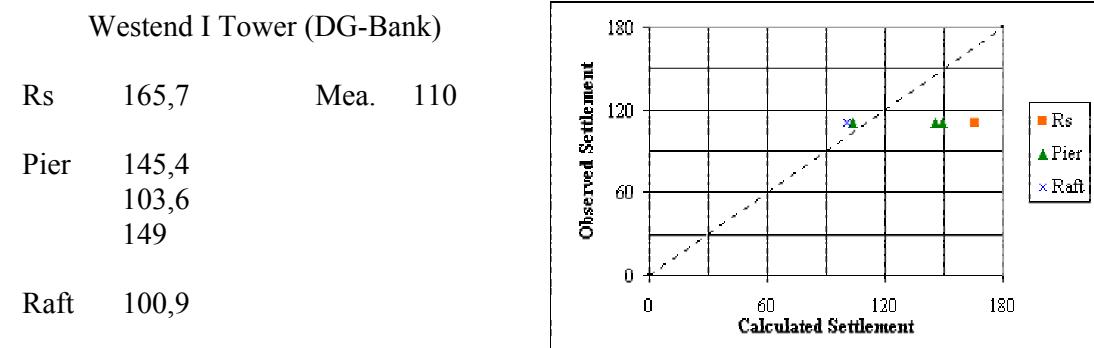
$$\delta_c = 55,76 \text{ mm}$$

$$\delta_T = \delta_{i \text{ ave}} + \delta_c = 100,85 \text{ mm}$$

$$\delta_{\text{measured}} = 110 \text{ mm}$$

**Table A.13:** Measured and computed settlements for Westend I Tower (mm)

Set. Ratio		Settlement (mm)									
		Equivalent Pier				Equivalent Raft					
		d <sub>e1</sub>		d <sub>e2</sub>		H=64,4 m	H=84,4 m	H=64,4 m (at the pile tip)	H=77,72 m (1/6)	Mea.	
		Met1	Met2	Met1	Met2	Ave.	Ave.	Ave.	Ave.		
vs=0,1	165,7	76,21	103,6	149	213,1	148,4	86,08	100,85	106,51	108,78	110
		145,4		213,1						112,58	
vs=0,3	145,3	46,1	87,65	117,9	186,5	125,6	69,95	80,93	86,4	87,41	90,61
		123,9		186,5						90,61	



**Figure A.23:** Measured and computed settlements for Westend I Tower (mm)

### 13. Messe-Torhaus Building (n=42)

The 30-storey tall building is a 130-m-high structure supported by two identical separate piled rafts. The pile group beneath each raft comprised 42 bored piles having a diameter of 90 cm and length of 20 m. The pile spacing varied from  $6r_0$  to  $7r_0$ . The subsoil below the raft was underlain by layers of Frankfurt clay extending to great depth. Within the clay, thin calciferous sand, silt inclusions, and isolated floating limestone layers were embedded. Based on the computed settlement of single pile and group settlement ratio, the settlement of the pile group is obtained as 50 mm. (W.Shen, Y.Chow and K.Yong 2000)

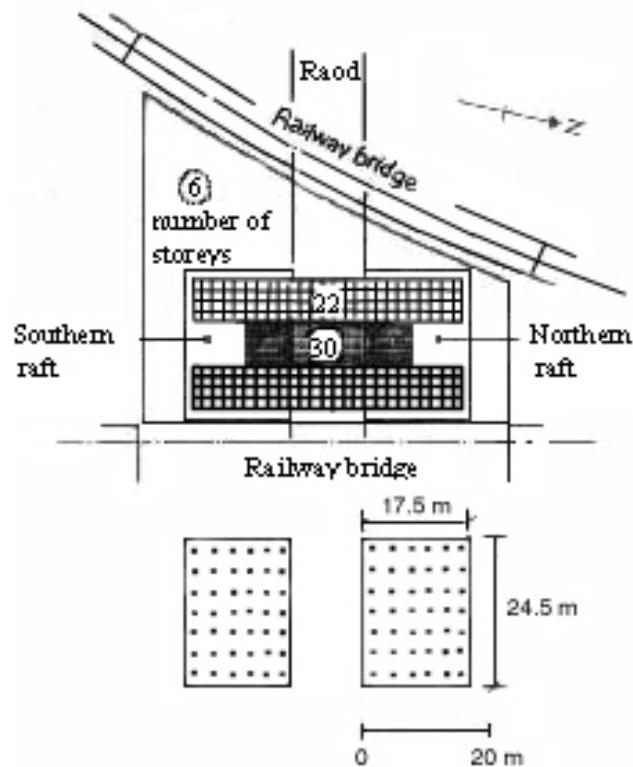


Figure A.24: Messe-Torhaus building, site plan (Shen et al, 2000)

### a) Settlement Ratio Method

$$G = 20 + 1,0z \text{ (MN/m}^2\text{)} \quad \text{Frankfurt clay} \quad E_p = 30000 \text{ MN/m}^2$$

$n = 42$  piles (under each raft)

$$L = 20 \text{ m} \quad s = 6r_0 - 7r_0 \quad d = 0,9 \text{ m} \quad r_0 = 0,45 \text{ m}$$

$$P = 180,75 \text{ MN} \quad v_s = 0,1 \quad v_s = 0,3$$

$$\lambda = E_p/G_l = 30000/40 \approx 750$$

$$\rho = G_{l/2}/G_l = 0,75 \rightarrow 1$$

$$\log \lambda = 2,875 \rightarrow 0,97$$

$$s/d_{ave} = 3,25 \rightarrow 0,98$$

$$L/d = 22,22 \rightarrow 0,537$$

$$v_s = 0,1 \rightarrow 1,05$$

$$v_s = 0,3 \rightarrow 1$$

$$\eta_w = n^e \quad R_s = n^e$$

$$\zeta = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et.al 1992})$$

$$\eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 1$$

$$\mu L = (2/(\lambda \zeta))^{0,5} L/r_0$$

$$P_{\text{single}} = 180750/42 = 4303,57 \text{ KN}$$

	e	$\eta_w$	R <sub>s</sub>	$\zeta$	$\mu L$	$\tanh \mu L L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s = 0,1$	0,536	0,134	7,427	4,317	1,104	32,275	37,395
$v_s = 0,3$	0,511	0,148	6,751	4,066	1,138	31,778	39,498

	P <sub>t</sub> /W <sub>t</sub>	K=mn <sub>w</sub> k	$\delta=P/K(mm)$	P <sub>single</sub> /k	$\delta=\delta_s R_s$
v <sub>s</sub> =0,1	673,119	3806,068	47,48	6,39	47,48
v <sub>s</sub> =0,3	710,971	4422,892	40,86	6,053	40,86

$\delta_{\text{measured}} = 45 \text{ mm}$

### b) Equivalent Pier Method

$$B=A_G^{0.5} = 20,706 \text{ m}$$

$$A_p = \pi d^2 n / 4 = 26,719 \text{ m}^2$$

$$E_p = 30000 \text{ KPa}$$

$$E_s' = 88 \text{ MPa} \quad E_u = 120 \text{ MPa}$$

$$d_e = 1,27 A_G^{0.5} = 26,296 \text{ m} \text{ (for friction piles)}$$

$$\rho = 0,75 \quad L = 20 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-v) L / r_0) \text{ (W. Fleming, et al. 1992)}$$

$$\zeta_2 = \ln / \{5 + [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L / r_0\} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

### Method 1

	E <sub>e</sub>	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu l d_e)$	I <sub>δ</sub>	δ
v <sub>s</sub> =0,1	1952,084	48,802	0,942	0,317	0,736	0,388	30,36
			2,023	0,216	0,748	0,578	45,20
v <sub>s</sub> =0,3	1967,087	49,177	0,691	0,369	0,727	0,350	23,16
			1,945	0,219	0,748	0,587	38,83

## Method 2

$$L/d_e = 20/26,29 = 0,76 \rightarrow I_s = 0,47 \text{ (Fig. 2.10)}$$

	$v_s=0,1$	$v_s=0,3$
$\delta \text{ (mm)}$	36,71	31,06

$$K \approx 250 \text{ (pile stiffness factor)} \quad s/d \approx 3,25 \quad L/d \approx 22,22 \quad B = 20,7 \text{ m}$$

$$d_e/B \approx 0,82 \text{ assumed, then } d_e \approx 17 \text{ (Fig. 2.9)}$$

## Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,1$	1952,084	48,802	1,378	0,405	1,115	0,38	46,88
			2,193	0,321	1,137	0,502	60,73
$v_s=0,3$	1967,087	49,177	1,127	0,446	1,104	0,376	38,48
			2,090	0,328	1,136	0,520	53,18

## Method 2

$$L/d_e = 20/17 = 1,17 \rightarrow I_\delta = 0,38 \text{ (Fig 2.10)}$$

	$v_s=0,1$	$v_s=0,3$
$\delta \text{ (mm)}$	45,91	38,85

$$\delta_{\text{measured}} = 45 \text{ mm}$$

### c) Equivalent Raft Method

L	B	H	L/B	H/B	D/B
30,26	23,26	15,5	1,300	0,666	0,571
38,01	31,01	15,5	1,225	0,499	0,928
45,76	38,76	15,5	1,180	0,399	1,142

$$P=180750 \text{ KN} \quad v_s = 0,1$$

$$q_n = P/(B*L) = 240,272 \text{ KN}$$

$$\delta_{i \text{ ave}} = \mu_1 \mu_0 q_n B / E_u$$

$\mu_0$	$\mu_1$	$E_{uave}$	q	$\delta_i$
0,93	0,23	123,15	256,802	10,374
0,92	0,18	169,65	153,348	4,641
0,91	0,13	216,15	101,908	2,161

$$\delta_{i \text{ ave}} = 17,17 \text{ mm}$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)]$$

$$D/(LB)^{0,5} = 0,501 \rightarrow \mu_d = 0,86$$

$$\text{Frankfurt Clay} \rightarrow \mu_g = 0,7$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g$$

$E_{\text{mid-dr}}$	$m_v$	$\sigma_z$	$\delta_c$
90,31	0,0108	172,057	17,38
124,41	0,0078	74,472	5,46
158,51	0,0061	19,935	1,14

$$\delta_c = 23,99 \text{ mm}$$

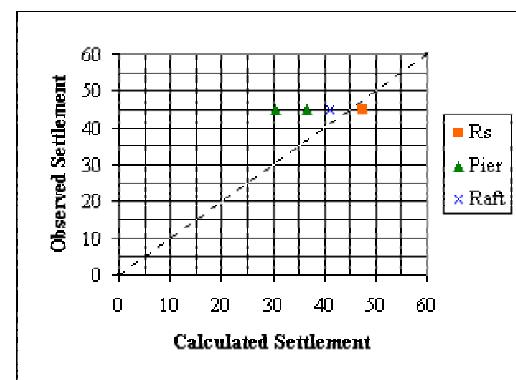
$$\delta_T = \delta_{i \text{ ave}} + \delta_c = 41,17 \text{ mm}$$

$$\delta_{\text{measured}} = 45 \text{ mm}$$

**Table A.14:** Measured and computed settlements for Messe Torhaus (mm)

Settlement (mm)								
Set. Ratio		Equivalent Pier				Equivalent Raft		Mea.
		d <sub>e1</sub>		d <sub>e2</sub>		H=35 m	H=46,46 m	
		Met1	Met2	Met1	Met2	Ave.	Ave.	
vs=0,1	47,49	30,36	36,71	46,88	45,91	35,42	41,17	45
		45,21		60,73				
vs=0,3	40,86	23,16	31,08	38,48	38,84	29,04	32,60	45
		38,83		53,18				

Messe Torhaus  
 Rs      47,49      Mea. 45  
 Pier    30,36  
         36,71  
 Raft    41,17



**Figure A.25:** Measured and computed settlements for Messe Torhaus (mm)

#### 14. Gratham Road (n=48)

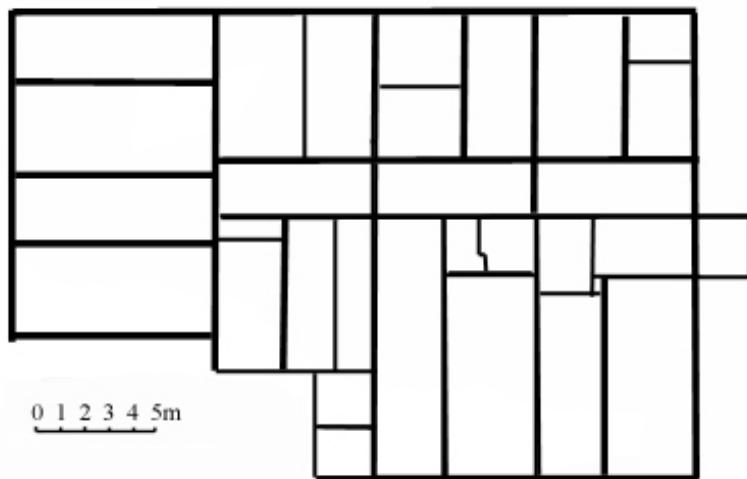
This is a 22-storey structure constructed at a site in London Borough of Lambeth. A site investigation showed 2 m Flood Plain Gravels overlying London Clay ( $c_u=60-180 \text{ kN/m}^2$ ). It was decided that large diameter underreamed (1.52 to 2.74 m) piles taken to depths of 19 m should be constructed to support the building. Pile lengths are between 16.2 and 18.7m and shafts are 0.76 and 0.91 m diameter. (Morton, K., and Au, E., 1974)

##### a) Settlement Ratio Method

$$n = 48 \quad r_0 = 0.455 \text{ m} \quad r_b = 1.065 \text{ m}$$

$$L = 17.45 \text{ m} \quad s = 3.64 \text{ m}$$

$$c_u = 60-180 \text{ (kN/m}^2\text{)} \quad \text{London Clay} \quad N=62-136 \text{ Flood Plain Gravel}$$



**Figure A.26:** Gratham Road foundation plan (Morton and Au, 1974)

$$E_p = 30000 \text{ MN/m}^2$$

$$v_s=0,1 \quad v_s=0,3 \quad P=100 \text{ MN}$$

$$\lambda=E_p/G_l=30000/25 \approx 1200$$

$$\rho=G_{l/2}/G_l=20/25=0,8 \rightarrow 1,02$$

$$\log \lambda = 3,079 \rightarrow 1,01$$

$$s/d=4 \rightarrow 0,93$$

$$L/d=19,175 \rightarrow 0,535$$

$$v_s=0,1 \rightarrow 1,05$$

$$v_s=0,3 \rightarrow 1$$

$$\eta_w=n^{-e} \quad R_s=n^e$$

$$\zeta=\ln(2,5 \rho (1-v) L/r_0) \text{ (W. Fleming, et al., 1992)}$$

$$\eta=r_b/r_0=2,34 \quad \xi=G_l/G_b=1$$

$$\mu L=(2/(\lambda\zeta))^{0,5}L/r_0$$

$$P_{\text{single}}=100000/48=2083 \text{ KN}$$

	e	$\eta_w$	R_s	$\zeta$	$\mu L$	$\tan \mu L L/(\mu L r_0)$	$P_t/(w_t G_l r_0)$
$v_s=0,1$	0,538	0,124	8,032	4,235	0,760	32,339	44,793
$v_s=0,3$	0,512	0,137	7,273	3,983	0,784	32,034	48,309

	$P_t/w_t$	K=n $\eta_w k$	$\delta=P/K(\text{mm})$	$P_{\text{single}}/k$	$\delta=\delta_s R_s$
$v_s=0,1$	509,523	3044,762	32,84	4,088	32,84
$v_s=0,3$	549,522	3626,289	27,57	3,790	27,57

$$\delta_{\text{measured}}=30 \text{ mm}$$

### b) Equivalent Pier Method

$$B = A_G^{0.5} = 23,47 \text{ m}$$

$$A_p = \pi d^2 n / 4 = 31,218 \text{ m}^2$$

$$E_p = 30000 \text{ MPa}$$

$$E_s' = 55 \text{ MPa} \quad E_u = 75 \text{ MPa}$$

$$d_e = 1,27 \text{ A}_G^{0.5} = 29,80 \text{ (for friction piles)}$$

$$\rho = 0,8 \quad L = 17,45 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-v) L / r_0) \text{ (W. Fleming, et al. 1992)}$$

$$\zeta_2 = \ln / \{5 + [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L / r_0\} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s = 0,1$	17,52,15	70,086	0,745	0,229	0,575	0,369	22,50
			1,961	0,141	0,581	0,606	36,99
$v_s = 0,3$	1761,59	70,463	0,494	0,280	0,570	0,309	15,95
			1,893	0,143	0,581	0,608	31,040

### Method 2

$$L/d_e = 17,45/29,80 = 0,585 \rightarrow I_\delta = 0,5 \text{ (Fig. 2.10)}$$

$\delta$ (mm)	$v_s = 0,1$	$v_s = 0,3$
	30,49	25,80

$K \approx 400$  (pile stiffness factor)     $s/d \approx 4$      $L/d \approx 19,175$      $B=23,47 \text{ m}$

$d_e/B \approx 0,84$  assumed, then  $d_e \approx 19,71 \text{ m}$  (Fig. 2.9)

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,1$	17,52,15	70,086	1,158	0,277	0,863	0,381	35,19
			2,102	2,206	0,872	0,528	48,74
$v_s=0,3$	1761,59	70,463	0,907	0,313	0,857	0,357	27,86
			2,010	0,210	0,872	0,539	42,10

### Method 2

$L/d_e = 17,45/29,065 = 0,6 \rightarrow I_\delta = 0,5$  (Fig. 2.10)

$\delta$ (mm)	$v_s=0,1$	$v_s=0,3$
	42,42	35,89

$\delta_{\text{measured}} = 30 \text{ mm}$

### c) Equivalent Raft Method

$L=34,38 \quad B=25,09 \quad H=50,18 \quad D=12,63$

$L/B=1,37 \quad H/B=2$

$E_{\text{uave}}=146,4 \quad E_s'=107,36$

$q_n=100000/(BL) = 115,93 \text{ Kpa}$

$$\mu_0=0,93 \quad \mu_l=0,56$$

$$\delta_{i\ ave}=q_n B \mu_0 \mu_l / E_u = 115,93 \cdot 25,09 \cdot 0,93 \cdot 0,56 / 146,4 = 10,34 \text{ mm}$$

$$D/(LB)^{0,5}=0,430 \rightarrow \mu_d=0,876$$

$$\text{London Clay} \rightarrow \mu_g=0,7$$

$$z/B=1 \quad \sigma_z/q=0,3 \quad \sigma_z=34,77 \text{ KPa}$$

$$m_v=[(1+v)(1-2v)]/[E_s'(1-v)] \approx 0,0091$$

$$\delta_c=m_v \sigma_z H \mu_d \mu_g$$

$$=0,0091 \cdot 34,77 \cdot 50,18 \cdot 0,876 \cdot 0,7 \approx 9,74 \text{ mm}$$

$$\delta_T=\delta_i+\delta_c = \boxed{20,09 \text{ mm}}$$

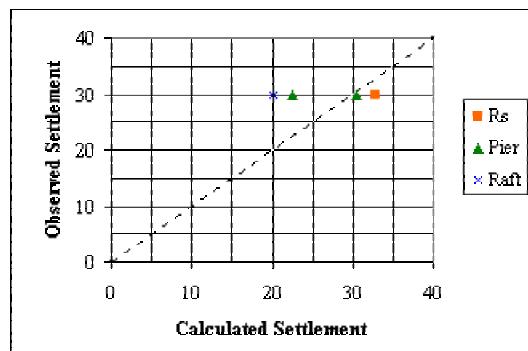
$$\delta_{\text{measured}}=30 \text{ mm}$$

**Table A.15:** Measured and computed settlements for Gratham Road (mm)

Set. Ratio		Settlement (mm)										Mea.	
		Equivalent Pier				Equivalent Raft							
		d <sub>e1</sub>		d <sub>e2</sub>		H=38,56 m	H=50,18 m	H=38,56 m (at the tip)	H=46,3 m (1/6)	H=44,36 m (1/8)			
		Met1	Met2	Met1	Met2	Ave.	Ave.	Ave.	Ave.	Ave.	Ave.		
vs=0,1	32,84	22,50	30,49	35,19	42,42	20,29	20,09	23,94	22,01	22,82	30		
		36,99		48,74									
vs=0,3	27,57	15,95	25,80	27,86	35,89	16,56	16,61	19,86	18,09	18,78	30		
		31,40		42,01									

Gratham

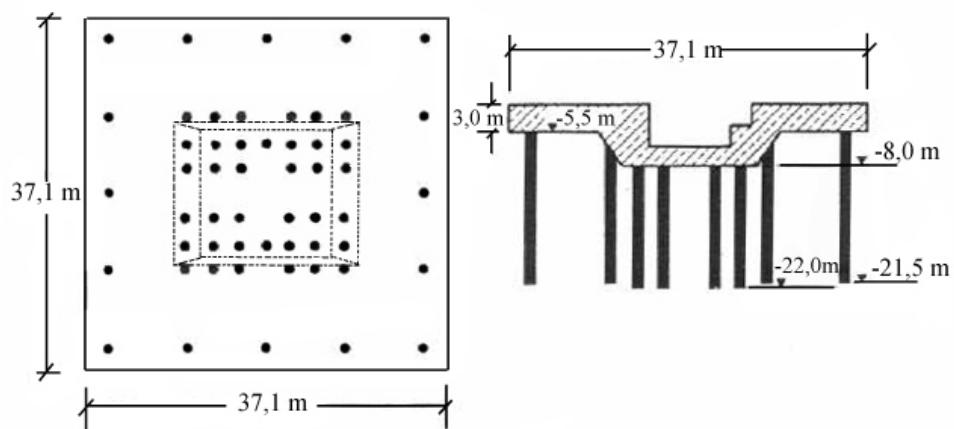
Rs	32,84	Mea.	30
Pier	22,5		
	30,49		
Raft	20,09		



**Figure A.27:** Measured and computed settlements for Gratham Road (mm)

## 15. Treptowers Building (n=54)

The 121 m high Treptowers office building in Berlin is 37.1 m square in plan, and is located close to the river Spree. The raft of thickness 2-3 m is founded 8 m below ground level in the remainin area of he elevator pit, and 5.5 below ground level in the remaining area. To transmit part of the total building load of 670 MN through the loose sands just below raft level to medium dense to dense sand at greater depth, 54 bored piles with diameter of 0.9 m have been arranged under the raft. Due to the different founding levels of the raft, the length of piles varies between 12.5 m and 16.0 m. At the end of the construction, the mean settlement of the building was 63 mm.(Katzenbach, R., Arslan,U., and Moormann, C., 2000)



**Figure A.28:** Treptowers building, Berlin; plan and cross-section of piled raft foundation (Katzenbach et al, 2000)

### a) Settlement Ratio Method

$$n = 54 \quad d = 0,9 \text{ m} \quad r_0 = 0,45 \text{ m}$$

$$L = 14,25 \text{ m} \quad s = 5 \text{ m}$$

$$E_u \approx 20000 \sqrt{z} \text{ kPa} \quad \text{for } 0 < z < 20 \text{ m}$$

$$E_u \approx 60000 \sqrt{z} \text{ kPa} \quad \text{for } z > 20 \text{ m} \quad (z = \text{depth below surface})$$

$$\text{Berlin Sand} \quad v_s = 0,25 \quad v_s = 0,35 \quad v_u = 0,5$$

$$E_p = 30000 \text{ MN/m}^2$$

$$P = 670 \text{ MN}$$

$$\lambda = E_p / G_l = 30000 / 31,27 \approx 959,386$$

$$\rho = G_{l/2} / G_l = 0,825 \rightarrow 1,02$$

$$\log \lambda = 2,981 \rightarrow 0,99$$

$$s/d = 5 \rightarrow 0,87$$

$$L/d = 15,83 \rightarrow 0,528$$

$$v_s = 0,25 \rightarrow 1,02$$

$$v_s = 0,35 \rightarrow 0,98$$

$$v_u = 0,5 \rightarrow 0,93$$

$$\eta_w = n^{-e} \quad R_s = n^e \quad \eta = r_b / r_0 = 1 \quad \xi = G_l / G_b = 0,333$$

$$\zeta = \ln(2,5 \rho (1-v) L / r_0) \quad (\text{W. Fleming, et al., 1992})$$

$$\mu L = (2 / (\lambda \zeta))^{0,5} L / r_0$$

$$P_{\text{single}} = 670000 / 54 = 12407,4 \text{ KN}$$

	e	$\eta_w$	R_s	$\zeta$	$\mu L$	$\tanh \mu L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s=0,25$	0,473	0,151	6,601	3,074	0,824	26,020	52,613
$v_s=0,35$	0,454	0,163	6,130	2,968	0,839	25,862	54,934
$v_u=0,5$	0,431	0,179	5,589	2,784	0,866	25,566	59,498

	$P_t / w_t$	$K = n \eta_w k$	$\delta = P / K (mm)$	$P_{\text{single}} / k$	$\delta = \delta_s R_s$
$v_s=0,25$	740,352	6055,767	110,63	16,75	110,63
$v_s=0,35$	773,011	6808,638	98,40	16,05	98,40
$v_u=0,5$	837,226	8089,04	82,82	14,81	82,82

$$\delta_{\text{measured}} = 63 \text{ mm}$$

### b) Equivalent Pier Method

$$B = A_G^{0.5} = 37,1 \text{ m}$$

$$A_p = \pi d^2 n / 4 = 34,35 \text{ m}^2$$

$$E_p = 30000 \text{ MPa}$$

$$E_s' = 78,167 \text{ MPa} \quad E_u = 93,8 \text{ MPa}$$

$$d_e = 1,13 A_G^{0.5} = 41,923 \text{ m} \text{ (for friction piles)}$$

$$\rho = 0,825 \quad L = 14,25 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-v) L / r_0) \text{ (W. Fleming, et al., 1992)}$$

$$\zeta_2 = \ln \left\{ 5 + [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L / r_0 \right\} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,25$	824,975	26,385	-0,766				
			1,698	0,143	0,337	0,313	64,044
$v_s=0,35$	831,072	26,58	-0,873				
			1,689	0,143	0,337	0,302	57,27
$v_u=0,5$	840,218	26,872	-1,057				
			1,676	0,143	0,337	0,274	46,756

### Method 2

$$L/d_e = 14,25/41,923 = 0,34 \rightarrow I_\delta = 0,26$$

	$v_s=0,25$	$v_s=0,35$	$v_u=0,5$
$\delta$ (mm)	53,15	49,22	44,29

$$K \approx 300 \text{ (pile stiffness factor)} \quad s/d \approx 5 \quad L/d \approx 15,833 \quad B=37,1 \text{ m}$$

$d_e/B \approx 0,81$  assumed, then  $d_e \approx 30,051 \text{ m}$  (Fig. 2.9)

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,25$	824,975	26,385	-0,433				
			1,731	0,198	0,468	0,314	89,63
$v_s=0,35$	831,072	26,58	-0,540				
			1,719	0,198	0,468	0,306	80,95
$v_u=0,5$	840,218	26,872	-0,724				

			1,701	0,198	0,468	0,283	67,31
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## Method 2

$$L/d_e = 14,25 / 30,051 = 0,474 \rightarrow I_\delta = 0,25$$

$\delta$ (mm)	$v_s = 0,25$	$v_s = 0,35$	$v_u = 0,5$
	71,037	66,02	59,422

$$\delta_{\text{measured}} = 63 \text{ mm}$$

## c) Equivalent Raft Method

L	B	H	L/B	H/B	D/B
37,1	37,1	37,1	1	1	0,59
55,65	55,65	37,1	1	0,66	1,06

$$P = 670 \text{ KN} \quad v_s = 0,25$$

$$\delta_{i \text{ ave}} = \mu_1 \mu_0 q_n B / E_u$$

$\mu_0$	$\mu_1$	$E_{uave}$	q	$\delta_i$
0,93	0,36	382,07	486,77	15,82
0,92	0,24	528,71	216,34	5,02

$$\delta_{i \text{ ave}} = 20,85 \text{ mm}$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)]$$

$$D/(LB)^{0,5} = 0,592 \rightarrow \mu_d = 0,82$$

Berlin Sand  $\rightarrow \mu_g = 1$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g$$

$E_{\text{mid-dr}}$	$m_v$	$\sigma_z$	$\delta_c$
318,33	0,00571	250,68	43,54
588,48	0,004	70,58	8,59

$$\delta_c = 52,10 \text{ mm}$$

$$\delta_T = \delta_{i \text{ ave}} + \delta_c = 72,98 \text{ mm}$$

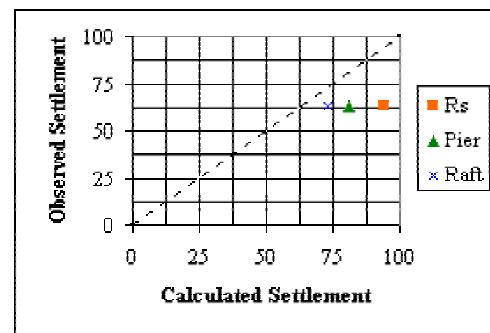
$q_c$	$m_v$	$\delta_c$	$\delta_T$
25	0,008	63,97	87,749
30	0,0067	53,57	77,349
35	0,00571	45,66	69,439
40	0,005	39,98	63,759
45	0,0044	35,18	58,959
ave		70,808	

$$\delta_{\text{measured}} = 63 \text{ mm}$$

**Table A.16:** Measured and computed settlements for Treptowers Building (mm)

Set. Ratio		Settlement (mm)				Mea.	
		Equivalent Pier		Eq.Raft			
		d <sub>e1</sub>	d <sub>e2</sub>	Met1	Met2		
		Met1	Met2				
vs=0,35	110,63	—	53,15	71,3			
		64,04	89,63				
vs=0,35	98,40	—	49,22	66,02	72,98	63	
		57,27	80,95				
vs=0,50	82,82	—	44,29	59,42			
		46,75	67,31				

Treptowers  
 Rs      94,4      Mea.      63  
 Pier    80,95  
 Raft    72,98



**Figure A.29:** Measured and computed settlements for Treptowers Building (mm)

## **16. Molasses Tank (n=55)**

The tank under examination was constructed in Scotland in 1978 to store molasses. It is supported by 55 precast concrete piles, each  $250 \times 250 \text{ mm}^2$  in cross section and 29 m long, laid out on a triangular grid at a spacing of 2 m. A 2 m thick pad of dense granular material was constructed over the piles and incorporated a 150 mm thick reinforced concrete membrane connecting the pile heads. The effective pile length was then reduced to 27 m.

The foundation soil is a silty clay with interbedded sandy silt and silty sand layers until a maximum depth of 18 m below ground level, overlying a slightly over consolidated silty clay with occasional intercalations of sand and silt. According to Randolph (1994), the subsoil can be modelled as a unique cohesive layer. The average settlement is calculated as 29.4 mm by using non-linear analysis by the program GRUPPALO. Linear elastic analysis slightly underpredicts the settlement for this case. Average settlement may be estimated as 27.8 mm Randolph (1994). (Mandolini, A., and Viggiani, C., 1997, Randolph, M.F., 1994, Randolph, M.F., and Guo, W.D., 1999 )

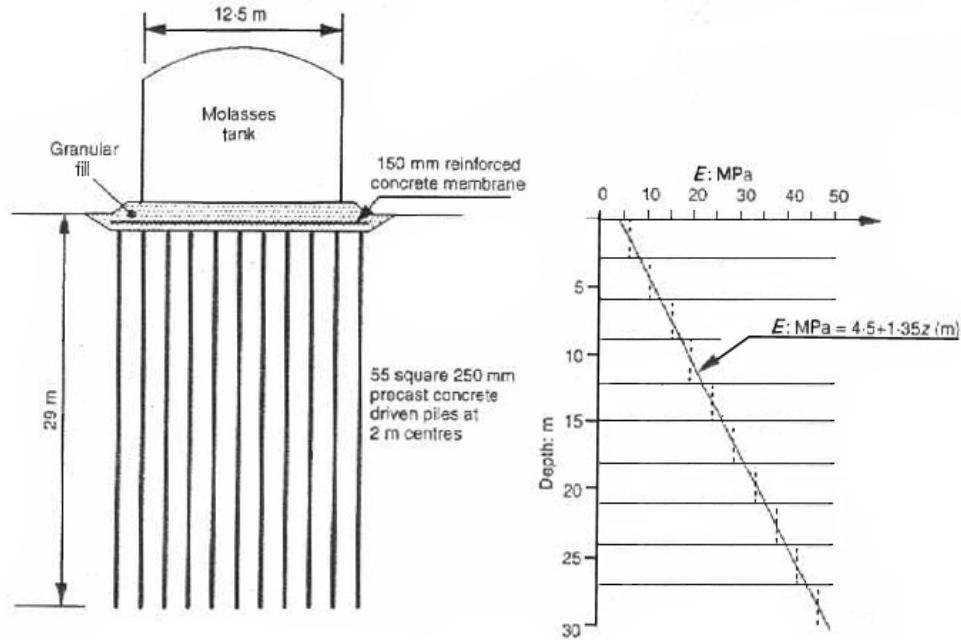
### **a) Settlement Ratio Method**

$$n = 55 \quad d = 0.28 \text{ m} \quad r_0 = 0.141 \text{ m}$$

$$L = 27 \text{ m} \quad s = 2 \text{ m}$$

$$E = 4.5 + 1.35z \text{ (MN/m}^2\text{)} \quad E_p = 20000 \text{ MN/m}^2$$

$$P = 24.2 \text{ MN} \quad v_s = 0.2 \quad v_s = 0.3$$



**Figure A.30:** Schematic of the Molasses tank and subsoil model adopted in the analysis (Mandolini and Viggiani, 1997, Randolph, 1994, Randolph and Guo, 1999)

$$\lambda = E_p/G_l = 20000/14,55 \approx 1374,57$$

$$\rho = G_{l/2}/G_l = 0,582 \rightarrow 0,95$$

$$\log \lambda = 3,138 \rightarrow 1,03$$

$$s/d = 7 \rightarrow 0,79$$

$$L/d = 95,74 \rightarrow 0,51$$

$$v_s = 0,2 \rightarrow 1,03$$

$$v_s = 0,3 \rightarrow 1$$

$$\eta_w = n^e \quad R_s = n^e$$

$$\zeta = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et al., 1992})$$

$$\eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 1$$

$$\mu L = (2/(\lambda\zeta))^{0.5} L/r_0$$

$$P_{\text{single}} = 24200/55 = 440 \text{ KN}$$

	e	$\eta_w$	R_s	$\zeta$	$\mu L$	$\tanh \mu L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s = 0,2$	0,406	0,196	5,089	5,408	3,141	60,735	43,076
$v_s = 0,3$	0,394	0,206	4,854	5,274	3,180	59,998	43,866

	$P_t/w_t$	$K = n\eta_w k$	$\delta = P/K(\text{mm})$	$P_{\text{single}}/k$	$\delta = \delta_s R_s$
$v_s = 0,2$	88,373	954,960	25,34	4,97	25,34
$v_s = 0,3$	89,994	1019,67	23,73	4,88	23,73

$$\delta_{\text{measured}} = 29,5 \text{ mm}$$

## b) Equivalent Pier Method

$$B = A_G^{0.5} = 12,071 \text{ m}$$

$$A_p = \pi d^2 n / 4 = 3,386 \text{ m}^2$$

$$E_s' = 34,92 \text{ MPa} \quad E_u = 43,65 \text{ MPa} \quad E_p = 20000 \text{ MPa}$$

$$d_e = 1,27 A_G^{0.5} = 15,331 \text{ m} \text{ (for friction piles)}$$

$$\rho = 0,582 \quad L = 27 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-v) L / r_0) \text{ (W. Fleming, et al., 1992)}$$

$$\zeta_2 = \ln \{ 5 + [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L / r_0 \} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,2$	498,897	34,288	1,411	0,716	1,511	0,426	19,27
			2,208	0,572	1,591	0,536	24,24
$v_s=0,3$	501,74	34,483	1,278	0,750	1,491	0,422	17,61
			2,150	0,578	1,587	0,546	22,78

### Method 2

$$L/d_e = 27/15,33 = 1,76 \rightarrow I_\delta = 0,33 \text{ (Fig. 2.10)}$$

$\delta$ (mm)	$v_s=0,2$	$v_s=0,3$
	14,91	13,77

$$K \approx 460 \quad s/d \approx 7 \quad L/d \approx 95,74 \quad B = 12,07 \text{ m}$$

$$d_e/B \approx 0,44 \text{ assumed, then } d_e \approx 5,311 \text{ m (Fig. 2.9)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,2$	498,897	34,288	2,471	1,561	2,980	0,443	57,82
			2,823	1,461	3,123	0,472	61,68
$v_s=0,3$	501,74	34,483	2,338	1,601	2,926	0,457	55,09
			2,732	1,481	3,094	0,492	59,31

## Method 2

$$L/d_e = 27/5,31 = 5,08 \rightarrow I_\delta = 0,21 \text{ (Fig. 2.10)}$$

$\delta$ (mm)	$v_s = 0,2$	$v_s = 0,3$
	27,39	25,29

$$\delta_{\text{measured}} = 29,5 \text{ mm}$$

### c) Equivalent Raft Method

L	B	H	L/B	H/B	D/B
26,6	17,28	17,28	1,54	1	1,15
35,24	25,92	17,28	1,36	0,66	1,43

$$P=24200 \text{ KN} \quad v_s = 0,2$$

$$\delta_{i \text{ ave}} = \mu_1 \mu_0 q_n B / E_u$$

$\mu_0$	$\mu_1$	$E_{uave}$	q	$\delta_i$
0,91	0,36	43,16	52,64	6,90
0,907	0,24	66,49	26,49	2,24

$$\delta_{i \text{ ave}} = 9,15 \text{ mm}$$

$$m_b = [(1+v)(1-2v)]/[E_s'(1-v)]$$

$$D/(LB)^{0,5} = 0,932 \rightarrow \mu_d = 0,74$$

$$\text{Cohesive layer} \rightarrow \mu_g = 1$$

$$\delta_c = m_b \sigma_z H \mu_d \mu_g$$

$E_{\text{mid-dr}}$	$m_v$	$\sigma_z$	$\delta_c$
34,53	0,0260	30,01	10,00
53,19	0,0169	9,47	2,05

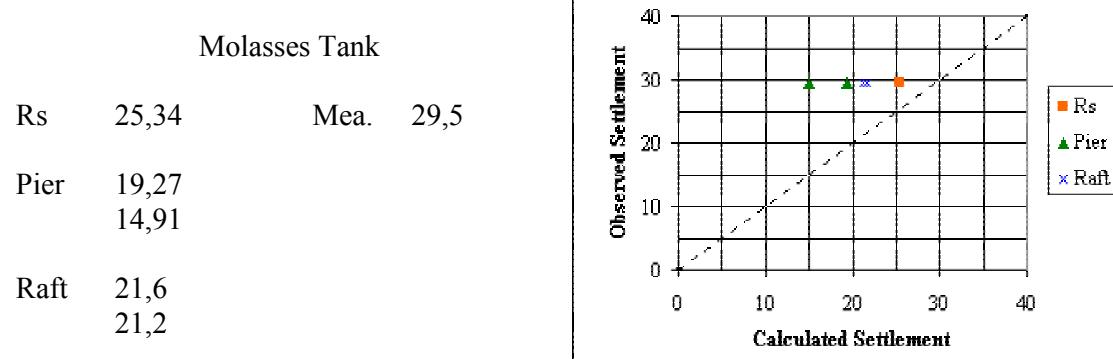
$$\delta_c = 12,05 \text{ mm}$$

$$\delta_T = \delta_{i \text{ ave}} + \delta_c = 21,20 \text{ mm}$$

$$\delta_{\text{measured}} = 29,5 \text{ mm}$$

**Table A.17:** Measured and computed settlements for Molasses Tank (mm)

Set. Ratio		Settlement (mm)									Mea.	
		Equivalent Pier				Equivalent Raft						
		d <sub>e1</sub>		d <sub>e2</sub>		H=16,56 m	H=34,56 m	H=16,56 m (at the tip)	H=28,56 m (1/6)	H=25,56 m (1/8)		
		Met1	Met2	Met1	Met2	Ave.	Ave.	Ave.	Ave.	Ave.		
vs=0,2	25,34	19,27	14,91	57,82	27,40	16,75	21,2	27,71	25,11	27,89	29,5	
		24,24		61,68								
vs=0,3	23,73	17,61	13,77	55,09	25,29	14,38	18,33	24,16	21,75	24,13		
		22,78		59,31								



**Figure A.31:** Measured and computed settlements for Molasses Tank (mm)

## **17. Messeturm Tower (n=64)**

The building has a basement with two underground floors, 58,8 m square in plan, and a 60-storey core shaft (41 m\* 41 m in plan) up to height of 210 m. The estimated total load of the building is 1880 MN. At the site of the Messeturm building there are gravels and sands with a thickness of 8 m, followed by Frankfurt Clay to a depth of more than 100 m below the ground surface.

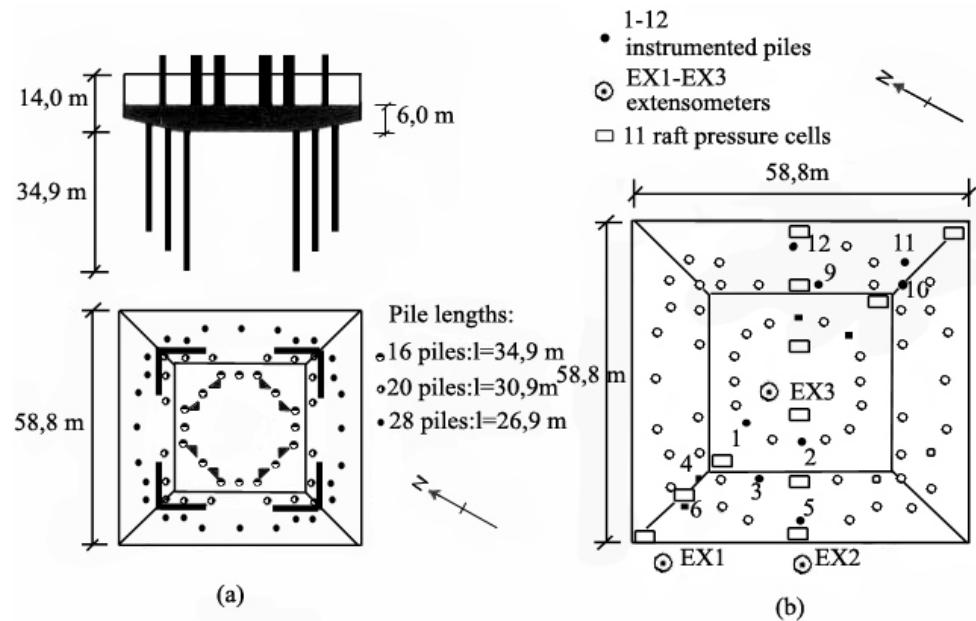
In order to reduce settlements and tilt, the foundation system comprised a base slab or raft supported and stabilised against tilt by 64 large diameter bored piles. The raft is founded at a depth of 14 m below the ground surface on the Frankfurt Clay, and is 9 m below the groundwater table. The thickness of the raft decrease from 6.0 m at the centre to 3.0 m at the edges. The bored piles have a diameter of 1.3 m and are arranged in three concentric circles below the raft. The distance between the piles varies from 3,5 to 6 pile diameters. The pile length varies from 26.9 m for the 28 piles in the outer circle to 30.9 m for the 20 piles in the middle circle, and to 34.9 m for the 16 piles in the inner circle. Calculated range of settlement is 150-200 mm using different methods.(Katzenbach, R. et al., 2000, Poulos, H.G., 2000, Poulos, H.G., 2001)

### **a) Settlement Ratio Method**

$$n = 64 \quad d = 1,3 \text{ m} \quad r_0 = 0,65 \text{ m} \quad s = 4,75 \text{ m}$$

$$P = 1.880 \text{ MN} \quad L = 30,9 \text{ m}$$

$$G = 20 + 1,0z \text{ (MN/m}^2\text{)} \quad E_p = 30000 \text{ MN/m}^2$$



**Figure A.32:** Piled raft foundation for Messeturm building, (a) plan and cross-section (b) location of instrumentation. (Katzenbach et al, 2000, Poulos, 2000, Poulos, 2001)

$$v_s = 0,1 \quad v_s = 0,3 \quad \text{Frankfurt Clay}$$

$$\lambda = E_p/G_l = 30000/56,9 \approx 572,24$$

$$\rho = G_{l/2}/G_l = 0,728 \rightarrow 0,99$$

$$\log \lambda = 2,722 \rightarrow 0,93$$

$$s/d = 4,75 \rightarrow 0,88$$

$$L/d = 23,769 \rightarrow 0,54$$

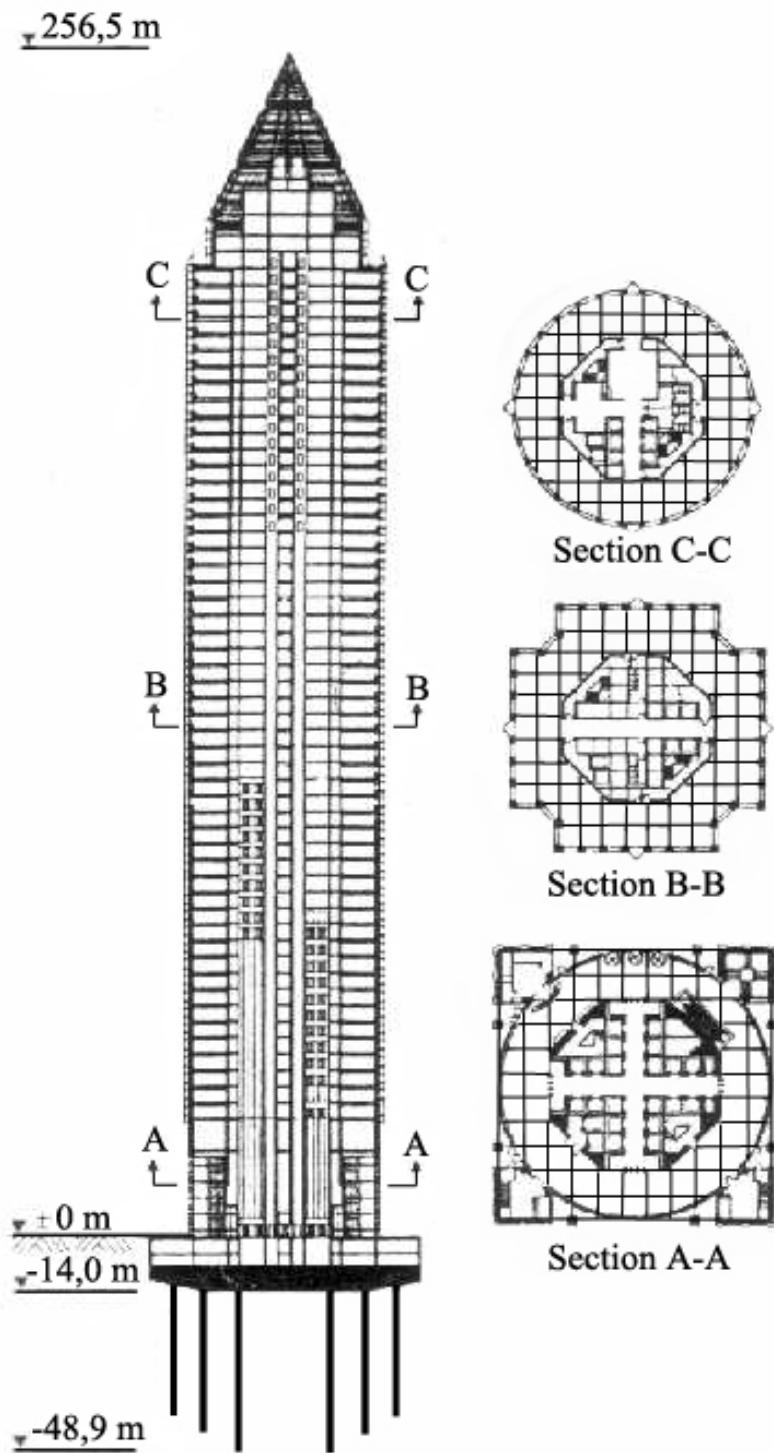
$$v_s = 0,1 \rightarrow 1,05$$

$$v_s = 0,3 \rightarrow 1$$

$$\eta_w = n^e \quad R_s = n^e$$

$$\zeta = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et al., 1992})$$

$$\eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 1$$



**Figure A.33:** Messeturm building, cross-sections .(Katzenbach et al, 2000, Poulos, 2000, Poulos, 2001)

$$\mu L = (2/(\lambda\zeta))^{0.5} L/r_0$$

$$P_{\text{single}} = 1880000/64 = 29375 \text{ KN}$$

	e	$\eta_w$	R_s	$\zeta$	$\mu L$	$\tan \mu L L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s=0,1$	0,459	0,147	6,756	4,356	1,403	30,022	33,309
$v_s=0,3$	0,437	0,162	6,169	4,104	1,445	29,431	34,983

	$P_t/w_t$	K=n $\eta_w k$	$\delta=P/K(\text{mm})$	$P_{\text{single}}/k$	$\delta=\delta_s R_s$
$v_s=0,1$	1231,954	11668,88	161,11	23,84	161,11
$v_s=0,3$	1293,872	13422,63	140,06	22,70	140,06

$$\delta_{\text{measured}} = 130 \text{ mm}$$

### b) Equivalent Pier Method

$$B = A_G^{0.5} = 58,8 \text{ m}$$

$$A_p = \pi d^2 n / 4 = 84,9487 \text{ m}^2$$

$$E_p = 30000 \text{ MPa}$$

$$E_s' = 125,18 \text{ MPa} \quad E_u = 170,7 \text{ MPa}$$

$$d_e = 1,27 A_G^{0.5} = 74,676 \text{ (for friction piles)}$$

$$\rho = 0,728 \quad L = 30,9 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-v) L / r_0) \text{ (W. Fleming, et al., 1992)}$$

$$\zeta_2 = \ln / \{ 5 + [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L / r_0 \} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,1$	859,199	15,100	0,304	0,545	0,377	0,298	60,08
			1,849	0,221	0,407	0,733	147,43
$v_s=0,3$	881,4	15,49	0,053	1,285	0,276	0,104	17,80
			1,800	0,221	0,407	0,732	124,55

### Method 2

$$L/d_e = 30,9/74,676 = 0,413 \rightarrow I_\delta = 0,5 \text{ (Fig. 2.10)}$$

$\delta$ (mm)	$v_s=0,1$	$v_s=0,3$
	100,55	85,08

$$K \approx 200 \text{ (pile stiffness factor)} \quad s/d \approx 4,75 \quad L/d \approx 23,769 \quad B=58,8 \text{ m}$$

$$d_e/B \approx 0,77 \text{ assumed, then } d_e \approx 45,276 \text{ m (Fig.2.9)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,1$	859,199	15,100	0,805	0,553	0,620	0,427	141,70
			1,979	0,353	0,655	0,660	219,20
$v_s=0,3$	881,4	15,49	0,554	0,659	0,598	0,380	106,69
			1,908	0,355	0,655	0,677	190,12

## Method 2

$$L/d_e = 30,9/45,276 = 0,68 \rightarrow I_\delta = 0,47 \text{ (Fig. 2.10)}$$

$\delta$ (mm)	$v_s=0,1$	$v_s=0,3$
	155,90	131,91

$$\delta_{\text{measured}} = 130 \text{ mm}$$

## c) Equivalent Raft Method

L	B	H	L/B	H/B	D/B
62	62	40	1	0,645	0,558
82	82	40	1	0,487	0,909

$$P = 1880000 \text{ KN} \quad v_s = 0,1$$

$$\delta_{i \text{ ave}} = \mu_1 \mu_0 q_n B / E_u$$

$\mu_0$	$\mu_1$	$E_{uave}$	q	$\delta_i$
0,93	0,23	199,8	489,07	32,46
0,92	0,18	320,4	279,59	11,84

$$\delta_{i \text{ ave}} = 44,31 \text{ mm}$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)]$$

$$D/(LB)^{0,5} = 0,558 \rightarrow \mu_d = 0,83$$

$$\text{Frankfurt Clay} \rightarrow \mu_g = 0,7$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g$$

$E_{\text{mid-dr}}$	$m_v$	$\sigma_z$	$\delta_c$
146,52	0,0066	322,78	50,06
234,96	0,0041	134,49	13,00

$$\delta_c = 63,06 \text{ mm}$$

$$\delta_T = \delta_{i \text{ ave}} + \delta_c = 107,38 \text{ mm}$$

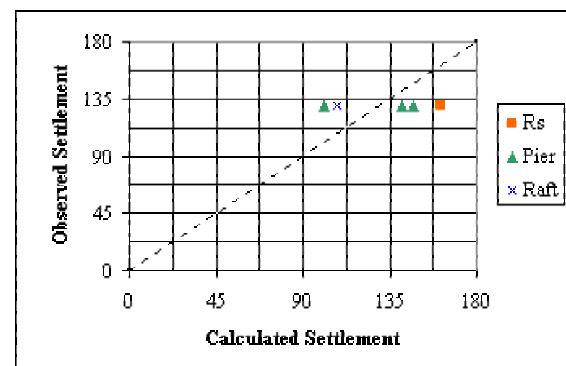
$$\delta_{\text{measured}} = 130 \text{ mm}$$

**Table A.18:** Measured and computed settlements for Messeturn Building (mm)

Settlement (mm)										
Set. Ratio	Equivalent Pier				Equivalent Raft (ave.)				Mea.	
	d <sub>e1</sub>		d <sub>e2</sub>		H=80 m (at the tip)	H=71 m	H=80 m (1/6)	H=80 m (1/8)		
	Met1	Met2	Met1	Met2						
vs=0,1	161,11	60,08	100,55	141,7	155,9	107,38	113,75	115,21	120,88	
		147,43		219,2						
vs=0,3	140,06	17,8	85,08	106,69	131,91	84,85	90,75	91,24	95,91	
		124,55		190,12						

Messe Turm

Rs	161,11	Mea.	130
Pier	147,43		
	100,55		
	141,70		
Raft	107,38		



**Figure A.34:** Measured and computed settlements for Messeturn Building (mm)

## **18. New Law Court Building I, Naples (n=82-77-82)**

The building (cases 18,19,20) belongs to the New Directional Centre of Naples, in the eastern area of the town. It consists of three towers, ranging in the height between 70 m (Tower C ) and 110 m (Tower A), and has a steel frame structure with reinforced concrete stiffening cores.

The foundation is a reinforced concrete slab, 1 m thick, stiffened by heavy reinforced concrete frames in lower stages and resting on 241 (Tower A:82, Tower B:77, Tower C:82), bored piles with a length of 42 m and diameters ranging between 1.5 m and 2.2 m. Equipped with a preloading cell at the base.

Starting from the ground surface and moving downwards, the following soils are typically found; made ground; volcanic ashes and organic soils; stratified sands; pozzolana, cohesionless or slightly indurated; volcanic tuff. The groundwater table is found at a shallow depth below the ground surface, located at an average elevation of 5 m above mean sea level. The predicted settlements by GRUPPALO (NL analysis) are 32,7 mm, 32,5 mm, 24,8 mm for Towers A,B,C.(Mandolini, A., and Viggiani, C., 1997)

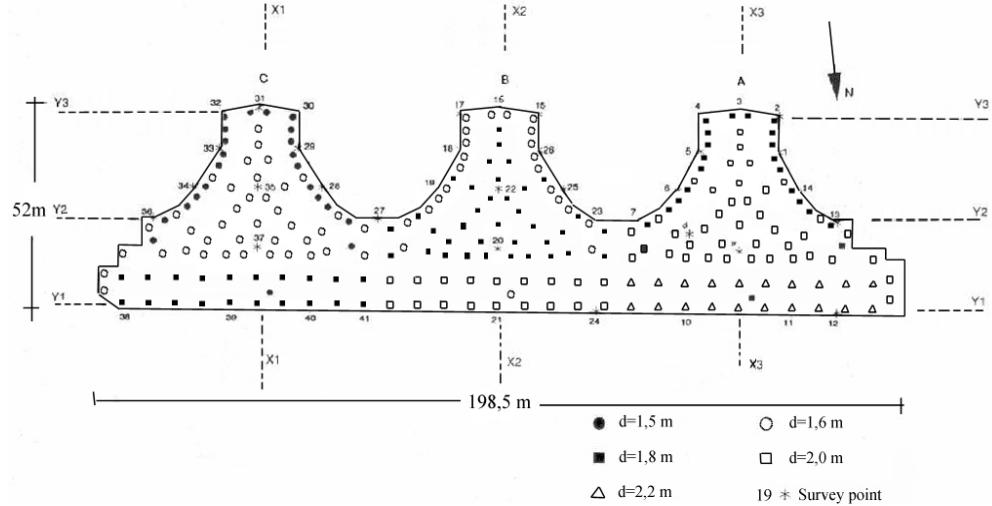
### **a) Settlement Ratio Method**

$$n = 82 \quad d = 2 \text{ m} \quad r_0 = 1 \text{ m}$$

$$L = 42 \text{ m} \quad s/d \approx 2,9$$

$$E_l = 39,3 \text{ MN/m}^2 \quad E_p = 47160 \text{ MN/m}^2$$

$$\nu_s = 0,2 \quad \nu_s = 0,3$$



**Figure A.35:** Layout of the foundation (Mandolini and Viggiani, 1997)

$$P=567875 \text{ KN}$$

$$\lambda = E_p/G_I = 47160/39,3 \approx 1200$$

$$\rho = G_{I/2}/G_I = 1 \rightarrow 1,06$$

$$\log \lambda = 3,079 \rightarrow 1,01$$

$$s/d = 2,9 \rightarrow 1,01$$

$$L/d = 21 \rightarrow 0,536$$

$$v_s = 0,2 \rightarrow 1,03$$

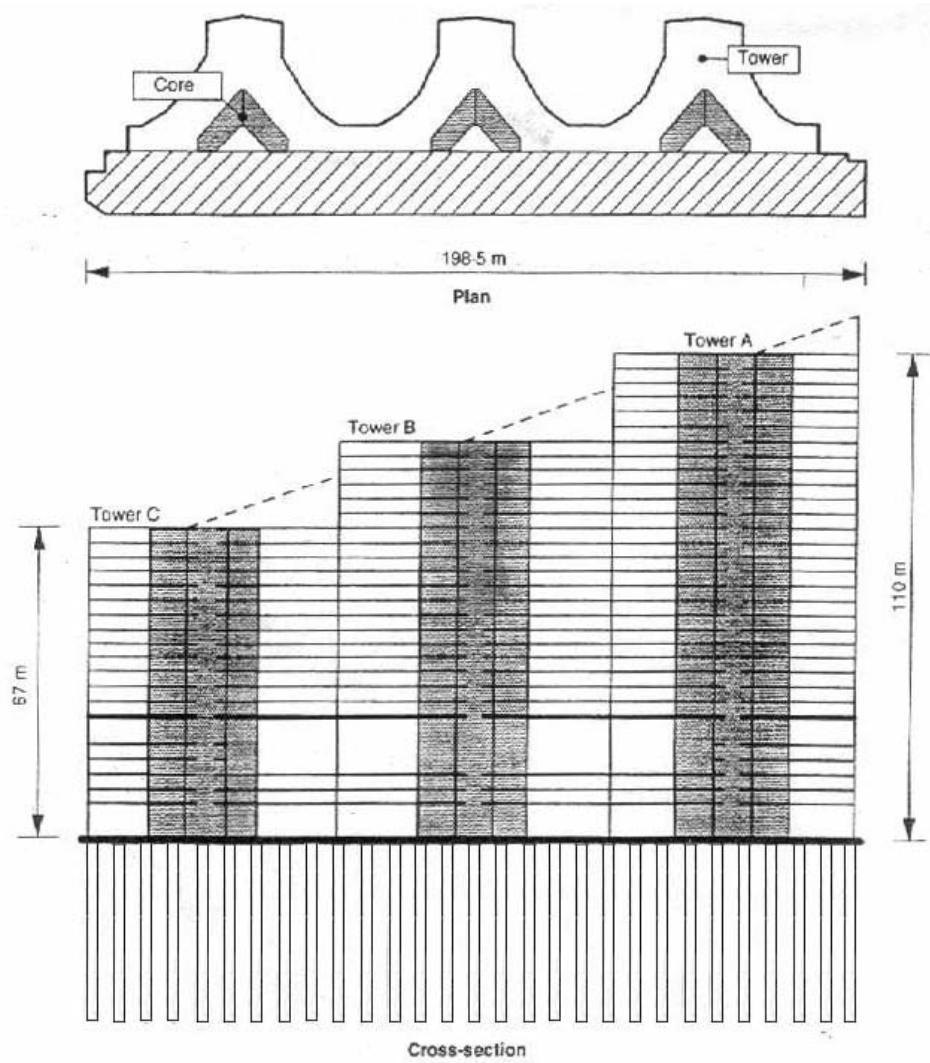
$$v_s = 0,3 \rightarrow 1$$

$$\eta_w = n^{-e} \quad R_s = n^e$$

$$\zeta = \ln \{ [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L/r_0 \} \quad (\text{W. Fleming, et al., 1992})$$

$$\eta = r_b/r_0 = 1 \quad \xi = G_I/G_b = 0,3$$

$$\mu L = (2/(\lambda \zeta))^{0,5} L/r_0$$



**Figure A.36:** Schematic plan and section of the structure (Mandolini and Viggiani, 1997)

$$P_{\text{single}} = 567875/82 = 6925,3 \text{ KN}$$

	e	$\eta_w$	$R_s$	$\zeta$	$\mu L$	$\tanh \mu L L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s=0,2$	0,596	0,072	13,883	3,483	0,918	33,156	66,705
$v_s=0,3$	0,579	0,077	12,859	3,381	0,932	32,958	68,834

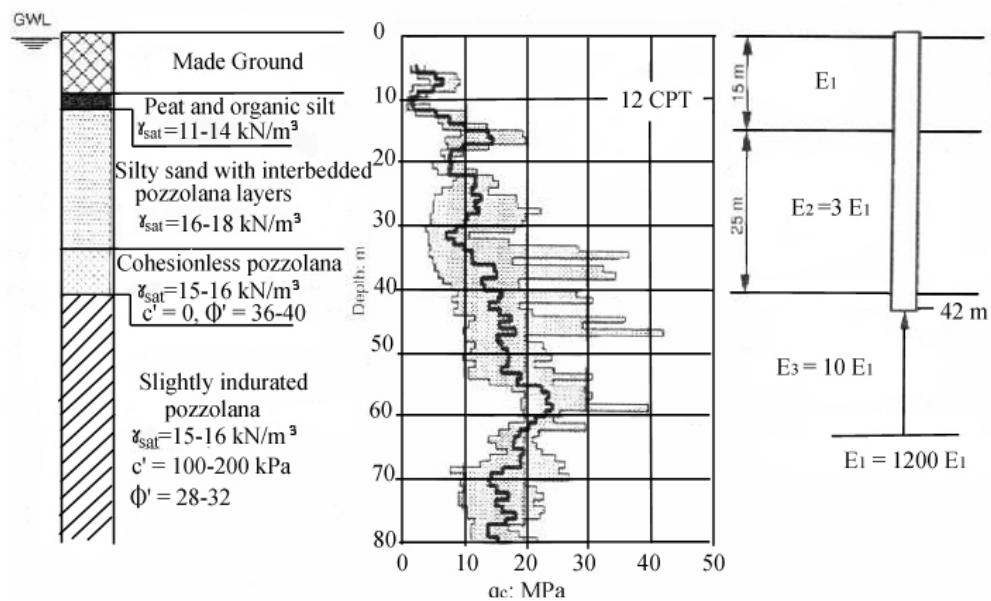
	$P_t/W_t$	$K = n\eta_w k$	$\delta = P/K(\text{mm})$	$P_{\text{single}}/k$	$\delta = \delta_s R_s$
$v_s=0,2$	2621,520	15483,980	36,67	2,64	36,66
$v_s=0,3$	2705,194	17250,59	32,92	2,56	32,92

$$\delta_{\text{measured}} = 28,1 \text{ mm}$$

### b) Equivalent Pier Method

$$B = A_G^{0.5} = 47,21 \text{ m}$$

$$A_p = \pi d^2 n / 4 = 257,61 \text{ m}^2$$



**Figure A.37:** Subsoil profile and properties, and subsoil model adopted in the analysis (Mandolini and Viggiani, 1997)

$$E_p = 47160 \text{ MPa}$$

$$E_s' = 94,32 \text{ MPa} \quad E_u = 117,9 \text{ MPa}$$

$$d_e = 1,13 \text{ A}_G^{0,5} = 53,34 \text{ m (for end bearing piles)}$$

$$\rho = 1 \quad L = 42 \text{ m} \quad \xi = G_l/G_b = 0,3$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln \{ [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L / r_0 \} \quad (\text{W. Fleming, et al., 1992})$$

$$\zeta_2 = \ln \{ 5 + [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L / r_0 \} \quad (\text{K. Horikoshi, M. Randolph, 1999})$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s = 0,2$	5534,335	140,822	0,199	0,420	0,744	0,079	8,99
			1,827	0,138	0,782	0,230	26,02
$v_s = 0,3$	5541,286	140,999	0,097	0,601	0,704	0,050	5,22
			1,808	0,139	0,782	0,226	23,61

### Method 2

$$L/d_e = 42/53,34 = 0,78 \quad E_b/E_s = 393/117,9 = 3,33 \rightarrow I_\delta = 0,225 \text{ (Fig. 2.10)}$$

$\delta$ (mm)	$v_s = 0,2$	$v_s = 0,3$
	25,39	23,44

$$K \approx 400 \text{ (pile stiffness factor)} \quad s/d \approx 2,9 \quad L/d \approx 21 \quad B = 47,21 \text{ m}$$

$$d_e/B \approx 0,82 \text{ assumed, then } d_e \approx 38,71 \text{ m (Fig. 2.9)}$$

## Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu l$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,2$	5534,335	140,822	0,519	0,358	1,040	0,123	19,24
			1,899	0,187	1,072	0,218	33,95
$v_s=0,3$	5541,286	140,999	0,417	0,399	1,030	0,113	16,24
			1,874	0,188	1,072	0,216	31,08

## Method 2

$$L/d_e = 42/38,71 = 1,084 \quad E_b/E_s = 393/117,9 = 3,33 \rightarrow I_\delta = 0,21 \text{ (Fig. 2.10)}$$

	$v_s=0,2$	$v_s=0,3$
$\delta \text{ (mm)}$	32,66	30,14

$$\delta_{\text{measured}} = 28,1 \text{ mm}$$

## c) Equivalent Raft Method

$$L=59,12 \text{ m} \quad B=51,21 \text{ m} \quad H=102,4 \text{ m}$$

$$L/B=1,154 \quad D/B=0,806 \quad H/B=2$$

$$P=567875 \text{ KN}$$

$$q_n=P/(B*L) = 187,570 \text{ KN}$$

$$E_u=393 \text{ Mpa} \quad E_s'=314,4 \text{ Mpa}$$

$$\mu_1 = 0,54 \quad \mu_0 = 0,92$$

$$\delta_{i \text{ ave}} = \mu_1 \mu_0 q_n B / E_u = 0,92 \cdot 0,54 \cdot 187,570 \cdot 51,21 / 393 = 12,14 \text{ mm}$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)] \approx 0,0029$$

$$z/B = 1 \quad \sigma_z/q = 0,29 \quad \sigma_z = 54,395 \text{ kN/m}^2$$

$$D/(LB)^{0,5} = 0,750 \rightarrow \mu_d = 0,775$$

$$\text{Stiff Clay} \rightarrow \mu_g = 0,85$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g = 0,0029 \cdot 54,395 \cdot 102,4 \cdot 0,775 \cdot 0,85 = 10,51 \text{ mm}$$

$$\delta_T = \delta_i + \delta_c = 22,65 \text{ mm}$$

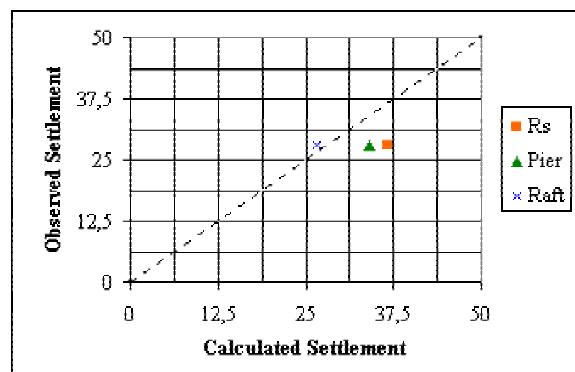
$$\delta_{\text{measured}} = 28,1 \text{ mm}$$

**Table A.19:** Measured and computed settlements for New Law Court I (mm)

		Settlement (mm)								Mea.
Set. Ratio	vs=0,2	Equivalent Pier				Equivalent Raft (ave.)				Mea.
		d <sub>e1</sub>		d <sub>e2</sub>		H=101,1m	H=102,4 m	H=101 m	H=129 m	
		Met1	Met2	Met1	Met2	end-bearing piles		friction piles		
vs=0,2	36,67	8,99	25,39	19,24	33,95	32,66	22,29	22,65	25,34	28,10
		26,02		33,95					26,5	
vs=0,3	32,92	5,22	23,44	16,24	31,08	30,14	19,82	20,15	21,61	22,75
		23,61		31,08					22,75	

New Law I

Rs	36,67	Mea.	28,1
Pier	33,95		
Raft	26,5		



**Figure A.38:** Measured and computed settlements for New Law Court I (mm)

## **19. New Law Court Building II, Naples**

### **a) Settlement Ratio Method**

$$n = 77 \quad d = 1,8 \text{ m} \quad r_0 = 0,9 \text{ m}$$

$$L = 42 \text{ m} \quad s/d \approx 3,375 \text{ m}$$

$$E_p = 47160 \text{ MN/m}^2$$

$$v_s = 0,2 \quad v_s = 0,3$$

$$P = 449220 \text{ KN}$$

$$\lambda = E_p/G_l = 47160/39,3 \approx 1200$$

$$\rho = G_{l/2}/G_l = 1 \rightarrow 1,06$$

$$\log \lambda = 3,079 \rightarrow 1,01$$

$$s/d = 3,375 \rightarrow 0,98$$

$$L/d = 23,33 \rightarrow 0,54$$

$$v_s = 0,2 \rightarrow 1,03$$

$$v_u = 0,5 \rightarrow 0,93$$

$$\eta_w = n^{-e} \quad R_s = n^e$$

$$\zeta = \ln \{ [0,25 + (2,5 \rho (1-v) - 0,25)\xi] L/r_0 \} \quad (\text{W. Fleming, et al., 1992})$$

$$\eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 0,3$$

$$\mu L = (2/(\lambda \zeta))^{0,5} L/r_0$$

$$P_{\text{single}} = 449220/77 = 5834,02 \text{ KN}$$

	e	$\eta_w$	R_s	$\zeta$	$\mu L$	$\tanh \mu L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s=0,2$	0,583	0,079	12,614	3,588	1,005	35,449	68,073
$v_s=0,3$	0,566	0,085	11,717	3,486	1,020	35,217	70,052

	$P_t / w_t$	$K = n \eta_w k$	$\delta = P / K (mm)$	$P_{\text{single}} / k$	$\delta = \delta_s R_s$
$v_s=0,2$	2407,75	14696,87	30,56	2,423	30,56
$v_s=0,3$	2477,74	16282,97	27,58	2,354	27,58

$$\delta_{\text{measured}} = 31,5 \text{ mm}$$

### b) Equivalent Pier Method

$$B = A_G^{0.5} = 46,14 \text{ m}$$

$$A_p = \Pi d^2 n / 4 = 195,94 \text{ m}^2$$

$$E_p = 47160 \text{ MPa}$$

$$E_s' = 94,32 \text{ MPa} \quad E_u = 117,9 \text{ MPa}$$

$$d_e = 1,13 A_G^{0.5} = 52,13 \text{ m} \text{ (for end bearing piles)}$$

$$\rho = 1 \quad L = 42 \text{ m} \quad \xi = G_l / G_b = 0,3$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln \{ [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L / r_0 \} \quad (\text{W. Fleming, et al., 1992})$$

$$\zeta_2 = \ln \{ 5 + [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L / r_0 \} \quad (\text{K. Horikoshi, M. Randolph, 1999})$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,2$	4426,184	112,625	0,222	0,455	0,754	0,086	7,91
			1,832	0,158	0,798	0,233	21,29
$v_s=0,3$	4433,32	112,807	0,120	0,618	0,716	0,059	5,02
			1,812	0,159	0,798	0,229	19,36

### Method 2

$$L/d_e = 42/52,13 = 0,805 \quad E_b/E_s = 393/117,9 = 3,33 \rightarrow I_\delta = 0,225 \text{ (Fig. 2.10)}$$

	$v_s=0,2$	$v_s=0,3$
$\delta \text{ (mm)}$	20,55	18,97

$$K \approx 400 \text{ (pile stiffness factor)} \quad s/d \approx 3,375 \quad L/d \approx 23,33 \quad B = 46,14 \text{ m}$$

$$d_e/B \approx 0,82 \text{ assumed, then } d_e \approx 37,83 \text{ m (Fig. 2.9)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,2$	4426,184	112,625	0,542	0,401	1,054	0,128	16,17
			1,905	0,214	1,093	0,221	27,91
$v_s=0,3$	4433,32	112,807	0,441	0,445	1,042	0,118	13,78
			1,880	0,215	1,093	0,220	25,62

## Method 2

$$L/d_e = 42/37,83 \approx 1,11 \quad E_b/E_s = 393/117,9 = 3,33 \rightarrow I_\delta = 0,21 \text{ (Fig. 2.10)}$$

$\delta$ (mm)	$v_s = 0,2$	$v_s = 0,3$
	26,43	24,40

$$\delta_{\text{measured}} = 31,5 \text{ mm}$$

### c) Equivalent Raft Method

$$L = 59,12 \text{ m} \quad B = 51,21 \text{ m} \quad H = 102,4 \text{ m}$$

$$L/B = 1,154 \quad D/B = 0,806 \quad H/B = 2$$

$$P = 449220 \text{ KN} \quad q_n = P/(B*L) = 148,378 \text{ KN}$$

$$E_u = 393 \text{ MPa} \quad E_s' = 314,4 \text{ MPa}$$

$$\mu_1 = 0,54 \quad \mu_0 = 0,92$$

$$\delta_i = \mu_1 \mu_0 q_n B / E_u = 0,92 \cdot 0,54 \cdot 148,378 \cdot 51,21 / 393 = 9,60 \text{ mm}$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)] \approx 0,0029$$

$$z/B = 1 \quad \sigma_z/q = 0,29 \quad \sigma_z = 43,03 \text{ kN/m}^2$$

$$D/(LB)^{0,5} = 0,750 \rightarrow \mu_d = 0,775$$

$$\text{Stiff Clay} \rightarrow \mu_g = 0,85$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g = 0,0029 \cdot 43,03 \cdot 102,4 \cdot 0,775 \cdot 0,85 = 8,311 \text{ mm}$$

$$\delta_T = \delta_i + \delta_c = 17,92 \text{ mm}$$

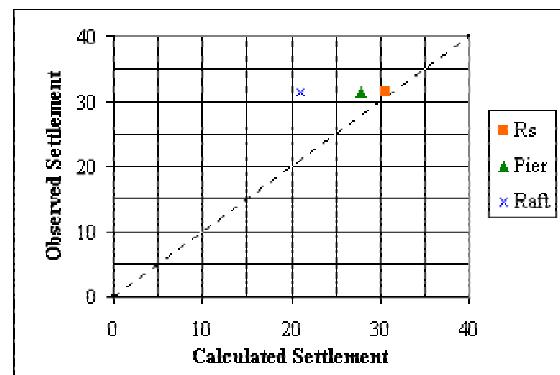
$$\delta_{\text{measured}} = 31,5 \text{ mm}$$

**Table A.20:** Measured and computed settlements for New Law Court II (mm)

Settlement (mm)									
Set. Ratio	Equivalent Pier				Equivalent Raft				Mea.
	d <sub>e1</sub>		d <sub>e2</sub>		H=101,1m	H=102,4 m	H=101 m	H=129 m	
	Met1	Met2	Met1	Met2	end-bearing piles		friction piles		
vs=0,2	30,56	7,91	20,55	16,17	26,43	17,63	17,92	20,05	31,50
		21,29		27,91				20,96	
vs=0,3	27,58	5,02	18,97	13,78	24,40	15,68	15,94	17,09	18
		19,36		25,62					

New Law II

Rs	30,56	Mea.	31,5
Pier	27,91		
Raft	20,96		



**Figure A.39:** Measured and computed settlements for New Law Court II (mm)

## **20. New Law Court Building III, Naples**

### **a) Settlement Ratio Method**

$$n = 82 \quad d = 1,65 \text{ m} \quad r_0 = 0,825 \text{ m}$$

$$L = 42 \text{ m} \quad s/d \approx 3,55 \text{ m}$$

$$E_p = 47160 \text{ MN/m}^2$$

$$v_s = 0,2 \quad v_s = 0,3$$

$$P = 409335 \text{ KN}$$

$$\lambda = E_p/G_l = 47160/39,3 \approx 1200$$

$$\rho = G_{l/2}/G_l = 1 \rightarrow 1,06$$

$$\log \lambda = 3,079 \rightarrow 1,01$$

$$s/d = 3,55 \rightarrow 0,97$$

$$L/d = 25,45 \rightarrow 0,545$$

$$v_s = 0,2 \rightarrow 1,03$$

$$v_u = 0,5 \rightarrow 0,93$$

$$\eta_w = n^{-e} \quad R_s = n^e$$

$$\zeta = \ln \{ [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L/r_0 \} \quad (\text{W. Fleming, et al., 1992})$$

$$\eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 0,3$$

$$\mu L = (2/(\lambda \zeta))^{0,5} L/r_0$$

$$P_{\text{single}} = 409335/82 = 4991,9 \text{ KN}$$

	e	$\eta_w$	R_s	$\zeta$	$\mu L$	$\tanh \mu L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s=0,2$	0,583	0,076	13,051	3,675	1,084	37,319	69,072
$v_s=0,3$	0,566	0,082	12,110	3,573	1,099	37,057	70,926

	$P_t / w_t$	$K = n \eta_w k$	$\delta = P / K (\text{mm})$	$P_{\text{single}} / k$	$\delta = \delta_s R_s$
$v_s=0,2$	2239,51	14070,39	29,09	2,229	29,09
$v_s=0,3$	2299,619	15570,53	26,29	2,170	26,29

$\delta_{\text{measured}} = 25,1 \text{ mm}$

### b) Equivalent Pier Method

$$B = A_G^{0.5} = 47,21 \text{ m}$$

$$A_p = \Pi d^2 n / 4 = 175,33 \text{ m}^2$$

$$E_p = 47160 \text{ MPa}$$

$$E_s' = 94,32 \text{ MPa} \quad E_u = 117,9 \text{ MPa}$$

$$d_e = 1,13 A_G^{0.5} = 53,34 \text{ m} \text{ (for end bearing piles)}$$

$$\rho = 1 \quad L = 42 \text{ m} \quad \xi = G_l / G_b = 0,3$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln \{ [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L / r_0 \} \quad (\text{W. Fleming, et al., 1992})$$

$$\zeta_2 = \ln \{ 5 + [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L / r_0 \} \quad (\text{K. Horikoshi, M. Randolph, 1999})$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,2$	3796,930	96,613	0,199	0,507	0,726	0,083	6,74
			1,827	0,167	0,780	0,236	19,24
$v_s=0,3$	3804,172	96,798	0,097	0,725	0,673	0,053	3,995
			1,808	0,168	0,779	0,233	17,52

### Method 2

$$L/d_e = 42/53,34 = 0,787 \quad E_b/E_s = 393/117,9 = 3,33 \rightarrow I_\delta = 0,225 \text{ (Fig. 2.10)}$$

$\delta$ (mm)	$v_s=0,2$	$v_s=0,3$
	18,30	16,89

$$K \approx 400 \text{ (pile stiffness factor)} \quad s/d \approx 3,55 \quad L/d \approx 25,45 \quad B = 47,21 \text{ m}$$

$$d_e/B \approx 0,82 \text{ assumed, then } d_e \approx 38,71 \text{ m (Fig. 2.9)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,2$	3796,930	96,613	0,519	0,433	1,021	0,129	14,46
			1,899	0,226	1,066	0,226	25,33
$v_s=0,3$	3804,172	96,798	0,418	0,482	1,008	0,118	12,28
			1,874	0,227	1,066	0,225	23,28

## Method 2

$$L/d_e = 42/38,71 \approx 1,08 \quad E_b/E_s = 393/117,9 = 3,33 \rightarrow I_s = 0,21 \text{ (Fig. 2.10)}$$

$\delta$ (mm)	$v_s = 0,2$	$v_s = 0,3$
	23,54	21,73

$$\delta_{\text{measured}} = 25,1 \text{ mm}$$

### c) Equivalent Raft Method

$$L = 59,12 \text{ m} \quad B = 51,21 \text{ m} \quad H = 102,4 \text{ m}$$

$$L/B = 1,154 \quad D/B = 0,806 \quad H/B = 2$$

$$P = 409335 \text{ KN} \quad q_n = P/(B*L) = 135,204 \text{ KN}$$

$$E_u = 393 \text{ MPa} \quad E_s' = 314,4 \text{ MPa}$$

$$\mu_1 = 0,54 \quad \mu_0 = 0,92$$

$$\delta_{i,\text{ave}} = \mu_1 \mu_0 q_n B / E_u = 0,92 \cdot 0,54 \cdot 135,204 \cdot 51,21 / 393 = 8,75 \text{ mm}$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)] \approx 0,0029$$

$$z/B = 1 \quad \sigma_z/q = 0,29 \quad \sigma_z = 39,209 \text{ kN/m}^2$$

$$D/(LB)^{0,5} = 0,750 \rightarrow \mu_d = 0,775$$

$$\text{Stiff Clay} \rightarrow \mu_g = 0,85$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g = 0,0029 \cdot 39,209 \cdot 102,4 \cdot 0,775 \cdot 0,85 = 7,57 \text{ mm}$$

$$\delta_T = \delta_i + \delta_c = 16,33 \text{ mm}$$

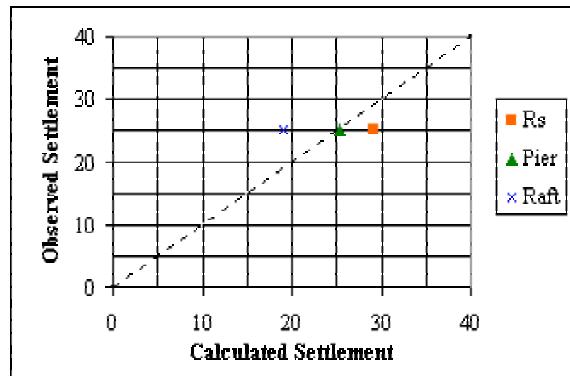
$$\delta_{\text{measured}} = 25,1 \text{ mm}$$

**Table A.21:** Measured and computed settlements for New Law Court III (mm)

		Settlement (mm)								Mea.
Set. Ratio	29,09	Equivalent Pier				Equivalent Raft				Mea.
		d <sub>e1</sub>		d <sub>e2</sub>		H=101,1m	H=102,4 m	H=101 m	H=129 m	
		Met1	Met2	Met1	Met2	end-bearing piles		friction piles		
vs=0,2	29,09	6,74	18,30	14,46	23,54	16,07	16,33	18,27	19,1	25,1
		19,24		25,33						
vs=0,3	26,29	3,99	16,89	12,28	21,73	14,29	14,52	15,58	16,4	25,1
		17,52		23,28						

New Law III

Rs	29,09	Mea.	25,1
Pier	25,33		
Raft	19,10		



**Figure A.40:** Measured and computed settlements for New Law Court III (mm)

## **21. Congress Centre (n=98,43)**

The Congress Centre Messe Frankfurt built in 1995-97 comprises a hotel with 13 storeys, a congress hall, and an office building with 14 storeys next to the hotel. This building complex is situated close to the Messeturm tower in the same subsoil conditions. The raft of the Congress Centre has a thickness of 0.8-2.7 m, and is founded 8 m below street level in the Frankfurt Clay. The raft of 10200 m<sup>2</sup> plan area is supported by 141 bored piles, which are concentrated under the highly loaded parts of the raft to minimise differential settlements. The length and spacing of the 1.3 m diameter piles varies according to the applied load distribution. (Katzenbach, R., Arslan, U., and Moormann, C., 2000)

### **Solution for Hotel**

#### **a) Settlement Ratio Method**

$$n = 98 \quad d = 1,3 \text{ m} \quad r_0 = 0,65 \text{ m}$$

$$L = 28 \text{ m} \quad s = 5,85 \text{ m}$$

$$G = 20 + 1,0z \text{ (MN/m}^2\text{)} \quad E_p = 30000 \text{ MN/m}^2$$

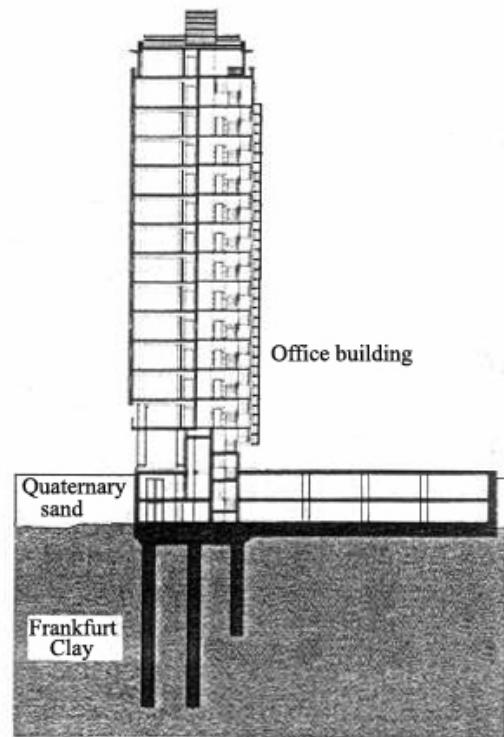
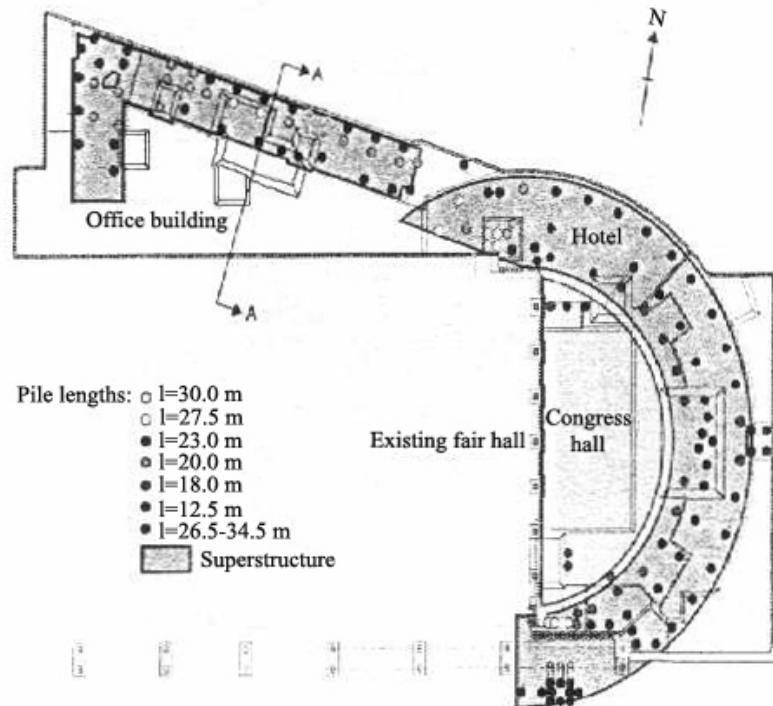
$$v_s = 0,1 \quad v_s = 0,3 \quad \text{Frankfurt Clay}$$

$$P = 1251 \text{ MN}$$

$$\lambda = E_p/G_l = 30000/48 \approx 625$$

$$\rho = G_{l/2}/G_l = 0,708 \rightarrow 0,98$$

$$\log \lambda = 2,79 \rightarrow 0,95$$



**Figure A.41:** Congress Centre Messe Frankfurt, ground plan and section A-A  
(Katzenbach et al, 2000)

$$s/d=4,5 \rightarrow 0,9$$

$$L/d=21,53 \rightarrow 0,531$$

$$v_s=0,1 \rightarrow 1,05$$

$$v_s=0,3 \rightarrow 1$$

$$\eta_w = n^e \quad R_s = n^e$$

$$\zeta = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et al., 1992})$$

$$\eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 1$$

$$\mu L = (2/(\lambda\zeta))^{0,5} L/r_0$$

$$P_{\text{single}} = 1251000/98 = 12765,3 \text{ KN}$$

	e	$\eta_w$	R_s	$\zeta$	$\mu L$	$\tan \mu L L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s=0,1$	0,472	0,114	8,724	4,229	1,185	30,137	1056,153
$v_s=0,3$	0,449	0,127	7,869	3,978	1,221	29,622	35,773

	$P_t/w_t$	K=n $\eta_w k$	$\delta=P/K(\text{mm})$	$P_{\text{single}}/k$	$\delta=\delta_s R_s$
$v_s=0,1$	1056,153	11863,1	105,45	12,08	105,45
$v_s=0,3$	1116,140	13899,15	90,00	11,43	90,00

$$\delta_{\text{measured}} = 50 \text{ mm}$$

### b) Equivalent Pier Method

$$B = A_G^{0,5} = 79,19 \text{ m}$$

$$A_p = \Pi d^2 n / 4 = 130,078 \text{ m}^2$$

$$E_p = 30000 \text{ MPa}$$

$$E_s' = 105,6 \text{ MPa} \quad E_u = 144 \text{ MPa}$$

$$d_e = 1,27 \text{ A}_G^{0,5} = 100,57 \text{ (for friction piles)}$$

$$\rho = 0,708 \quad L = 28 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-v) L / r_0) \text{ (W. Fleming, et al., 1992)}$$

$$\zeta_2 = \ln / \{5 + [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L / r_0\} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s = 0,1$	725,593	15,116	-0,119				
			1,772	0,151	0,276	0,793	93,465
$v_s = 0,3$	744,394	15,508	-0,370				
			1,738	0,151	0,276	0,776	77,411

### Method 2

$$L/d_e = 28/100,57 = 0,278 \rightarrow I_\delta = 0,5 \text{ (Fig. 2.10)}$$

$\delta \text{ (mm)}$	$v_s = 0,1$	$v_s = 0,3$
	58,89	49,83

$$K \approx 200 \text{ (pile stiffness factor)} \quad s/d \approx 4,5 \quad L/d \approx 21,53 \quad B = 79,19 \text{ m}$$

$$d_e/B \approx 0,75 \text{ assumed, then } d_e \approx 59,39 \text{ m (Fig. 2.9)}$$

## Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,1$	725,593	15,116	0,407	0,537	0,430	0,343	68,442
			1,872	0,250	0,461	0,719	143,59
$v_s=0,3$	744,394	15,508	0,155	0,857	0,382	0,205	34,73
			1,819	0,251	0,461	0,722	121,98

## Method 2

$$L/d_e = 28/59,39 = 0,471 \rightarrow I_\delta = 0,46 \quad (\text{Fig. 2.10})$$

$\delta$ (mm)	$v_s=0,1$	$v_s=0,3$
	99,72	84,38

$$\delta_{\text{measured}} = 50 \text{ mm}$$

## c) Equivalent Raft Method

L	B	H	L/B	H/B	D/B
121,3	65,3	42,815	1,85	0,65	0,45
142,71	86,707	42,815	1,64	0,49	0,83

$$P = 1251000 \text{ KN} \quad v_s = 0,1$$

$$\delta_{\text{ave}} = \mu_1 \mu_0 q_n B / E_u$$

$\mu_0$	$\mu_1$	$E_{\text{uave}}$	q	$\delta_i$
0,93	0,24	188,325	157,937	12,22
0,92	0,18	316,775	101,101	4,58

$$\delta_{\text{ave}} = 16,80 \text{ mm}$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)]$$

$$D/(LB)^{0.5} = 0,329 \rightarrow \mu_d = 0,908$$

$$\text{Frankfurt Clay} \rightarrow \mu_g = 0,7$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g$$

$E_{\text{mid-dr}}$	$m_v$	$\sigma_z$	$\delta_c$
138,105	0,00708	112,451	21,66
232,301	0,00421	55,277	6,33

$$\delta_c = 27,99 \text{ mm}$$

$$\delta_T = \delta_i \text{ ave} + \delta_c = 44,80 \text{ mm}$$

$$\delta_{\text{measured}} = 50 \text{ mm}$$

## Solution for Office Building

### a) Settlement Ratio Method

$$n = 43 \quad d = 1,3 \text{ m} \quad r_0 = 0,65 \text{ m}$$

$$L = 28 \text{ m} \quad s = 5,85 \text{ m}$$

$$G = 20 + 1,0z \text{ (MN/m}^2\text{)} \quad E_p = 30000 \text{ MN/m}^2$$

$$v_s = 0,1 \quad v_s = 0,3 \quad \text{Frankfurt Clay}$$

$$P = 549 \text{ MN}$$

$$\lambda = E_p/G_l = 30000/48 \approx 625$$

$$\rho = G_{l/2}/G_l = 0,708 \rightarrow 0,98$$

$$\log \lambda = 2,79 \rightarrow 0,95$$

$$s/d = 4,5 \rightarrow 0,9$$

$$L/d=21,53 \rightarrow 0,531$$

$$v_s=0,1 \rightarrow 1,05$$

$$v_s=0,3 \rightarrow 1$$

$$\eta_w = n^{-e} \quad R_s = n^e$$

$$\zeta = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et al., 1992})$$

$$\eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 1$$

$$\mu L = (2/(\lambda \zeta))^{0.5} L/r_0$$

$$P_{\text{single}} = 549000/43 = 12767,44 \text{ KN}$$

	$e$	$\eta_w$	$R_s$	$\zeta$	$\mu L$	$\tan \mu L L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s=0,1$	0,472	0,169	5,911	4,229	1,185	30,137	33,851
$v_s=0,3$	0,449	0,184	5,432	3,978	1,221	29,622	35,773

	$P_t/w_t$	$K = n \eta_w k$	$\delta = P/K(\text{mm})$	$P_{\text{single}}/k$	$\delta = \delta_s R_s$
$v_s=0,1$	1056,153	7681,805	71,46	12,088	71,46
$v_s=0,3$	1116,140	8834,956	62,14	11,439	62,14

$$\delta_{\text{measured}} = 45 \text{ mm}$$

### b) Equivalent Pier Method

$$B = A_G^{0.5} = 53,68 \text{ m}$$

$$A_p = \pi d^2 n / 4 = 57,07 \text{ m}^2$$

$$E_s' = 105,6 \text{ MPa} \quad E_u = 144 \text{ MPa}$$

$$E_p = 30000 \text{ MPa}$$

$$d_e = 1,27 \text{ A}_G^{0,5} = 68,17 \text{ (for friction piles)}$$

$$\rho = 0,708 \quad L = 28 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-v) L / r_0) \text{ (W. Fleming, et al., 1995)}$$

$$\zeta_2 = \ln / \{5 + [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L / r_0\} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s = 0,1$	697,717	14,535	0,269	0,587	0,369	0,283	21,60
			1,842	0,224	0,404	0,742	56,58
$v_s = 0,3$	716,536	14,927	0,018	2,237	0,179	0,057	3,720
			1,794	0,224	0,404	0,740	47,75

### Method 2

$$L/d_e = 28/68,17 = 0,410 \rightarrow I_\delta = 0,5 \text{ (Fig. 2.10)}$$

	$v_s = 0,1$	$v_s = 0,3$
$\delta \text{ (mm)}$	38,13	32,26

$$K \approx 200 \text{ (pile stiffness factor)} \quad s/d \approx 4,5 \quad L/d \approx 21,53 \quad B = 53,68 \text{ m}$$

$$d_e/B \approx 0,75 \text{ assumed, then } d_e \approx 40,26 \text{ m (Fig. 2.9)}$$

## Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,1$	697,717	14,535	0,796	0,578	0,627	0,431	55,65
			1,976	0,367	0,665	0,667	86,22
$v_s=0,3$	716,536	14,927	0,544	0,689	0,602	0,383	41,87
			1,905	0,368	0,665	0,684	74,84

## Method 2

$$L/d_e = 28/40,26 = 0,695 \rightarrow I_\delta = 0,48 \quad (\text{Fig. 2.10})$$

$\delta$ (mm)	$v_s=0,1$	$v_s=0,3$
	61,98	52,44

$$\delta_{\text{measured}} = 45 \text{ mm}$$

## c) Equivalent Raft Method

L	B	H	L/B	H/B	D/B
90,7	44,7	42,815	2,03	0,95	0,65
112,1	66,1	42,815	1,69	0,64	1,09

$$P = 549000 \text{ KN} \quad v_s = 0,1$$

$$\delta_{i \text{ ave}} = \mu_1 \mu_0 q_n B / E_u$$

$\mu_0$	$\mu_1$	$E_{uave}$	q	$\delta_i$
0,93	0,35	188,325	135,41	10,46
0,92	0,23	316,775	74,07	3,27

$$\delta_{i \text{ ave}} = 13,73 \text{ mm}$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)]$$

$$D/(LB)^{0.5} = 0,461 \rightarrow \mu_d = 0,86$$

$$\text{Frankfurt Clay} \rightarrow \mu_g = 0,7$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g$$

$E_{\text{mid-dr}}$	$m_v$	$\sigma_z$	$\delta_c$
138,105	0,00708	85,309	15,56
232,301	0,00421	30,738	3,33

$$\delta_c = 18,90 \text{ mm}$$

$$\delta_T = \delta_{i \text{ ave}} + \delta_c = 32,63 \text{ mm}$$

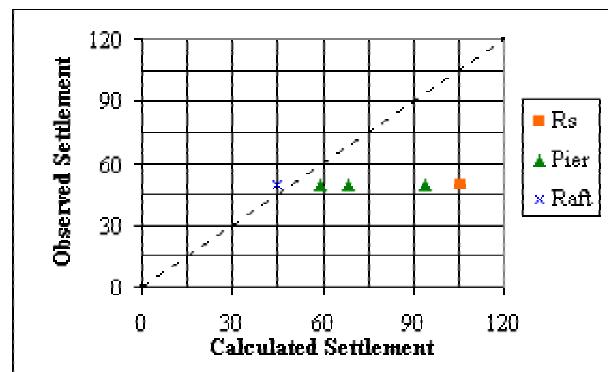
$$\delta_{\text{measured}} = 45 \text{ mm}$$

**Table A.22:** Measured and computed settlements for Congress Centre (mm)

		Settlement (mm)								Mea.	
Set. Ratio		Equivalent Pier (Hotel)				Equivalent Pier (Office B.)					
Hotel	Office Build.	d <sub>e1</sub>		d <sub>e2</sub>		d <sub>e1</sub>		d <sub>e2</sub>			
		Met1	Met2	Met1	Met2	Met1	Met2	Met1	Met2		
vs=0,1	105,45	71,47		58,89	68,42	99,72	21,60	38,13	55,65	61,98	
			93,46		143,59		56,58		86,22		
vs=0,3	90,00	62,14		49,83	34,73	84,38	3,72	32,26	41,87	52,44	
			77,41		121,98		47,75		74,84		

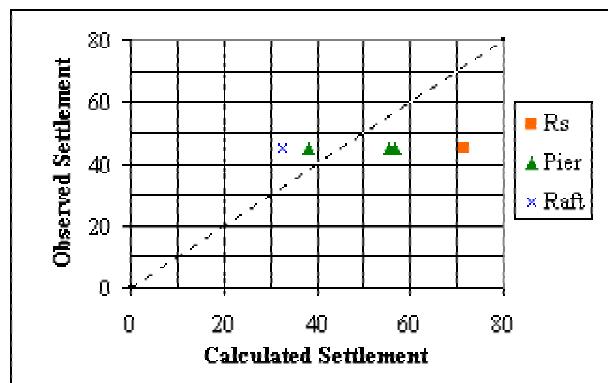
Equivalent Raft								
Hotel				Office Building				
H=85,63 m	H=76,3 m (at the pile tip)	H=85,63 m (1/6)	H=85,63 m (1/8)	H=85,63 m	H=76,3 m	H=85,63 m (1/6)	H=85,63 m (1/8)	
Ave.	Ave.	Ave.	Ave.	Ave.	Ave.	Ave.	Ave.	
vs=0,1	44,8	43,93	47,31	48,85	32,63	33,52	34,34	35,38
vs=0,3	34,8	34,24	36,57	37,83	25,88	26,89	27,25	28,01

Congress Centre - Hotel		
	Rs	Mea.
Pier	93,69	
	58,89	
	68,42	
Raft	44,8	
		50



**Figure A.42:** Measured and computed settlements for Congress Centre Hotel (mm)

Congress Centre - Office Building		
	Rs	Mea.
Pier	56,58	
	38,13	
	55,65	
Raft	32,63	
		45



**Figure A.43:** Measured and computed settlements for Congress Centre Office Building (mm)

## **22. Commerz Bank (n=111)**

The tower stands as the highest office structure in Europe and ranks 24th tallest in the world. The building plan is a rounded equilateral triangle 60 meters wide. Three 52\*131-ft-wide sections join to form the triangular structure with a central atrium. The mat was placed in a 7.5 meter deep excavation and varies from 2.5 to 4.5 meters in thickness. There are 111 piles concentrated in clusters under each of the Tower's columns. A foundation on 111 piles of up to 48.5 m in length and up to 1.8 m in diameter driven into the lower rock was chosen. This rock lies about 30 m beneath the Frankfurt clay. Calculated range of settlement is 60-70 mm using different methods. (Katzenbach, R. et al, 2000, Poulos, H.G., 2000)

### **a) Settlement Ratio Method**

$$n = 111 \quad d = 1,66 \text{ m} \quad r_0 = 0,83 \text{ m}$$

$$L = 45 \text{ m} \quad s = 4,5 \text{ m} \quad E_p = 40000 \text{ MN/m}^2$$

$$G = 20 + 1,0z \text{ (MN/m}^2\text{)} \quad \text{Frankfurt Clay}$$

$$E_u = 20000 \text{ MN/m}^2 \quad \text{Frankfurt Limestone}$$

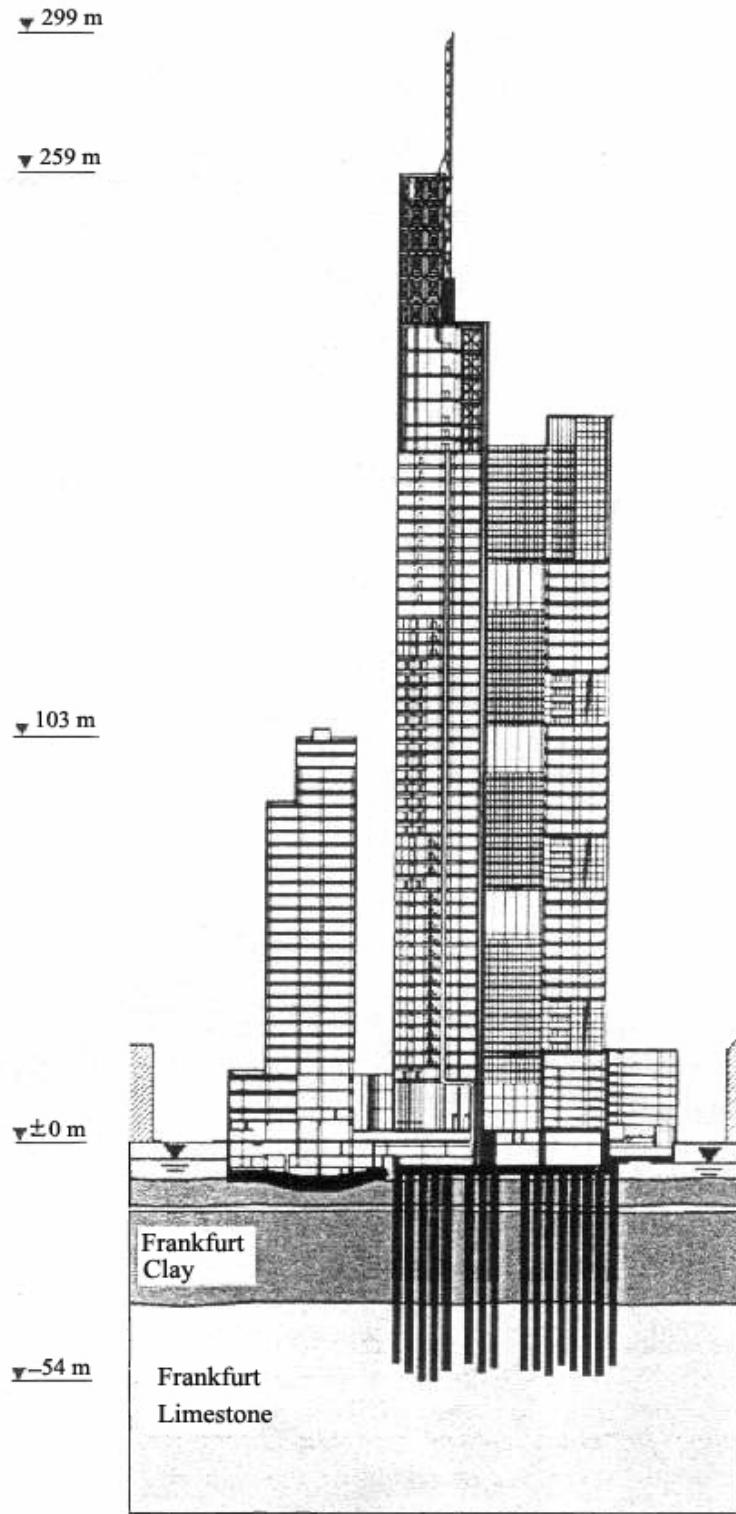
$$\nu_s = 0,1 \quad \nu_s = 0,3$$

$$P = 1300 \text{ MN}$$

$$\lambda = E_p / G_l = 40000 / 49 \approx 816,326$$

$$\rho = G_{l/2} / G_l = 0,704 \rightarrow 0,98$$

$$\log \lambda = 2,911 \rightarrow 0,97$$



**Figure A.44:** Sectional elevation of new Commerzbank Tower (Katzenbach et al, 2000, Poulos, 2000)

$$s/d=4,5 \rightarrow 0,9$$

$$L/d=27,108 \rightarrow 0,547$$

$$v_s=0,1 \rightarrow 1,05$$

$$v_s=0,3 \rightarrow 1$$

$$\eta_w = n^{-e} \quad R_s = n^e$$

$$\eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 0,00735$$

$$\zeta = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et al., 1992})$$

$$\mu L = (2/(\lambda\zeta))^{0,5} L/r_0$$

$$P_{\text{single}} = 1300000/111 = 11711,71 \text{ KN}$$

	e	$\eta_w$	R_s	$\zeta$	$\mu L$	$\tan \mu L \ L / (\mu L \ r_0)$	$P_t / (w_t G_l r_0)$
$v_s=0,1$	0,419	0,098	10,116	2,645	1,650	30,520	80,003
$v_s=0,3$	0,467	0,110	9,060	2,635	1,653	30,477	80,926

	$P_t/w_t$	K=n $\eta_w k$	$\delta = P/K(\text{mm})$	$P_{\text{single}}/k$	$\delta = \delta_s R_s$
$v_s=0,1$	3253,725	35700,51	36,41	3,599	36,41
$v_s=0,3$	3291,282	40319,68	32,24	3,558	32,24

$$\delta_{\text{measured}} = 15-19 \text{ mm}$$

## b) Equivalent Pier Method

$$B = A_G^{0.5} = 46,37 \text{ m}$$

$$A_p = \pi d^2 n / 4 = 240,231 \text{ m}^2$$

$$E_p = 40000 \text{ MPa}$$

$$E_s' = 107,8 \text{ MPa} \quad E_u = 147 \text{ MPa}$$

$$d_e = 1,13 \text{ A}_G^{0,5} = 52,398 \quad (\text{for end-bearing piles})$$

$$\rho = 0,704 \quad L = 45 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-v) L / r_0) \quad (\text{W. Fleming, et al., 1992})$$

$$\zeta_2 = \ln / \{ 5 + [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L / r_0 \} \quad (\text{K. Horikoshi, M. Randolph, 1999})$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s = 0,1$	4564,80	93,159	-0,806				
			1,694	0,193	0,848	0,032	7,489
$v_s = 0,3$	4582,21	93,514	-0,816				
			1,694	0,192	0,848	0,036	7,11

### Method 2

$$L/d_e = 45/52,398 = 0,858 \rightarrow I_\delta = 0,023 \quad (\text{Fig. 2.10.})$$

	$v_s = 0,1$	$v_s = 0,3$
$\delta \text{ (mm)}$	5,29	4,48

$$K \approx 270 \text{ (pile stiffness factor)} \quad s/d \approx 4,5 \quad L/d \approx 27,108 \quad B = 46,37 \text{ m}$$

$$d_e/B \approx 0,78 \text{ assumed, then } d_e \approx 36,16 \text{ m} \quad (\text{Fig. 2.9})$$

## Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,1$	4564,80	93,159	-0,436				
			1,731	0,277	1,213	0,043	14,44
$v_s=0,3$	4582,21	93,514	-0,446				
			1,729	0,276	1,213	0,049	13,89

## Method 2

$$L/d_e = 45/36,16 = 1,244 \rightarrow I_\delta = 0,0328$$

$\delta$ (mm)	$v_s=0,1$	$v_s=0,3$
	9,33	7,89

$$\delta_{\text{measured}} = 15-19 \text{ mm}$$

## c) Equivalent Raft Method

$$\delta = \% 0,01-0,05 B \text{ (M. J. Tomlinson, 1986)}$$

$$\text{For } B = 46,37$$

$$\delta = 4,637 - 23,185 \quad (\text{ave} = 13,911)$$

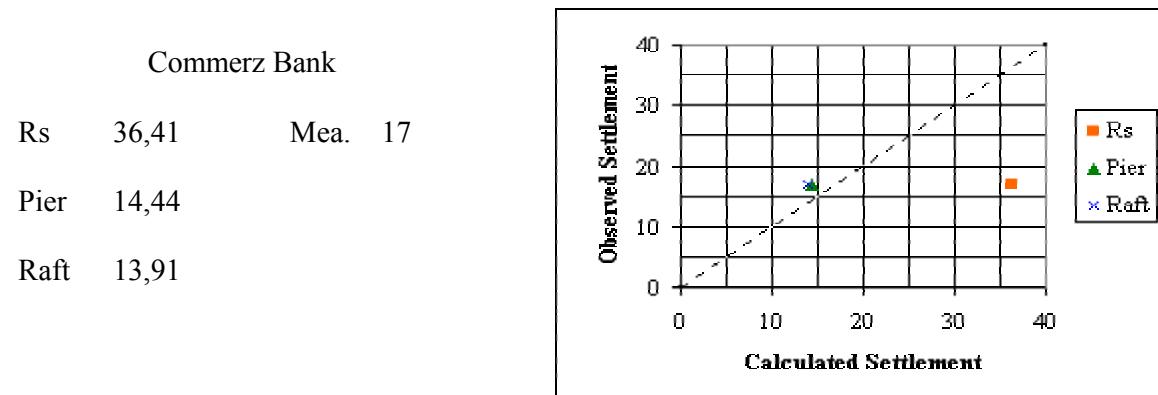
$$\text{For } B = 39,48$$

$$\delta = 3,948 - 19,74 \quad (\text{ave} = 11,844)$$

$$\delta_{\text{measured}} = 15-19 \text{ mm}$$

**Table A.23:** Measured and computed settlements for Commerz Bank (mm)

Settlement (mm)												
Set. Ratio	Equivalent Pier								Equivalent Raft			Mea.
	B*L=2150 m2				B*L=1558 m2				B=46,37 m	B=39,48 m		
	d <sub>e1</sub>		d <sub>e2</sub>		d <sub>e1</sub>		d <sub>e2</sub>		Ave	Ave		
	Met1	Met2	Met1	Met2	Met1	Met2	Met1	Met2				
vs=0,1	36,41		5,29		9,33		6,75		11,74	13,91	11,84	17
		7,49		14,44		7,81		14,91				
vs=0,3	32,24		4,48		7,89		5,71		9,94	(4,63 - 23,18)	(3,94 - 19,74)	(15-19)
		7,11		13,89		7,37		14,29				



**Figure A.45:** Measured and computed settlements for Commerz Bank (mm)

## **23. Main Tower (n=112)**

The new Main Tower skyscraper with five basement levels, ground floor and a further 57 storeys above grade, will rise to a height of 198 m. The raft is founded at the considerable depth of 21 m below street level, which is 14 m below groundwater level. The entire excavation for the Main Tower building has a plan area 50m\*85m and fully equipped with a five-storey parking basement. The Main Tower core shaft has dimensions of 30m\*50m in plan, and arranged asymmetrically with respect to the basement. The total load of the Main Tower building is about 2000 MN. The raft has a plan area 3800 m<sup>2</sup> with a thickness of 3,8 m in the centre, and 3,0 m in the remaining area. The piled raft incorporates 112 large-diameter bored piles and a secant bored pile wall, which is connected to the raft. The piles have a diameter of 1.5 m and a length of 30 m, except for some 20 m long piles near the edge of the raft. The bases of the 30 m piles are situated 5-8 m above the upperboundary of the Frankfurt Limestone. (Katzenbach, R., Arslan, U., and Moormann, C., 2000)

### **a) Settlement Ratio Method**

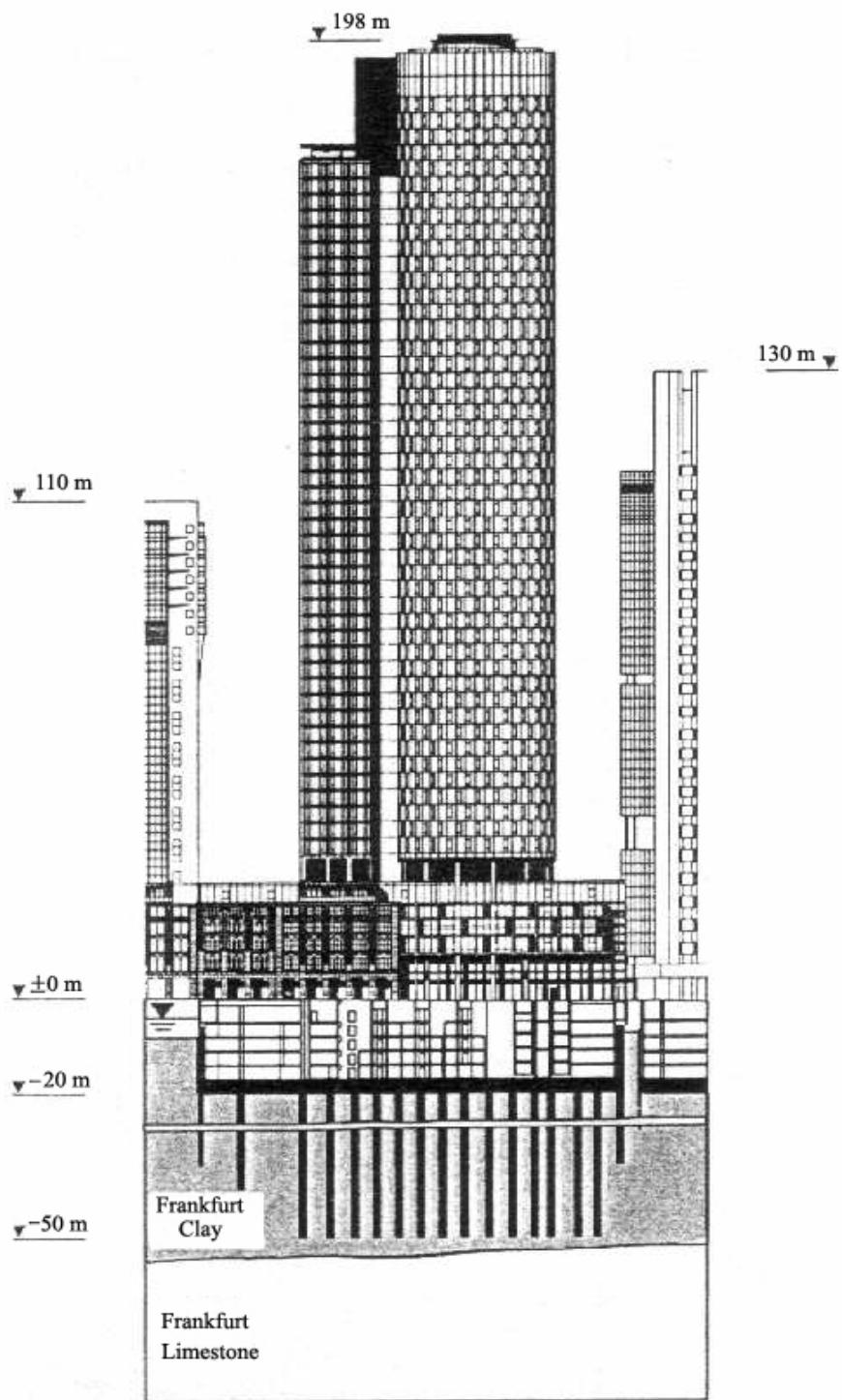
$$n = 112 \quad d = 1,5 \text{ m} \quad r_0 = 0,75 \text{ m}$$

$$L = 30 \text{ m} \quad s = 4,5 \text{ m}$$

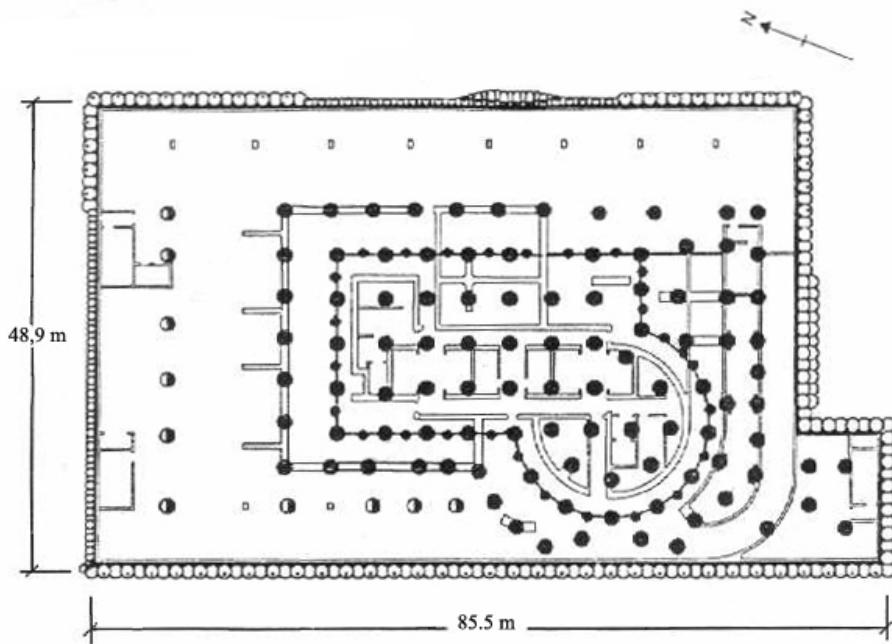
$$G = 20 + 1,0z \text{ (MN/m}^2\text{)} \quad \text{Frankfurt Clay} \quad E_p = 35000 \text{ MN/m}^2$$

$$E_u = 20000 \text{ MN/m}^2 \quad \text{Frankfurt Limestone}$$

$$P = 2000 \text{ MN} \quad v_s = 0,1 \quad v_s = 0,3$$



**Figure A.46:** Sectional elevation of Main Tower building (Katzenbach et al, 2000)



**Figure A.47:** Plan of piled raft foundation for Main Tower building (Katzenbach et al, 2000)

$$\lambda = E_p / G_l = 35000 / 61 \approx 573,770$$

$$\rho = G_{l/2} / G_l = 0,754 \rightarrow 1$$

$$\log \lambda = 2,758 \rightarrow 0,94$$

$$s/d = 4,5 \rightarrow 0,9$$

$$L/d = 20 \rightarrow 0,536$$

$$v_s = 0,1 \rightarrow 1,05$$

$$v_s = 0,3 \rightarrow 1$$

$$\eta_w = n^e \quad R_s = n^e \quad \eta = r_b / r_0 = 1 \quad \xi = G_l / G_b = 0,00915$$

$$\zeta = \ln(2,5 \rho (1-v) L / r_0) \quad (\text{W. Fleming, et al., 1992})$$

$$\mu L = (2 / (\lambda \zeta))^{0,5} L / r_0$$

$$P_{\text{single}} = 2000000 / 112 = 17857,142 \text{ KN}$$

	e	$\eta_w$	R_s	$\zeta$	$\mu L$	$\tanh \mu L / (\mu L r_0)$	$P_t / (w_t G I r_0)$
$v_s=0,1$	0,476	0,105	9,455	2,354	1,539	23,700	72,216
$v_s=0,3$	0,453	0,117	8,496	2,341	1,543	23,653	73,127

	$P_t / w_t$	$K = n \eta_w k$	$\delta = P / K (mm)$	$P_{\text{single}} / k$	$\delta = \delta_s R_s$
$v_s=0,1$	3303,915	39134,09	51,10	5,404	51,10
$v_s=0,3$	3345,559	44101,82	45,34	5,337	45,34

$\delta_{\text{mea.}} = 20 \text{ mm}$

### b) Equivalent Pier Method

$$B = A_G^{0.5} = 52,32 \text{ m}$$

$$A_p = \pi d^2 n / 4 = 197,92 \text{ m}^2$$

$$E_p = 35000 \text{ MPa}$$

$$E_s' = 134,2 \text{ MPa} \quad E_u = 183 \text{ MPa}$$

$$d_e = 1,13 A_G^{0.5} = 59,12 \text{ (for end-bearing piles)}$$

$$\rho = 0,754 \quad L = 30 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-v) L / r_0) \text{ (W. Fleming, et al., 1992)}$$

$$\zeta_2 = \ln / \{ 5 + [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L / r_0 \} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,1$	2654,53	43,516	-1,32				
			1,661	0,168	0,502	0,041	10,37
$v_s=0,3$	2677,16	43,887	-1,33				
			1,660	0,168	0,502	0,046	9,81

### Method 2

$$L/d_e = 30/59,12 = 0,507 \rightarrow I_\delta = 0,018 \text{ (Fig. 2.10)}$$

	$v_s=0,1$	$v_s=0,3$
$\delta \text{ (mm)}$	4,53	3,83

$$K \approx 190 \text{ (pile stiffness factor)} \quad s/d \approx 4,5 \quad L/d \approx 20 \quad B=53,32 \text{ m}$$

$$d_e/B \approx 0,78 \text{ assumed, then } d_e \approx 40,81 \text{ m} \quad (\text{Fig. 2.9})$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,1$	2654,53	43,516	-0,949				
			1,683	0,242	0,721	0,055	20,08
$v_s=0,3$	2677,16	43,887	-0,962				
			1,683	0,241	0,721	0,062	19,25

## Method 2

$$L/d_e = 30/40,81 = 0,735 \rightarrow I_\delta = 0,02 \quad (\text{Fig. 2.10})$$

$\delta$ (mm)	$v_s = 0,1$	$v_s = 0,3$
	7,30	6,17

$$\delta_{\text{mea.}} = 20 \text{ mm}$$

### c) Equivalent Raft Method

$$L=74 \quad B=37 \quad L/B=2$$

$$H=6,5 \quad D=51 \quad D/B=1,37 \quad H/B=0,175$$

$$E_{\text{uave}}=192,75 \quad E_s' = 141,35$$

$$\mu_0 \rightarrow 0,91 \quad \mu_1 \rightarrow 0,04$$

$$q_n = 2000000/(BL) = 730,46 \text{ KPa}$$

$$\delta_{\text{iave}} = q_n B \mu_0 \mu_1 / E_u = 5,10 \text{ mm}$$

$$D/(LB)^{0,5} = 0,974 \rightarrow \mu_d = 0,732$$

$$\text{Frankfurt Clay} \rightarrow \mu_g = 0,7$$

$$z/B = 0,087 \quad \sigma_z/q = 0,93 \quad \sigma_z = 679,328 \text{ KPa}$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)] \approx 0,00701$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g = 0,00701 \cdot 679,328 \cdot 6,5 \cdot 0,732 \cdot 0,7 \approx 15,87 \text{ mm}$$

$$\delta_{\text{Taverage}} = 20,98 \text{ mm}$$

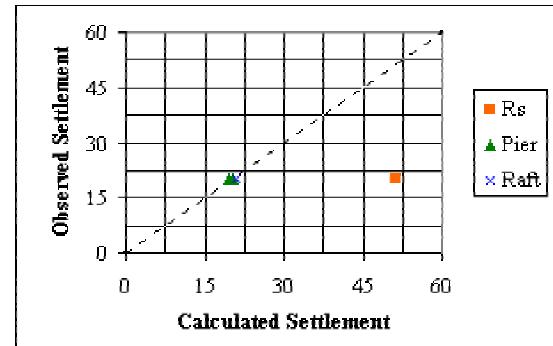
$$\delta_{\text{mea.}} = 20 \text{ mm}$$

**Table A.24:** Measured and computed settlements for Main Tower (mm)

Set. Ratio	Settlement (mm)										Mea.			
	Equivalent Pier								Equivalent Raft					
	B*L(37*74)				B*L(43*80)				B*L (43*80)	B*L (37*74)				
	d <sub>e1</sub>	d <sub>e2</sub>	d <sub>e1</sub>	d <sub>e2</sub>	Met1	Met2	Met1	Met2	Ave.	Ave.				
v <sub>s</sub> =0,1	51,10		4,53		Met1	Met2	Met1	Met2	6,51	17,22	20,98	20 (ave)		
			10,37				7,30		4,04					
				20,08					19,53					
							10,03							
v <sub>s</sub> =0,3	45,35		3,83		6,18				3,42		5,51	12,22	15,16	25 (Max)
			9,81			19,25		9,51		18,74				

Main Tower

Rs	51,1	Mea.	20
Pier	20,08		
	19,53		
Raft	20,98		



**Figure A.48:** Measured and computed settlements for Main Tower (mm)

## 24.Cambridge Road (n=116)

This is one of three 23-storey blocks of maisonettes constructed for the G.L.C. at a site in London Borough of Waltham Forest. One side of the structure is connected to a semi-basement car park.

The structure was founded on 0,62 m diameter straight shafted piles taken to depths of 15 m. The site investigation showed 3 of Toplow Gravel overlying London Clay. (Morton, K., and Au, E., 1974)

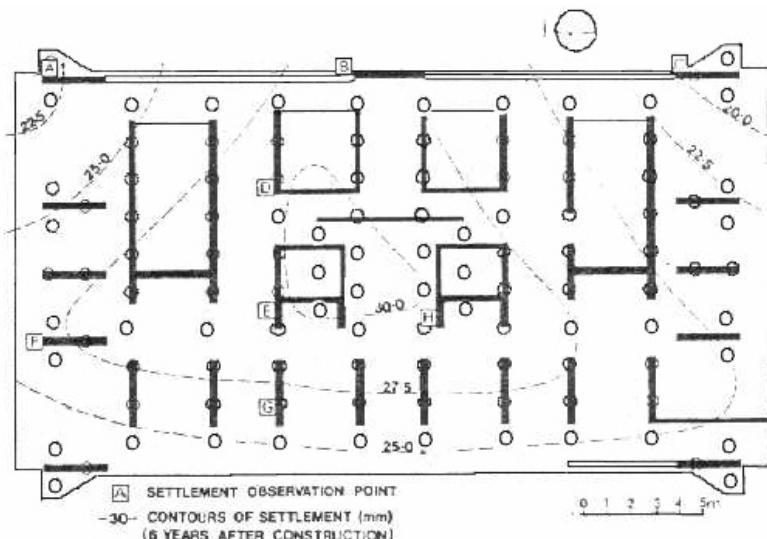
### a) Settlement Ratio Method

$$n = 116 \quad d = 0,62 \text{ m} \quad r_0 = 0,31 \text{ m}$$

$$L = 15,3 \text{ m} \quad s = 4,5 \text{ m}$$

$$c_u = 70-400 \text{ (kN/m}^2\text{)} \quad \text{London Clay}$$

$$N = 23-94 \text{ Taplow Gravel}$$



**Figure A.49:** Cambridge Road foundation plan (Morton and Au, 1974)

$$E_p = 25000 \text{ MN/m}^2$$

$$P=122 \text{ MN} \quad v_s=0,1 \quad v_s=0,3$$

$$\lambda=E_p/G_l=25000/29,1 \approx 859,106$$

$$\rho=G_{l/2}/G_l=23,3/29,1=0,8 \rightarrow 1,02$$

$$\log \lambda = 2,934 \rightarrow 0,97$$

$$s/d=4,5 \rightarrow 0,9$$

$$L/d=24,67 \rightarrow 0,545$$

$$v_s=0,1 \rightarrow 1,05$$

$$v_s=0,3 \rightarrow 1$$

$$\eta_w=n^{-e} \quad R_s=n^e$$

$$\zeta=\ln(2,5 \rho (1-v) L/r_0) \text{ (W. Fleming, et al., 1992)}$$

$$\eta=r_b/r_0=1 \quad \xi=G_l/G_b=1$$

$$\mu L=(2/(\lambda\zeta))^{0,5}L/r_0$$

$$P_{\text{single}}=122000/116=1051,72 \text{ KN}$$

	e	$\eta_w$	R_s	$\zeta$	$\mu L$	$\tan \mu L L/(\mu L r_0)$	$P_t/(w_t G_l r_0)$
$v_s=0,1$	0,509	0,088	11,27	4,400	1,124	35,519	41,817
$v_s=0,3$	0,485	0,099	10,04	4,236	1,157	34,982	43,998

	$P_t/w_t$	K=n $\eta_w k$	$\delta=P/K(\text{mm})$	$P_{\text{single}}/k$	$\delta=\delta_s R_s$
$v_s=0,1$	377,232	3882,309	31,42	2,787	31,42
$v_s=0,3$	396,909	4584,23	26,61	2,649	26,61

$$\delta_{\text{measured}}=27,5 \text{ mm}$$

### b) Equivalent Pier Method

$$B = A_G^{0.5} = 21,908 \text{ m}$$

$$A_p = \pi d^2 n / 4 = 35,02 \text{ m}^2$$

$$E_p = 25000 \text{ MPa}$$

$$E_s' = 64,02 \text{ MPa} \quad E_u = 87,3 \text{ MPa}$$

$$d_e = 1,27 A_G^{0.5} = 27,82 \text{ (for friction piles)}$$

$$\rho = 0,8 \quad L = 15,3 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-v) L / r_0) \text{ (W. Fleming, et al., 1992)}$$

$$\zeta_2 = \ln / \{ 5 + [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L / r_0 \} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s = 0,1$	1883,37	64,72	0,663	0,233	0,540	0,363	24,89
			1,943	0,138	0,548	0,619	42,42
$v_s = 0,3$	1894,16	65,09	0,432	0,293	0,534	0,294	17,09
			1,878	0,140	0,546	0,620	35,94

### Method 2

$$L/d_e = 15,3 / 28,28 = 0,549 \rightarrow I_\delta = 0,5 \text{ (Fig. 2.10)}$$

$\delta \text{ (mm)}$	$v_s = 0,1$	$v_s = 0,3$
	34,24	28,97

$K \approx 280$  (pile stiffness factor)     $s/d \approx 4,5$      $L/d \approx 24,67$      $B=21,908$  m

$d_e/B \approx 0,78$  assumed, then  $d_e \approx 17,37$  m (Fig. 2.9)

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,1$	1883,37	64,72	1,171	0,290	0,870	0,383	42,70
			2,107	0,216	0,881	0,528	58,88
$v_s=0,3$	1894,16	65,09	0,919	0,327	0,864	0,359	33,90
			2,016	0,221	0,881	0,539	50,91

### Method 2

$$L/d_e = 15,3/17,37 = 0,880 \rightarrow I_\delta = 0,43$$

$\delta$ (mm)	$v_s=0,1$	$v_s=0,3$
	47,95	40,57

$$\delta_{\text{measured}} = 27,5 \text{ mm}$$

### c) Equivalent Raft Method

L	B	H	L/B	H/B	D/B
35,1	21,1	21,1	1,66	1	0,48
45,65	31,65	21,1	1,44	0,66	0,98

$$P = 122000 \text{ KN} \quad v_s = 0,1$$

$$\delta_{\text{ave}} = \mu_1 \mu_0 q_n B / E_u$$

$\mu_0$	$\mu_1$	$E_{uave}$	q	$\delta_i$
0,93	0,36	105	164,73	11,08
0,92	0,24	191,79	84,44	3,07

$$\delta_{i\ ave} = 14,16 \text{ mm}$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)]$$

$$D/(LB)^{0.5} = 0,374 \rightarrow \mu_d = 0,9$$

$$\text{London Clay} \rightarrow \mu_g = 0,7$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g$$

$E_{mid-dr}$	$m_v$	$\sigma_z$	$\delta_c$
77	0,01269	97,190	16,40
140,646	0,00695	31,298	2,89

$$\delta_c = 19,29 \text{ mm}$$

$$\delta_T = \delta_{i\ ave} + \delta_c = 33,45 \text{ mm}$$

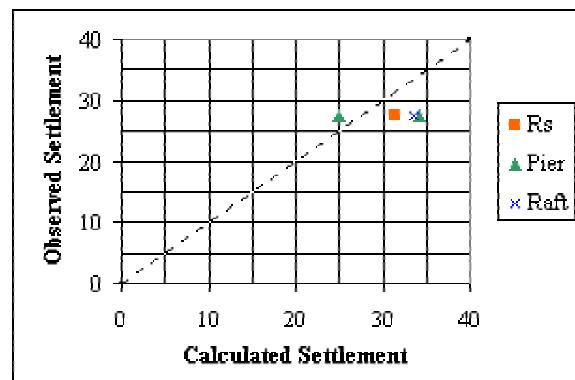
$$\delta_{mea.} = 27,5 \text{ mm}$$

**Table A.25:** Measured and computed settlements for Cambridge Road (mm)

Set. Ratio		Settlement (mm)										Mea.	
		Equivalent Pier				Equivalent Raft							
		d <sub>e1</sub>		d <sub>e2</sub>		H=32 m	H=42,2 m	H=32 m (at the tip)	H=38,8 m (1/6)	H=37,1 m (1/8)			
vs=0,1	31,42	24,89	34,24	42,70	47,95	26,15	33,46	30,43	35,68	37,3	27,5		
		42,42		58,88									
vs=0,3	26,61	17,09	28,97	33,90	40,57	20,99	26,56	24,96	28,35	29,62	27,5		
		35,93		50,91									

Cambridge

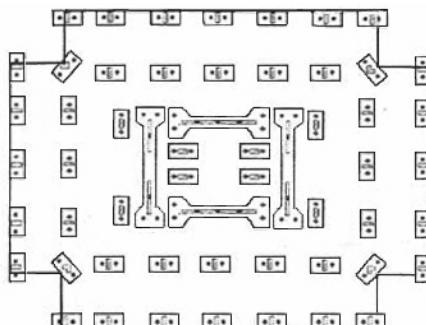
Rs	31,42	Mea.	27,5
Pier	24,89		
	34,24		
Raft	33,46		



**Figure A.50:** Measured and computed settlements for Cambridge Road (mm)

## 25. 19-Storey Reinforced Concrete Building (n=132)

The building was constructed in the USA in the period 1967 to 1970; the overall dimensions in plan area 34 m \* 24 m. It is founded on 132 permanently cased driven piles with expanded base with a length of 7.6 m, a shaft diameter of 0.41 m and a base diameter of 0.76 m. The subsoil consists essentially of cohesionless soils, with a layer of highly compressible organic silt between depths of 3 and 7 below the ground surface. In this case, the LE (Randolph (1994)) and NL (GRUPPALO) analyses grossly underestimate the actual values of the settlement. 25.1 mm (LE) and 27.8 mm (NL) settlement predictions are obtained. (Mandolini, A., and Viggiani, C., 1997, Randolph, M.F., and Guo, W.D., 1999)

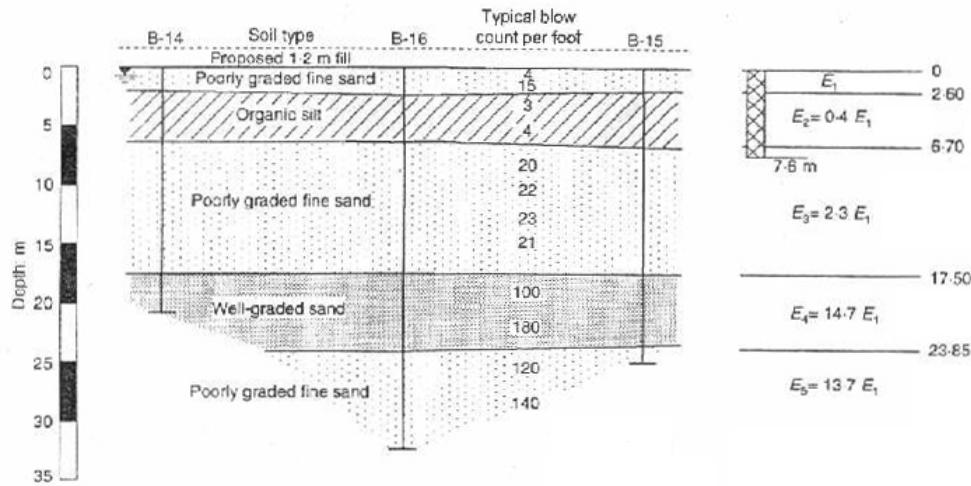


**Figure A.51:** Layout of the foundations of the building; overall dimensions are 33.6 m \* 24.4 m (Mandolini and Viggiani, 1997, Randolph and Guo, 1999)

### a) Settlement Ratio Method

$$n = 132 \quad r_b = 0.38 \text{ m} \quad r_0 = 0.205 \text{ m}$$

$$L = 7.6 \text{ m} \quad s \approx 2.5 \text{ m}$$



**Figure A.52:** Typical soil profile and properties at the building site; the subsoil model adopted in the analysis is shown on the right-hand side (Mandolini and Viggiani, 1997, Randolph and Guo, 1999)

$$E_1 = 21 \text{ MN/m}^2 \quad E_p = 25000 \text{ MN/m}^2$$

$$v_s = 0,3 \quad v_s = 0,4$$

$$P = 158,4 \text{ MN}$$

$$\lambda = E_p/G_I = 25000/16,1 \approx 1552,795$$

$$\rho = G_{I/2}/G_I = 0,372 \rightarrow 0,92$$

$$\log \lambda = 3,191 \rightarrow 1,03$$

$$s/d = 6 \rightarrow 0,825$$

$$L/d = 18,53 \rightarrow 0,532$$

$$v_s = 0,3 \rightarrow 1$$

$$v_s = 0,4 \rightarrow 0,97$$

$$\eta_w = n^{-e} \quad R_s = n^e$$

$$\zeta = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming et al., 1992})$$

$$\eta = r_b/r_0 = 1,853 \quad \xi = G_l/G_b = 1$$

$$\mu L = (2/(\lambda\zeta))^{0.5} L/r_0$$

$$P_{\text{single}} = 158400/132 = 1200 \text{ KN}$$

	$e$	$\eta_w$	$R_s$	$\zeta$	$\mu L$	$\tanh \mu L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s = 0,3$	0,415	0,131	7,619	3,185	0,745	31,451	31,556
$v_s = 0,4$	0,403	0,139	7,169	3,031	0,764	31,219	33,800

	$P_t/w_t$	$K = n\eta_w k$	$\delta = P/K(\text{mm})$	$P_{\text{single}}/k$	$\delta = \delta_s R_s$
$v_s = 0,3$	104,153	1804,255	87,79	11,52	87,79
$v_s = 0,4$	111,559	2053,94	77,12	10,75	77,12

$$\delta_{\text{measured}} = 64 \text{ mm}$$

### b) Equivalent Pier Method

$$B = A_G^{0.5} = 28,632 \text{ m}$$

$$A_p = \pi d^2 n / 4 = 17,427 \text{ m}^2$$

$$E_p = 25000 \text{ MPa}$$

$$E_s' = 41,86 \text{ MPa} \quad E_u = 48,3 \text{ MPa}$$

$$d_e = 1,27 A_G^{0.5} = 36,36 \text{ m (for friction piles)}$$

$$\rho = 0,372 \quad L = 7,6 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-v) L / r_0) \quad (\text{W. Fleming et al., 1992})$$

$$\zeta_2 = \ln / \{ 5 + [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L/r_0 \} \quad (\text{K. Horikoshi, M. Randolph, 1999})$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,3$	572,395	35,552	-1,299				
			1,662	0,076	0,208	0,842	87,69
$v_s=0,4$	575,547	35,748	-1,453				
			1,655	0,076	0,208	0,790	76,41

### Method 2

$$L/d_e = 7,6/36,33 = 0,208 \rightarrow I_\delta = 0,5 \quad (\text{Fig. 2.10})$$

	$v_s=0,3$	$v_s=0,4$
$\delta \text{ (mm)}$	52,03	48,31

$$K \approx 520 \text{ (pile stiffness factor)} \quad s/d \approx 6 \quad L/d \approx 18,53 \quad B=28,63 \text{ m}$$

$$d_e/B \approx 0,8 \text{ assumed, then } d_e \approx 22,90 \text{ m (Fig. 2.9)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,3$	572,395	35,552	-0,837				
			1,692	0,121	0,330	0,811	133,98
$v_s=0,4$	575,547	35,748	-0,991				
			1,681	0,121	0,330	0,767	117,66

## Method 2

$$L/d_e = 7,6 / 22,90 = 0,331 \rightarrow I_\delta = 0,5 \text{ (Fig. 2.10)}$$

$\delta$ (mm)	$v_s = 0,3$	$v_s = 0,3$
	82,59	76,69

$$\delta_{\text{measured}} = 64 \text{ mm}$$

### c) Equivalent Raft Method

L	B	H	D	D/B	L/B	H/B	z/B
36,53	26,53	1,63	5	0,190	1,377	0,061	0,030
38,41	28,41	10,8	6,7	0,235	1,352	0,380	0,2646

$$P = 158400 \text{ KN}$$

$$\delta_i \text{ ave} = \mu_1 \mu_0 q_n B / E_u$$

$\mu_0$	$\mu_1$	$q_n$	B	$E_u$	$\delta_i$
0,96	0,01	163,44	26,53	8,4	4,95
0,96	0,13	145,15	28,41	48,3	10,65

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)]$$

$$D/(LB)^{0,5} = 0,162 \rightarrow \mu_d = 0,975$$

$$\text{Sand} \rightarrow \mu_g = 1$$

$$N=22 \quad q_c/N=5 \quad M=5q_c$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g$$

$\sigma_z/q$	$\sigma_z$	$m_v$	$\delta_c$
0,97	158,54	0,102	25,71
0,74	120,94	0,018	22,92

$$\delta_T = \delta_i + \delta_c = 64,24 \text{ mm}$$

$$\delta_{\text{measured}} = 64 \text{ mm}$$

**Table A.26:** Measured and computed settlements for 19-Storey Reinforced Concrete Building (mm)

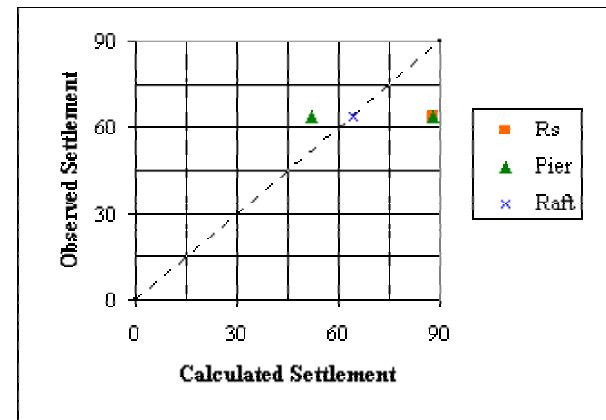
Set. Ratio	Settlement (mm)						Mea.	
	Equivalent Pier				Eq. Raft			
	d <sub>e1</sub>		d <sub>e2</sub>					
	Met1	Met2	Met1	Met2	Ave.			
vs=0,3	87,79		52,03		82,59	64,24	64	
		87,69		133,98				
vs=0,4	77,12		48,31		76,69	53,53		
		76,41		117,66				

19 - Storey Reinforced Concrete

Rs      87,79      Mea.      64

Pier      87,69  
          52,03

Raft      64,24



**Figure A.53:** Measured and computed settlements for 19-Storey Reinforced Concrete Building (mm)

## **26. Hotel Japan (n=157)**

The steel frame structure has up to 21 storeys above ground level (125 m in height) and generally a 3-storey basement, increasing to 4 storeys (19 m depth) beneath the tower. The plan area of the building complex is about 3300 m<sup>2</sup>. The raft thickness varies from 2.0 m to 3.7 m, and the 157 cast-in-place piles (1.0-1.8 m diameter) were designed to carry the entire building load. Modelling of piled raft foundation as beam grillage supported on springs of variable stiffness, average settlement is calculated between 20-25 mm (Nagao, T., and Majima, M., 2000)

### **a) Settlement Ratio Method**

$$n = 157 \quad d = 1,5 \text{ m} \quad r_0 = 0,75 \text{ m}$$

$$L = 20 \text{ m} \quad s = 2 \text{ m}$$

$$\text{Depth: } 32-38 \text{ m} \quad E_u = 87,2 \text{ MN/m}^2$$

$$38-65 \text{ m} \quad E_u = 129,0 \text{ MN/m}^2$$

$$65-105 \text{ m} \quad E_u = 245,0 \text{ MN/m}^2$$

$$E_p = 35000 \text{ MN/m}^2$$

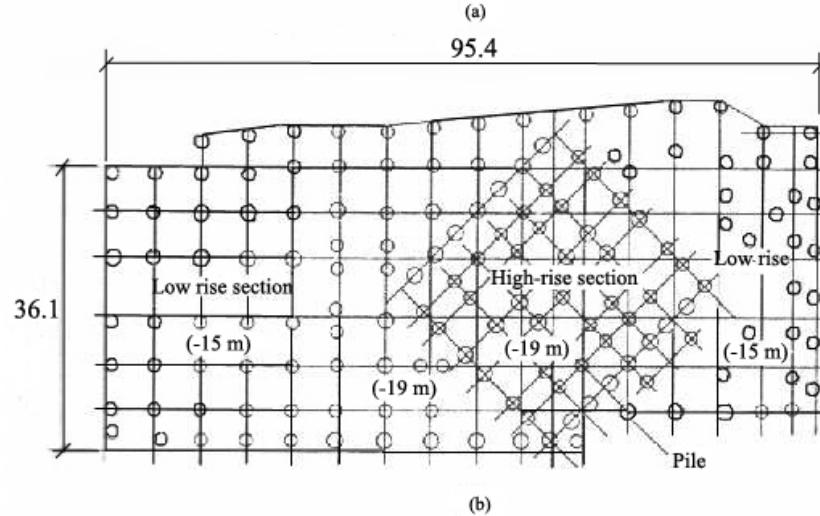
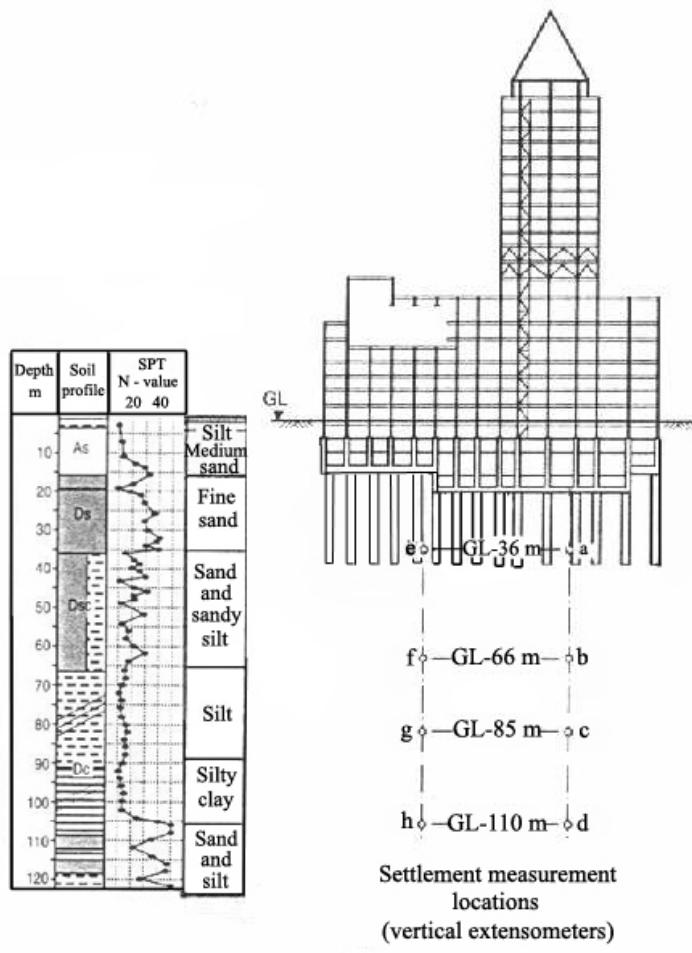
$$v_s = 0,33$$

$$P = 196,250 \text{ MN}$$

$$\lambda = E_p/G_l = 35000/43 \approx 813,95$$

$$\rho = G_{l/2}/G_l = 0,675 \rightarrow 0,975$$

$$\log \lambda = 2,91 \rightarrow 0,97$$



**Figure A.54:** Building complex in Nigita City, Japan; **(a)** longitudinal cross-section and soil profile; **(b)** foundation plan (Nagao and Majima, 2000)

$$s/d=2 \rightarrow 1,09$$

$$L/d=13,33 \rightarrow 0,518$$

$$v_s=0,33 \rightarrow 0,99$$

$$\eta_w = n^{-e} \quad R_s = n^e$$

$$\zeta = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et al, 1992})$$

$$\eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 1$$

$$\mu L = (2/(\lambda\zeta))^{0,5} L/r_0$$

$$P_{\text{single}} = 196250/157 = 1250 \text{ KN}$$

	$e$	$\eta_w$	$R_s$	$\zeta$	$\mu L$	$\tan \mu L L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s = 0,33$	0,528	0,069	14,483	3,407	0,716	22,882	32,737

	$P_t / w_t$	$K = n \eta_w k$	$\delta = P/K(\text{mm})$	$P_{\text{single}}/k$	$\delta = \delta_s R_s$
$v_s = 0,33$	1055,78	11444,94	17,14	1,184	17,14

$$\delta_{\text{measured}} = 17,5 \text{ mm}$$

### b) Equivalent Pier Method

$$B = A_G^{0,5} = 58,68 \text{ m}$$

$$A_p = \Pi d^2 n / 4 = 277,44 \text{ m}^2$$

$$E_p = 35000 \text{ MPa}$$

$$E_s' = 114,38 \text{ MPa} \quad E_u = 129 \text{ MPa}$$

$$d_e = 1,27 \text{ A}_G^{0,5} = 74,53 \text{ (for friction piles)}$$

$$\rho = 0,675 \quad L = 20 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-\nu) L / r_0) \text{ (W. Fleming, et al., 1992)}$$

$$\zeta_2 = \ln / \{5 + [0,25 + (2,5 \rho (1-\nu) - 0,25) \xi] L / r_0\} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s = 0,33$	2924,75	68,017	-0,498				
			1,724	0,070	0,267	0,740	17,05

### Method 2

$$L/d_e = 20/74,53 = 0,268 \rightarrow I_\delta = 0,5 \text{ (Fig. 3.10)}$$

$$\delta = 11,51 \text{ mm}$$

$$K \approx 270 \text{ (pile stiffness factor)} \quad s/d \approx 2 \quad L/d \approx 13,33 \quad B = 58,68 \text{ m}$$

$$d_e/B \approx 0,88 \text{ assumed, then } d_e \approx 51,64 \text{ m (Fig. 2.9)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s = 0,33$	2924,75	68,017	-0,131				
			1,771	0,099	0,385	0,694	23,08

## Method 2

$$L/d_e = 20/51,64 = 0,387 \rightarrow I_\delta = 0,5 \text{ (Fig. 2.10)}$$

$$\delta = 11,51 \text{ mm}$$

$$\delta_{\text{measured}} = 17,5 \text{ mm}$$

### c) Equivalent Raft Method

L	B	H	D	$\sigma_z/q$	$\sigma_z$	$E_s'$	$m_v$
102,1	42,76	6	32	0,93	41,82	77,31	0,014
109	49,68	27	38	0,64	28,78	114,38	0,018
140,2	80,85	40	65	0,29	13,04	217,23	0,003

$$D/(LB)^{0,5} = 0,484 \rightarrow m_d = 0,855$$

$$\text{Fine sand} \rightarrow \mu_g = 1$$

$$\text{Silt, silty clay} \rightarrow \mu_g = 0,7$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)]$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g = 3,00 + 11,96 + 0,97$$

$$= 15,93 \text{ mm}$$

$\mu_0$	$\mu_1$	$E_{\text{uave}}$	q	$\delta_i$
0,925	0,04	87,2	39,457	0,71
0,925	0,2	129	31,805	2,26
0,92	0,17	245	15,196	0,78

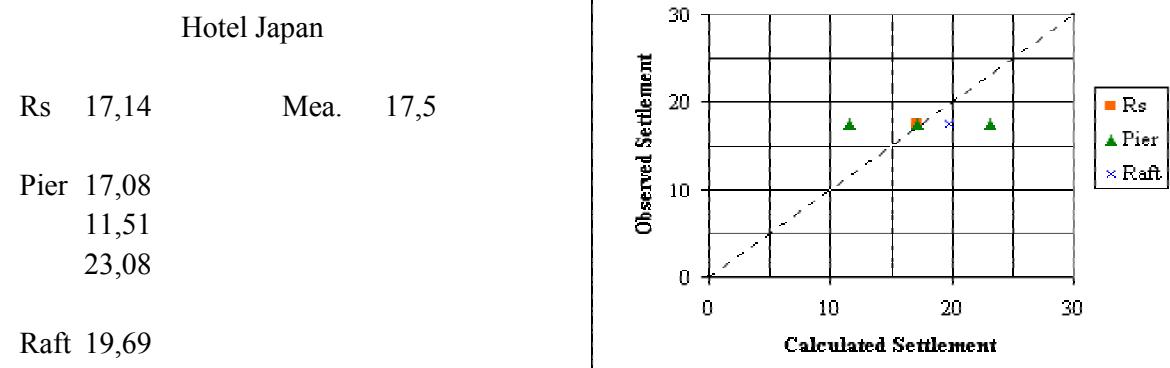
$$\delta_i = q_n B \mu_0 \mu_1 / E_u = 3,76 \text{ mm}$$

$$\delta_T = \delta_i + \delta_c = \boxed{19,69 \text{ mm}}$$

$$\delta_{\text{measured}} = 17,5 \text{ mm}$$

**Table A.27:** Measured and computed settlements for Hotel-Japan (mm)

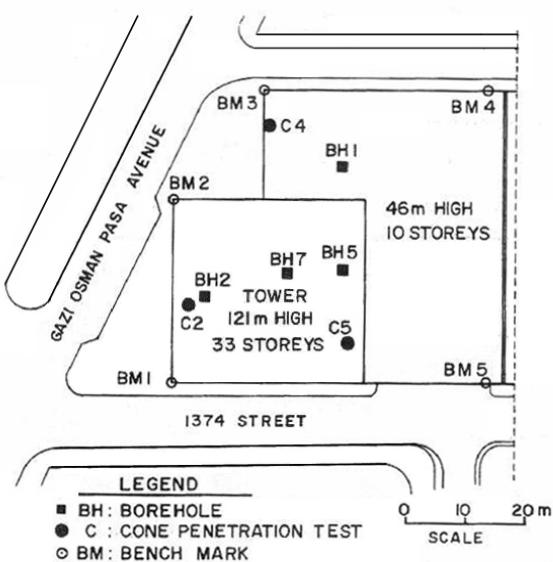
Settlement (mm)								
Set. Ratio		Equivalent Pier				Eq. Raft	Mea.	
		d <sub>e1</sub>		d <sub>e2</sub>				
		Met1	Met2	Met1	Met2	Ave		
v <sub>s</sub> =0,33	17,14	—	17,05	11,51	—	16,61	19,69	17,50
					23,08			



**Figure A.55:** Measured and computed settlements for Hotel-Japan (mm)

## 27. Izmir Hilton Complex (n=189)

The construction of the Izmir Hilton Complex founded on a single raft supported by piles. The soil profile indicates that the foundation soils are deep stiff clays containing sand-gravel layers except the upper 15 m where fills and soft and loose to medium dense recent alluvial deposits lie. These include sands, silts and clays. The ground water level is 3 m deep from the ground surface. There are 189 piles under the raft, 138 of them under the tower block. Foundation piles under the raft were bored piles 1.20 m in diameter when cased (1.06 m uncased). The ends of piles were located at depths of 33 m to 42 m from the ground surface. The closest spacing of the piles under the tower is 3.00 m by 2.50 m. Settlement of the piled raft has been estimated independently using the group interaction analysis, and the group settlement is obtained as 74.5 mm. (Ergun, M. U., 1995)



**Figure A.56:** Plan view of the tower and the site (Ergun, 1995)

**Table A.28:** Summary of soil properties (Ergun, 1995)

Sym.	Description	Engineering Properties
GS	Gravelly sand, contains silty and clayey bands	N=20-36 N=4 Clay bands $q_c=4-12 \text{ MPa}$
C1	Sand silty clay soft to firm black and grey	N=2-5 $q_c=0,6-0,9 \text{ MPa}$ $C_u=30 \text{ kPa}$ (UU Tests) $m_v=0,05-0,06*10^{-2} \text{ m}^2/\text{kN}$ (100-400 kPa Interval)
C	Silty clay light brown contains some gravel	N=20 (15m-40m) $q_c=1,5-2 \text{ MPa}$ (15m-35m) N=29 (40m 63m) $C_u=80-120 \text{ kPa}$ (UU Tests, 0-30m) $m_v=0,01-0,02*10^{-2} \text{ m}^2/\text{kN}$ (100-400 kPa)
SG	Sandy gravel gray	N=36 $q_c=16-20 \text{ MPa}$

**a) Settlement Ratio Method**

$$n = 189 \quad d = 1,06 \text{ m} \quad r_0 = 0,53 \text{ m}$$

$$L = 28,5 \text{ m} \quad s = 2,756 \text{ m}$$

$$v_s = 0,2 \quad v_s = 0,3 \quad E_p = 30000 \text{ MN/m}^2$$

$$P = 819315 \text{ KN}$$

$$\lambda = E_p / G_l = 30000 / 50 \approx 600$$

$$\rho = G_{l/2} / G_l = 30 / 50 = 0,6 \rightarrow 0,955$$

$$\log \lambda = 2,778 \rightarrow 0,945$$

$$s/d = 2,6 \rightarrow 1,04$$

$$L/d_{ave} = 26,9 \rightarrow 0,547$$

$$v_s=0,2 \rightarrow 1,03$$

$$v_s=0,3 \rightarrow 1$$

$$\eta_w = n^{-e} \quad R_s = n^e$$

$$\zeta = \ln(2,5 \rho (1-v) L/r_0) \text{ (W. Fleming, et al., 1992)}$$

$$\eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 1$$

$$\mu L = (2/(\lambda\zeta))^{0.5} L/r_0$$

$$P_{\text{single}} = 819315/189 = 4335 \text{ KN}$$

	e	$\eta_w$	R_s	$\zeta$	$\mu L$	$\tanh \mu L L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s=0,2$	0,528	0,062	15,988	4,167	1,520	32,134	31,395
$v_s=0,3$	0,513	0,067	14,748	4,034	1,545	31,763	32,291

	$P_t/w_t$	K=n $\eta_w k$	$\delta = P/K(\text{mm})$	$P_{\text{single}}/k$	$\delta = \delta_s R_s$
$v_s=0,2$	831,975	9835,013	83,30	5,21	83,30
$v_s=0,3$	855,729	10966,37	74,71	5,06	74,71

$$\delta_{\text{measured}} = 69,6 \text{ mm}$$

## b) Equivalent Pier Method

$$B = A_G^{0.5} = 51,3 \text{ m}$$

$$A_p = \pi d^2 n / 4 = 166,78 \text{ m}^2$$

$$E_p = 30000 \text{ MPa}$$

$$E_s' = 120 \text{ MPa} \quad E_u = 150 \text{ MPa}$$

$$d_e = 1,27 \text{ A}_G^{0,5} = 65,15 \text{ m (for friction piles)}$$

$$\rho = 0,6 \quad L = 28,5 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-\nu) L / r_0) \text{ (W. Fleming, et al., 1992)}$$

$$\zeta_2 = \ln / \{5 + [0,25 + (2,5 \rho (1-\nu) - 0,25) \xi] L / r_0\} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s = 0,2$	2013,65	40,272	0,048	0,883	0,350	0,083	8,71
			1,800	0,145	0,434	0,728	76,29
$v_s = 0,3$	2023,01	40,460	-0,084				
			1,778	0,145	0,434	0,715	69,17

### Method 2

$$L/d_e = 28,5/65,15 = 0,437 \rightarrow I_\delta = 0,5 \text{ (Fig. 2.10)}$$

$\delta$ (mm)	$v_s = 0,2$	$v_s = 0,3$
	52,39	46,36

$$K \approx 220 \text{ (pile stiffness factor)} \quad s/d \approx 2,6 \quad L/d \approx 26,88 \quad B = 51,3 \text{ m}$$

$$d_e/B \approx 0,8 \text{ assumed, then } d_e \approx 41,04 \text{ m (Fig. 2.9)}$$

## Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,2$	2013,65	40,272	0,510	0,433	0,654	0,344	57,31
			1,897	0,224	0,683	0,655	109,10
$v_s=0,3$	2023,01	40,460	0,377	0,502	0,641	0,296	45,57
			0,865	0,226	0,682	0,651	100,01

## Method 2

$$L/d_e = 28,5/41,04 = 0,694 \rightarrow I_\delta = 0,47 \text{ (Fig. 2.10)}$$

	$v_s=0,2$	$v_s=0,3$
$\delta \text{ (mm)}$	78,19	72,17

$$\delta_{\text{measured}} = 69,6 \text{ mm}$$

## c) Equivalent Raft Method

$$L=64,5 \text{ m} \quad B=57,35 \text{ m} \quad H=114,7 \text{ m}$$

$$L/B=1,124 \quad D/B=0,331 \quad H/B=2$$

$$P=819315 \text{ KN} \quad q_n=P/(B*L) = 221,49 \text{ KN}$$

$$E_u=150 \text{ Mpa} \quad E_s'=120 \text{ Mpa} \quad v_s=0,2$$

$$\mu_1 = 0,52 \quad \mu_0 = 0,95$$

$$\delta_{\text{ave}}=\mu_1 \mu_0 q_n B/E_u = 0,95 \cdot 0,52 \cdot 221,49 \cdot 57,35 / 150 = 41,83 \text{ mm}$$

$$m_v=[(1+v)(1-2v)]/[E_s'(1-v)] \approx 0,0075$$

$$z/B = 1 \quad \sigma_z/q = 0,294 \quad \sigma_z = 65,118 \text{ kN/m}^2$$

$$D/(LB)^{0.5} = 0,312 \rightarrow \mu_d = 0,92$$

$$\text{Stiff Clay} \rightarrow \mu_g = 0,7$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g = 0,0075 \cdot 65,118 \cdot 114,7 \cdot 0,92 \cdot 0,7 = 36,07 \text{ mm}$$

$$\delta_T = \delta_i + \delta_c = 77,91$$

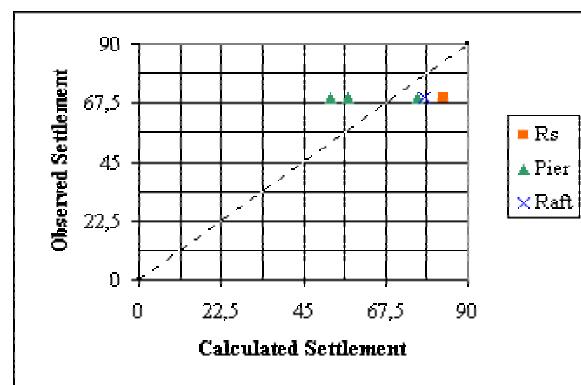
$$\delta_{\text{measured}} = 69,6 \text{ mm}$$

**Table A.29:** Measured and computed settlements for Izmir Hilton (mm)

Set. Ratio		Settlement (mm)						Mea.	
		Equivalent Pier			Equivalent Raft				
		d <sub>e1</sub>	d <sub>e2</sub>	Met1	Met2	H=96 m	H=114,7 m		
		Met1	Met2	Met1	Met2	Ave.	Ave.		
$v_s=0,2$	83,30	8,71	52,39	57,31		78,19	74,11	77,91	
		76,29		109,10					
$v_s=0,3$	74,71		48,36	45,57		72,17	66,04	69,32	
		69,17		100,01					

Izmir Hilton

Rs	83,3	Mea.	69,6
Pier	76,29		
	52,39		
	57,31		
Raft	77,91		



**Figure A.57:** Measured and computed settlements for Izmir Hilton (mm)

## 28. Frame-Type Building 6 (n=192)

The building is 18 m square in plan, and is located on 192 piles with a length of 21 m. Shingle,  $E_u=80$  Mpa, is located under 35\*35 cm section piles. The over load on the foundation is 268,8 MN. The piles in the group are arranged in 1,3 m spacing. Different formulations are used to obtain settlement value. Settlement predictions and methods are given below:

USSR standarts    Poulos    Vesic    Skempton    Bartolomey:

20 mm      71 mm      67 mm      108 mm      24 mm

(Bartolomey, A.A., 1981)

### a) Settlement Ratio Method

$$n = 192 \quad d = 0,394 \text{ m} \quad r_0 = 0,197 \text{ m}$$

$$L = 21 \text{ m} \quad s = 1,3 \text{ m}$$

$$E_u = 80 \text{ MN/m}^2 \quad \text{Shingle} \quad E_p = 25000 \text{ MN/m}^2$$

$$P = 268,8 \text{ MN} \quad v_s = 0,35 \quad v_s = 0,4$$

$$\lambda = E_p/G_l = 25000/26,7 \approx 936,329$$

$$\rho = G_{l/2}/G_l = 1 \rightarrow 1,06$$

$$\log \lambda = 2,971 \rightarrow 0,99$$

$$s/d = 3,3 \rightarrow 0,98$$

$$L/d = 53,299 \rightarrow 0,548$$

$$v_s = 0,35 \rightarrow 0,98$$

$$v_s = 0,4 \rightarrow 0,97$$

$$\eta_w = n^{-e} \quad R_s = n^e \quad \eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 1$$

$$\zeta = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et al, 1992})$$

$$\mu L = (2/(\lambda \zeta))^{0.5} L/r_0$$

$$P_{\text{single}} = 268800/192 = 1400 \text{ KN}$$

	e	$\eta_w$	R_s	$\zeta$	$\mu L$	$\tan \mu L L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s = 0,35$	0,552	0,054	18,241	5,155	2,169	47,859	58,623
$v_s = 0,4$	0,546	0,056	17,71	5,075	2,187	47,528	59,144

	$P_t/w_t$	$K = n \eta_w k$	$\delta = P/K(\text{mm})$	$P_{\text{single}}/k$	$\delta = \delta_s R_s$
$v_s = 0,35$	308,351	3245,519	82,82	4,54	82,82
$v_s = 0,4$	311,093	3372,85	79,69	4,50	79,69

$$\delta_{\text{measured}} = 19 \text{ mm}$$

### b) Equivalent Pier Method

$$B = A_G^{0.5} = 18$$

$$A_p = \pi d^2 n / 4 = 4,712 \text{ m}^2$$

$$E_p = 25000 \text{ MPa}$$

$$E_s' = 72 \text{ MPa} \quad E_u = 80 \text{ MPa}$$

$$d_e = 1,13 A_G^{0.5} = 20,34 \text{ (for end-bearing piles)}$$

$$\rho = 1 \quad L = 21 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et al, 1992})$$

$$\zeta_2 = \ln/\{5+[0,25+(2,5 \rho (1-v)-0,25)\xi] L/r_0\} \quad (\text{K. Horikoshi, M. Randolph, 1999})$$

### Method 1

	E <sub>e</sub>	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,35$	1873,051	70,239	1,210	0,316	0,999	0,344	63,31
			2,123	0,239	1,013	0,469	86,17
$v_s=0,4$	1875,525	70,332	1,130	0,327	0,997	0,334	59,20
			2,091	0,240	1,012	0,465	82,47

### Method 2

$$L/d_e = 21/20,34 = 1,032 \rightarrow I_\delta = 0,415 \quad (\text{Fig. 2.10})$$

$\delta \text{ (mm)}$	$v_s=0,35$	$v_s=0,4$
	76,17	73,45

$$K \approx 300 \text{ (pile stiffness factor)} \quad s/d \approx 3,3 \quad L/d \approx 53,29 \quad B = 18 \text{ m}$$

$$d_e/B \approx 0,7 \text{ assumed, then } d_e \approx 12,6 \text{ m} \quad (\text{Fig. 2.9})$$

### Method 1

	E <sub>e</sub>	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tan \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,35$	1873,051	70,239	1,689	0,432	1,569	0,329	97,59
			2,343	0,367	1,595	0,399	118,45
$v_s=0,4$	1875,525	70,332	1,609	0,443	1,565	0,324	92,70
			2,302	0,370	1,594	0,399	114,12

## **Method 2**

$$L/d_e = 21/12,6 = 1,667 \rightarrow I_\delta = 0,33 \quad (\text{Fig. 2.10})$$

$\delta$ (mm)	$v_s = 0,35$	$v_s = 0,4$
	97,77	94,28

$$\delta_{\text{measured}} = 19 \text{ mm}$$

### **c) Equivalent Raft Method**

$$L=18 \quad B=18 \quad L/B=1$$

$$H=36 \quad D=21 \quad D/B=1,667 \quad H/B=2$$

$$\mu_0=0,91 \quad \mu_1=0,53$$

$$q_n = 268800/(BL) = 829,63 \text{ KPa}$$

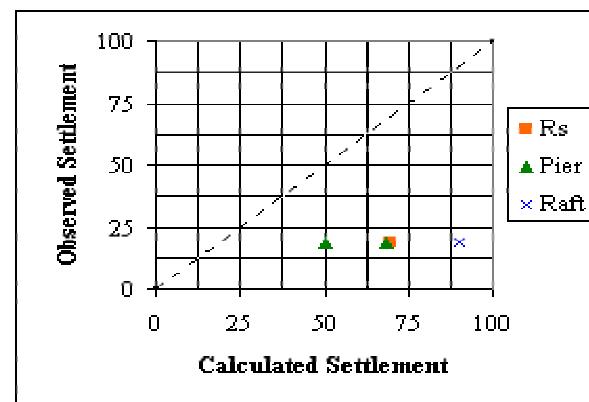
$$\delta_{\text{ave}} = q_n \mu_0 \mu_1 B / E_u = 829,63 \cdot 0,91 \cdot 0,53 \cdot 18 / 80 = 90,03$$

$$\delta_{\text{measured}} = 19 \text{ mm}$$

**Table A.30:** Measured and computed settlements for Frame Type Building 6 (mm)

Set. Ratio		Settlement (mm)						Mea.				
		Equivalent Pier				Eq. Raft						
		d <sub>e1</sub>		d <sub>e2</sub>								
		Met1	Met2	Met1	Met2							
vs=0,35	82,82	63,31	76,17	97,59	97,77	Ave.	90,03	19,00				
		86,17		118,45								
vs=0,4	79,69	59,20	73,45	92,70	94,28							
		82,47		114,12								

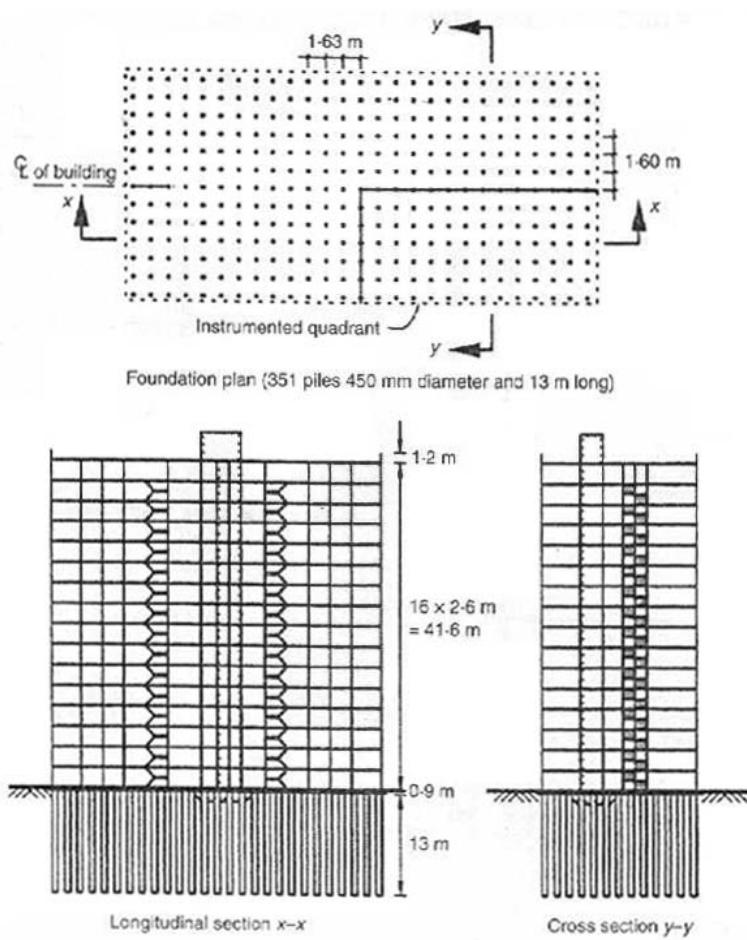
Frame 6 (Shingle)			
Rs	79,69	Mea.	19
Pier	82,47		
	73,45		
Raft	90,03		



**Figure A.58:** Measured and computed settlements for Frame Type Building 6 (mm)

## 29. Stonebridge Park Flats (n=351)

16-storey block of flats built at Stonebridge Pak in London borough of Brent. The actual foundation involved the use of a raft 0.9 mm thick, with 351 piles, 450 mm diameter and 13 m long, driven into London clay. The stiffness of the pile group is estimated, using program PIGLET (simplified continuum analysis), and the average settlement under a load of 156 MN may be calculated as 27 mm. (H.G. Poulos 2001, W.G.K. Fleming, et al. 1992)



**Figure A.59:** Stonebridge foundation details (Poulos, 2001, Fleming et al, 1992)

### a) Settlement Ratio Method

$$n = 351 \quad d = 0,45 \text{ m} \quad r_0 = 0,225 \text{ m}$$

$$L = 13 \text{ m} \quad s = 1,60-1,63 \text{ m}$$

$$G = 1,44z+20 \text{ (MN/m}^2\text{)} \quad \text{London Clay} \quad E_p = 25000 \text{ MN/m}^2$$

$$P = 156 \text{ MN} \quad v_s = 0,1 \quad v_s = 0,3$$

$$\lambda = E_p/G_l = 25000/38,72 \approx 645,66$$

$$\rho = G_{l/2}/G_l = 0,758 \rightarrow 1$$

$$\log \lambda = 2,810 \rightarrow 0,95$$

$$s/d = 3,58 \rightarrow 0,96$$

$$L/d = 28,89 \rightarrow 0,548$$

$$v_s = 0,1 \rightarrow 1,05$$

$$v_s = 0,3 \rightarrow 1$$

$$\eta_w = n^e \quad R_s = n^e$$

$$\zeta = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et al., 1992})$$

$$\eta = r_b/r_0 = 1 \quad \xi = G_l/G_b = 1$$

$$\mu L = (2/(\lambda \zeta))^{0,5} L/r_0$$

$$P_{\text{single}} = 156000/351 = 444,4 \text{ KN}$$

	$e$	$\eta_w$	$R_s$	$\zeta$	$\mu L$	$\tanh \mu L L / (\mu L r_0)$	$P_f / (w_t G_l r_0)$
$v_s = 0,1$	0,524	0,046	21,661	4,591	1,500	34,851	37,731
$v_s = 0,3$	0,499	0,053	18,710	4,339	1,543	34,162	39,426

	$P_t/w_t$	$K=n\eta_w k$	$\delta=P/K(\text{mm})$	$P_{\text{single}}/k$	$\delta=\delta_s R_s$
$v_s=0,1$	328,720	5326,55	29,28	1,35	29,28
$v_s=0,3$	343,486	6443,676	24,20	1,29	24,20

$\delta_{\text{measured}}=25 \text{ mm}$

### b) Equivalent Pier Method

$$B=A_G^{0.5}=29,494 \text{ m}$$

$$A_p=\Pi d^2 n/4=55,82 \text{ m}^2$$

$$E_p=25000 \text{ MPa}$$

$$G=1,44z+20 \text{ (MN/m}^2\text{)} \quad E_s'=85,184 \text{ MPa} \quad E_u=116,16 \text{ MPa}$$

$$d_e=1,27 A_G^{0.5}=37,45 \text{ m (for friction piles)}$$

$$\rho=0,758 \quad L=13 \text{ m}$$

$$E_e=E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1=\ln(2,5 \rho (1-v) L/r_0) \text{ (W. Fleming, et al., 1992)}$$

$$\zeta_2=\ln/\{5+[0,25+(2,5 \rho (1-v)-0,25)\xi] L/r_0\} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,1$	1683,99	43,491	0,169	0,331	0,332	0,193	9,47
			1,822	0,110	0,345	0,719	35,18
$v_s=0,3$	1698,49	43,866	-0,082				
			1,778	0,111	0,345	0,707	29,24

## Method 2

$$L/d_e = 13/37,45 = 0,347 \rightarrow I_\delta = 0,5 \text{ (Fig. 2.0)}$$

	$v_s=0,1$	$v_s=0,3$
$\delta \text{ (mm)}$	24,44	20,63

$$K \approx 300 \text{ (pile stiffness factor)} \quad s/d \approx 3,58 \quad L/d \approx 28,89 \quad B=29,49 \text{ m}$$

$$d_e/B \approx 0,8 \text{ assumed, then } d_e \approx 23,59 \text{ m (Fig. 2.9)}$$

## Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,1$	1683,99	43,491	0,631	0,297	0,535	0,363	28,21
			1,928	0,170	0,546	0,638	49,52
$v_s=0,3$	1698,49	43,866	0,379	0,381	0,525	0,287	18,85
			1,865	0,172	0,545	0,639	41,99

## Method 2

$$L/d_e = 13/23,59 = 0,55 \rightarrow I_\delta = 0,5 \text{ (Fig. 2.10)}$$

	$v_s=0,1$	$v_s=0,3$
$\delta \text{ (mm)}$	38,80	32,83

$$\delta_{\text{measured}} = 25 \text{ mm}$$

### c) Equivalent Raft Method

L	B	H	L/B	H/B	D/B
47,17	23,98	23,98	1,96	1	0,36
50,15	35,97	23,98	1,64	0,66	0,90

$$P=156000 \text{ KN} \quad v_s = 0,1$$

$$\delta_{i \text{ ave}} = \mu_1 \mu_0 q_n B / E_u$$

$\mu_0$	$\mu_1$	$E_{uave}$	q	$\delta_i$
0,95	0,35	149,38	137,94	7,36
0,92	0,23	252,97	73,32	2,20

$$\delta_{i \text{ ave}} = 9,56 \text{ mm}$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)]$$

$$D/(LB)^{0,5} = 0,258 \rightarrow \mu_d = 0,94$$

$$\text{London Clay} \rightarrow \mu_g = 0,7$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g$$

$E_{\text{mid-dr}}$	$m_v$	$\sigma_z$	$\delta_c$
109,54	0,0089	84,14	11,85
304,77	0,0052	27,58	2,29

$$\delta_c = 14,14 \text{ mm}$$

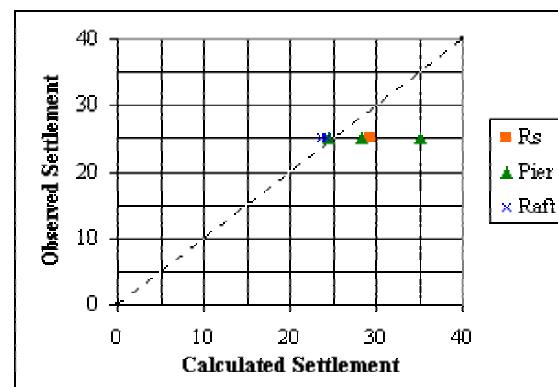
$$\delta_T = \delta_{i \text{ ave}} + \delta_c = 23,71 \text{ mm}$$

$$\delta_{\text{measured}} = 25 \text{ mm}$$

**Table A.31:** Measured and computed settlements for Stonebridge Park (mm)

		Settlement (mm)						Mea.	
Set. Ratio		Equivalent Pier				Equivalent Raft			
		d <sub>e1</sub>		d <sub>e2</sub>		H=39,3 m	H=47,96 m		
		Met1	Met2	Met1	Met2	Ave	Ave		
vs=0,1	29,28	9,47		28,21				25	
		35,18		24,44	49,52	38,80	24,33		
vs=0,3	24,21			20,68	18,85			25	
			29,24		41,99	32,83	18,83		
							18,66		

Stonebridge			
Rs	29,28	Mea.	25
Pier	35,18		
	24,44		
	28,21		
Raft	24,33		
	23,71		



**Figure A.60:** Measured and computed settlements for Stonebridge Park (mm)

### **30. Dashwood House (n=462)**

The pile group consisted of 462 bored piles with a diameter of 0,485 m and length of 15 m was capped by a rectangular raft of 33.8\*32.6 m. The piles in the group were arranged in a grid of 1.5-m square spacing. The overall load on the foundation was 279 MN. Based on the computed settlement of single pile and group settlement ratio of actual pile group, the settlement of the pile group is obtained as 36.2 mm (W.Y. Shen, Y.K. Chow and K.Y. Yong 2000)

#### **a) Settlement Ratio Method**

$$G = 30 + 1,33z \text{ (MN/m}^2\text{)} \quad \text{London Clay} \quad E_p = 30000 \text{ MN/m}^2$$

$$n = 462 \quad d = 0,485 \text{ m} \quad r_0 = 0,2425 \text{ m}$$

$$L = 15 \text{ m} \quad s = 1,5 \text{ m}$$

$$v_s = 0,15 \quad v_s = 0,3 \quad P = 279 \text{ MN}$$

$$\lambda = E_p/G_l = 30000/49,95 \approx 600$$

$$\rho = G_{l/2}/G_l = 0,8 \rightarrow 1,015$$

$$\log \lambda = 2,778 \rightarrow 0,94$$

$$s/d = 3,093 \rightarrow 0,99$$

$$L/d = 30,927 \rightarrow 0,55$$

$$v_s = 0,15 \rightarrow 1,04$$

$$v_s = 0,3 \rightarrow 1$$

$$\eta_w = n^{-e} \quad R_s = n^e$$

$$\zeta = \ln(2,5 \rho (1-\nu) L/r_0) \quad (\text{W. Fleming et al. 1992})$$

$$\eta = r_b/r_0 = 1 \quad \xi = G_p/G_b = 1$$

$$\mu L = (2/(\lambda\zeta))^{0.5} L/r_0$$

$$P_{\text{single}} = 279000/462 = 603,896 \text{ KN}$$

	$e$	$\eta_w$	$R_s$	$\zeta$	$\mu L$	$\tanh \mu L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s = 0,15$	0,540	0,036	27,521	4,656	1,654	34,753	38,87
$v_s = 0,3$	0,519	0,041	24,227	4,462	1,689	34,192	40,09

	$P_t/w_t$	$K = n\eta_w k$	$\delta = P/K(\text{mm})$	$P_{\text{single}}/k$	$\delta = \delta_s R_s$
$v_s = 0,15$	470,845	7903,998	35,29	1,28	35,29
$v_s = 0,3$	485,706	9262,208	30,12	1,24	30,12

$$\delta_{\text{measured}} = 33 \text{ mm}$$

### b) Equivalent Pier Method

$$B = A_G^{0.5} = 31,241 \text{ m}$$

$$A_p = \pi d^2 n / 4 = 85,35 \text{ m}^2$$

$$E_p = 30000 \text{ MPa}$$

$$E_s' = 114,885 \text{ MPa} \quad E_u = 149,85 \text{ MPa}$$

$$d_e = 1,27 A_G^{0.5} = 39,67 \text{ (for friction piles)}$$

$$\rho = 0,8 \quad L = 15 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-v) L/r_0) \quad (\text{W. Fleming, et al. 1992})$$

$$\zeta_2 = \ln\{5 + [0,25 + (2,5 \rho (1-v) - 0,25)\xi] L/r_0\} \quad (\text{K. Horikoshi, M. Randolph, 1999})$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,15$	2728,373	54,622	0,251	0,288	0,368	0,241	14,79
			1,838	0,106	0,376	0,694	42,47
$v_s=0,3$	2742,047	54,895	0,057	0,603	0,338	0,081	4,42
			1,801	0,107	0,376	0,681	36,92

### Method 2

$$L/d_e = 15/39,67 = 0,378 \rightarrow I_\delta = 0,5 \quad (\text{Fig. 2.10})$$

$\delta$ (mm)	$v_s=0,15$	$v_s=0,3$
	30,60	27,07

$$K \approx 200 \text{ (pile stiffness factor)} \quad s/d \approx 3,093 \quad L/d \approx 30,92 \quad B = 31,24 \text{ m}$$

$$d_e/B \approx 0,8 \text{ (Fig. 2.9) assumed, then } d_e \approx 28 \text{ m}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s=0,15$	2728,373	54,622	0,713	0,271	0,585	0,366	35,59
			1,951	0,164	0,594	0,611	59,39
$v_s=0,3$	2742,047	54,895	0,519	0,317	0,580	0,318	27,37
			1,899	0,166	0,594	0,609	52,41

## Method 2

$$L/d_e = 15/28 = 0.535 \rightarrow I_\delta = 0.5 \quad (\text{Fig. 2.10})$$

	$v_s = 0,15$	$v_s = 0,3$
$\delta \text{ (mm)}$	48,58	42,97

$$\delta_{\text{measured}} = 33 \text{ mm}$$

### c) Equivalent Raft Method

$$L = 36,985 \text{ m} \quad B = 35,485 \text{ m} \quad H = 70,97 \text{ m}$$

$$L/B = 1,042 \quad D/B = 0,281 \quad H/B = 1,719$$

$$P = 279000 \text{ KN} \quad q_n = P/(B*L) = 212,585 \text{ KN}$$

$$E_u = 271,48 \text{ MPa} \quad E_s' = 208,13 \text{ MPa} \quad v_s = 0,15$$

$$\mu_1 = 0,525 \quad \mu_0 = 0,95$$

$$\delta_{i \text{ ave}} = \mu_1 \mu_0 q_n B / E_u = 0,95 \cdot 0,525 \cdot 212,585 \cdot 35,485 / 271,48 = 13,85 \text{ mm}$$

$$m_v = [(1+v)(1-2v)]/[E_s'(1-v)] \approx 0,00455$$

$$z/B = 1 \quad \sigma_z/q = 0,32 \quad \sigma_z = 68,027 \text{ kN/m}^2$$

$$D/(LB)^{0,5} = 0,276 \rightarrow \mu_d = 0,935$$

$$\text{London Clay} \rightarrow \mu_g = 0,7$$

$$\delta_c = m_v \sigma_z H \mu_d \mu_g = 0,00455 \cdot 68,027 \cdot 70,97 \cdot 0,935 \cdot 0,7 = 14,37 \text{ mm}$$

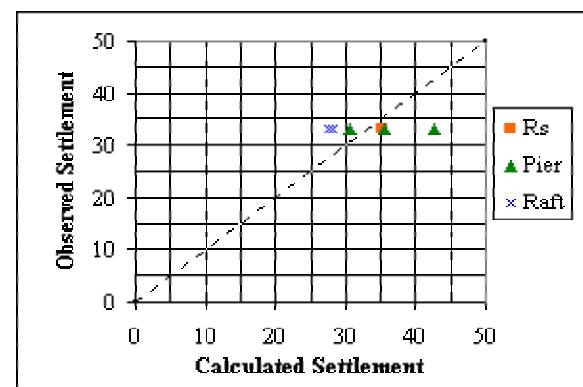
$$\delta_T = \delta_{i \text{ ave}} + \delta_c = 28,23 \text{ mm}$$

$$\delta_{\text{measured}} = 33 \text{ mm}$$

**Table A.32:** Measured and computed settlements for Dashwood House (mm)

		Settlement (mm)					
Set. Ratio		Equivalent Pier			Equivalent Raft		Mea.
		d <sub>e1</sub>		d <sub>e2</sub>	H=61 m	H=70,97 m	
		Met1	Met2	Met1	Met2	Ave.	Ave.
vs=0,15	35,29	14,79	30,6	35,59	48,58	27,57	28,23
		42,47		59,39			
vs=0,3	30,12	4,42	27,07	27,37	42,97	23,49	23,83
		36,92		52,41			

Dashwood			
Rs	35,29	Mea.	33
Pier	42,53		
	30,60		
	35,59		
Raft	27,57		
	28,23		



**Figure A.61:** Measured and computed settlements for Dashwood House (mm)

### **31. Ghent Grain Terminal (n=697)**

In 1975 a block of 40 cylindrical reinforced concrete grain silo cells was erected in Ghent, within a new terminal for storage and transit. The inner diameter of each cell is 8 m, the total height 52 m and the wall thickness 0,18 m. The foundation consists of 1.2 m thick slab, 34 m \* 84 m in plan, resting on 697 driven, cast in situ, reinforced concrete piles with a length of 13.4 m, a shaft diameter of 0.52 m and a diameter of expanded base of 0.8 m. Using the GASGROUP(using superposition principle, with interaction factors) analysis, the settlement can be estimated to be 186,3 mm and the settlement of the pile group is obtained approximately as 150 mm using the program GRUPPALO (based on the use of interaction factors). (Mandolini, A., and Viggiani, C. 1997, Poulo, H.G., 1993, Randolph, M.F., and Guo, W.D., 1999)

#### **a) Settlement Ratio Method**

$$n = 697 \quad d = 0,52 \text{ m} \quad d_{\text{base}} = 0,80 \text{ m} \quad r_0 = 0,26 \text{ m}$$

$$L = 13,4 \text{ m} \quad s = 2,08 \text{ m}$$

$$E_p = 30000 \text{ MN/m}^2$$

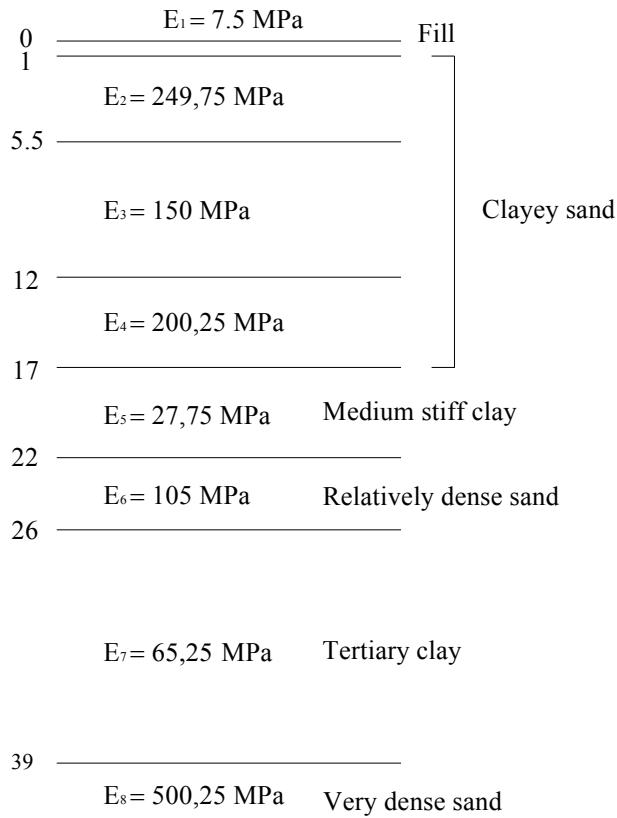
$$v_s = 0,15 \quad \text{Clayey Sand}$$

$$P = 906,1 \text{ MN}$$

$$P_{\text{single}} = 906100/697 = 1300 \text{ KN}$$

$$\lambda = E_p/G_l = 30000/66,75 \approx 449,43$$

$$\rho = G_{l/2}/G_l = 0,749 \rightarrow 1$$



**Figure A.62:** Subsoil profile and subsoil model adopted in the analysis (Mandolini and Viggiani, 1997, Poulo, 1993, Randolph and Guo, 1999)

$$\log \lambda = 2,65 \rightarrow 0,92$$

$$s/d = 4 \rightarrow 0,93$$

$$L/d = 25,77 \rightarrow 0,545$$

$$v_s = 0,15 \rightarrow 1,04$$

$$\eta_w = n^e \quad R_s = n^e$$

$$\zeta = \ln(2,5 \rho (1-v) L / r_0) \quad (\text{W. Fleming, et al., 1992})$$

$$r_m = 2,5 \rho (1-v) L \quad \eta = r_b / r_0 = 1,538 \quad \xi = G_l / G_b = 1$$

$$\mu L = (2 / (\lambda \zeta))^{0,5} L / r_0$$

	e	$\eta_w$	$R_s$	$\zeta$	$\mu L$	$\tanh \mu L / (\mu L r_0)$	$P_t / (w_t G_l r_0)$
$v_s=0,15$	0,484	0,041	23,924	4,407	1,637	29,177	33,401

	$P_t / w_t$	$K = n \eta_w k$	$\delta = P / K (mm)$	$P_{\text{single}} / k$	$\delta = \delta_s R_s$
$v_s=0,15$	579,690	16888,52	53,65	2,24	53,65

Effect of soft layers ( $E_u=27,75 - 65,25$  MPa for clay, 105 Mpa for sand )

$r_m$	$B_{\text{raft}}$	$L_{\text{raft}}$	D	H	z	$q_n$	$E_u$	$E_s'$	v
21,329	55,329	105,329	13,4	3,6	1,8	155,477	200,25	153,52	0,15
	57,129	107,129	17	5	6,1	148,049	27,75	22,2	0,2
	59,629	109,629	22	4	10,6	138,607	105	84	0,2
	61,629	111,629	26	13	19,1	131,706	65,25	52,2	0,2

$D / \sqrt{LB}$	$m_d$	$m_g$	$\sigma_z / q$	$\sigma_z$	$\mu_0$	$\mu_1$	$m_v$	$\delta_i$	$\delta_c$
0,175	0,97	0,85	0,98	152,368	0,95	0,01	0,00616		
	0,97	0,85	0,90	139,930	0,95	0,01	0,04054	2,89	23,38
	0,97	1	0,81	125,937	0,95	0,01	0,025	0,74	12,21
	0,97	0,85	0,71	110,389	0,94	0,0	0,01724	5,84	20,40

$$\delta_{\text{Total}} = 53,65 + 2,89 + 0,74 + 5,84 + 23,38 + 12,21 + 20,40 = 119,14$$

### b) Equivalent Pier Method

$$B = A_G^{0.5} = 53,44 \text{ m}$$

$$A_p = \Pi d^2 n / 4 = 148,023 \text{ m}^2$$

$$E_p = 30000 \text{ MPa} \quad E_s' = 153,525 \text{ MPa} \quad E_u = 200,25 \text{ MPa}$$

$$d_e = 1,27 A_G^{0.5} = 67,87 \text{ m} \text{ (for friction piles)}$$

$$\rho = 0,749 \quad L = 13,4 \text{ m}$$

$$E_e = E_p A_p / A_G + E_s (1 - A_p / A_G)$$

$$\zeta_1 = \ln(2,5 \rho (1-v) L/r_0) \text{ (W. Fleming, et al., 1992)}$$

$$\zeta_2 = \ln \{ 5 + [0,25 + (2,5 \rho (1-v) - 0,25) \xi] L/r_0 \} \text{ (K. Horikoshi, M. Randolph, 1999)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu L$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s = 0,15$	1700,432	25,474	-0,464				
			1,727	0,084	0,196	0,814	70,82

### Method 2

$$L/d_e = 13,4/67,87 = 0,197 \rightarrow I_\delta = 0,5 \text{ (Fig. 2.10)}$$

$$\delta = 43,48 \text{ mm}$$

$$K \approx 150 \text{ (pile stiffness factor)} \quad s/d \approx 4 \quad L/d \approx 25,77 \quad B = 53,44 \text{ m}$$

$$d_e/B \approx 0,75 \text{ assumed, then } d_e \approx 40,08 \text{ m (Fig. 2.9)}$$

### Method 1

	$E_e$	$\lambda$	$\zeta_{(1-2)}$	$\mu l$	$\tanh \mu L L / (\mu L d_e)$	$I_\delta$	$\delta$
$v_s = 0,15$	1700,432	25,474	0,062	0,750	0,283	0,100	14,75
			1,802	0,139	0,332	0,742	109,27

### Method 2

$$L/d_e = 13,4/40,08 = 0,334 \rightarrow I_\delta = 0,5 \text{ (Fig. 2.10)}$$

$$\delta = 73,62 \text{ mm}$$

Effect of soft layers ( $E_u=27,75 - 65,25$  MPa for clay, 105 Mpa for sand )

H/L	I_p	H_{k+1}/L_c	I_{p1}	E_s'	(I_k I_{p1})/E_s	$\delta$
1,2686	0,32	1,6418	0,315	22,2	0,000225	15,23
1,6417	0,315	1,9403	0,31	84	0,0000595	4,02
1,9402	0,31	2,9104	0,2	52,2	0,002107	142,49

Drained	$\delta_{total}$					
	-----	232,57	205,22	176,49	271,02	235,37

$$\delta_{measured}=185 \text{ mm}$$

### c) Equivalent Raft Method

$$P=906100 \text{ KN} \quad q_n=P/(B*L) \quad \delta_i=\mu_1\mu_0qB/E_u$$

For sand  $q_c=10 \quad M_0=40 \quad E_u=27,75 - 65,25$  MPa for clay, 105 Mpa for sand

L	B	H	D	L/B	H/B	D/B	$\mu_0$	$\mu_1$	$q_n$	E	$\delta_i$
88	38	8,07	8,93	2,315	0,212	0,235	0,96	0,06	270,96	200,25	2,96
97,31	47,31	5	17	2,056	0,105	0,359	0,95	0,03	196,91	27,75	9,56
103,08	53,08	4	22	1,942	0,075	0,414	0,94	0,01	165,60	105	0,79
107,69	57,69	13	26	1,866	0,225	0,450	0,93	0,06	145,84	65,25	7,19
											<b>20,50</b>

$$D/(LB)^{0,5}=0,154 \rightarrow \mu_d=0,975$$

$$\delta_c=m_v \sigma_z H \mu_d \mu_g$$

v	$E_{middle-dr.}$	$m_v$	$\mu_g$	$z/B$	$\sigma_z/q$	$\sigma_z$	$\delta_c$
0,15	153,525	0,006169	0,85	0,106	0,91	246,57	10,17
0,2	22,2	0,040541	0,85	0,278	0,78	211,35	35,50
0,2	84	0,025	1	0,396	0,68	184,25	17,96
0,2	52,2	0,017241	0,85	0,620	0,55	149,03	27,68
							<b>91,32</b>

$$\delta_T=\delta_i+\delta_c=111,83 \text{ mm}$$

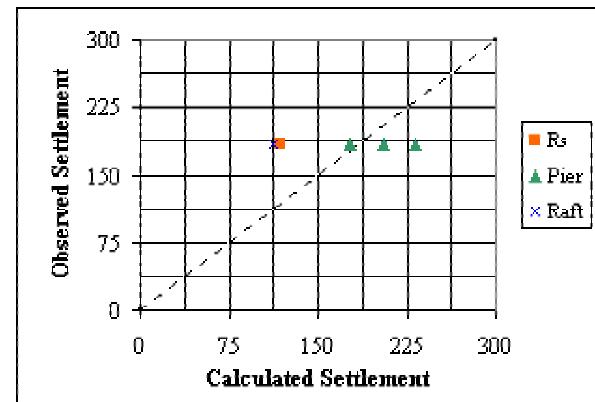
$$\delta_{measured}=185 \text{ mm}$$

**Table A.33:** Measured and computed settlements for Ghent Grain Terminal (mm)

Set. Ratio		Settlement (mm)						Mea.	
		Equivalent Pier				Eq. Raft			
		d <sub>e1</sub>		d <sub>e2</sub>					
		Met1	Met2	Met1	Met2	Ave1			
vs=0,15	119,14			205,22	176,49	235,37	111,83	185	
		232,57			271,02				

Ghent Grain

Rs	119,14	Mea.	185
Pier	232,57		
	205,22		
	176,49		
Raft	111,83		



**Figure A.63:** Measured and computed settlements for Ghent Grain Terminal (mm)